

# A comparison of optical and near-infrared colours of Magellanic Cloud star clusters with predictions of simple stellar population models

P. M. Pessev,<sup>1★</sup> P. Goudfrooij,<sup>1★</sup> T. H. Puzia<sup>2★</sup> and R. Chandar<sup>3,4★</sup>

<sup>1</sup>*Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA*

<sup>2</sup>*Herzberg Institute of Astrophysics, 5071 West Saanich Road, Victoria, BC V9E 2E7, Canada*

<sup>3</sup>*The Observatories of the Carnegie Institution of Washington, 813 Santa Barbara Street, Pasadena, CA 91101-1292, USA*

<sup>4</sup>*Department of Physics and Astronomy, The University of Toledo, 2801 West Bancroft Street, Toledo, OH 43606, USA*

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## ABSTRACT

We present integrated  $JHK_S$  Two-Micron All-Sky Survey photometry and a compilation of integrated-light optical photoelectric measurements for 84 star clusters in the Magellanic Clouds. These clusters range in age from  $\approx 200$  Myr to  $> 10$  Gyr, and have  $[\text{Fe}/\text{H}]$  values from  $-2.2$  to  $-0.1$  dex. We find a spread in the intrinsic colours of clusters with similar ages and metallicities, at least some of which is due to stochastic fluctuations in the number of bright stars residing in low-mass clusters. We use 54 clusters with the most-reliable age and metallicity estimates as test particles to evaluate the performance of four widely used simple stellar population models in the optical/near-infrared (near-IR) colour–colour space. All models reproduce the reddening-corrected colours of the old ( $\geq 10$  Gyr) globular clusters quite well, but model performance varies at younger ages. In order to account for the effects of stochastic fluctuations in individual clusters, we provide composite  $B - V$ ,  $B - J$ ,  $V - J$ ,  $V - K_S$  and  $J - K_S$  colours for Magellanic Cloud clusters in several different age intervals. The accumulated masses for most composite clusters are higher than that needed to keep luminosity variations due to stochastic fluctuations below the 10 per cent level. The colours of the composite clusters are clearly distinct in optical–near-IR colour–colour space for the following intervals of age:  $> 10$  Gyr, 2–9 Gyr, 1–2 Gyr, and 200 Myr–1 Gyr. This suggests that a combination of optical plus near-IR colours can be used to differentiate clusters of different age and metallicity.

**Key words:** techniques: photometric – Magellanic Clouds – galaxies: star clusters – infrared: general.

## 1 INTRODUCTION

The most-efficient method to determine the age and metallicity for unresolved stellar systems (especially at high redshift) is by comparing their observed colours with the predictions of evolution synthesis models (e.g. Bruzual & Charlot 1993, 2003; Worthey 1994; Maraston 1998; Vazdekis 1999; Anders & Fritze-v. Alvensleben 2003; Maraston 2005). Thus, it is important to test the integrated colours predicted by recent models, based on objects which have accurate ages and metallicities determined independently. In this paper, we focus our attention on the combination of visual and near-infrared (near-IR) photometry, which has proven to be important for breaking the age–metallicity degeneracy, particularly in stellar populations older than approximately a few times 100 Myr (e.g. Goudfrooij et al. 2001; Puzia et al. 2002; Hempel & Kissler-Patig 2004).

With the advent of the *Spitzer Space Telescope* (*Spitzer*) and mid-IR instrumentation for some large ground-based telescopes, the near-IR spectral region is now accessible at intermediate to high redshifts. In a recent paper based on *Spitzer* Infrared Array Camera (IRAC) imaging, van der Wel et al. (2006) reported significant discrepancies between some model predictions and the observed rest-frame  $K$ -band properties of early-type galaxies at  $z \approx 1$ . Their results show that the interpretation of near-IR photometry is hampered by model uncertainties. As a consequence, the determination of masses of distant stellar systems based on such data can have uncertainties up to a factor of 2.5 (see Bruzual 2007).

Unfortunately, providing accurate model predictions in the near-IR is challenging, since there are limitations imposed by the present lack of understanding of certain stages of stellar evolution [e.g. thermally pulsing asymptotic giant branch (AGB) stars]. These objects significantly affect the spectral energy distribution (SED) in the near-IR and mid-IR for stellar populations with ages between  $\approx 200$  Myr to 3 Gyr. Another possible complication is that the stellar libraries used by population synthesis models contain mostly stars from the solar neighbourhood. These stars have a star formation

★E-mail: pessev@stsci.edu (PMP); goudfroo@stsci.edu (PG); puziat@nrc.ca (THP); rupali.chandar@utoledo.edu (RC)

**Table 1.** Extended MC cluster sample.

ID (1)	$\alpha_{2000}$ (2)	$\delta_{2000}$ (3)	Age, errors and reference (4) (5) (6) (7)				[Fe/H], error and reference (8) (9) (10)			$A_V$ (11)	$\Delta A_V$ (12)
NGC 265	00:47:12	−73:28:38	8.5	+0.3	−0.3	2	−0.62	$^{+0.23}_{-0.61}$	2	0.34	0.02
NGC 1644	04:37:39	−66:12:00	9.53	+0.05	−0.05	1	−1.4	$\pm 0.2$	1	0.39	0.02
NGC 1928	05:20:58	−69:28:40	10.11	+0.06	−0.08	5	−1.27	$\pm 0.14$	5	0.34	0.06
NGC 1994	05:28:22	−69:08:30	7.06			4				0.41	0.02
NGC 2058	05:36:55	−70:09:44	7.85	+0.10	−0.15	4				0.39	0.02
NGC 2107	05:43:13	−70:38:23	8.55	+0.25	−0.24	3				0.36	0.04
NGC 2108	05:43:56	−69:10:48	8.90	+0.26	−0.26	3				0.50	0.05
NGC 2134	05:51:56	−71:05:54	8.27			7	−0.4		7	0.62	0.03
NGC 2154	05:57:38	−67:15:42	9.16	+0.28	−0.28	3	−0.56	$\pm 0.2$	6	0.39	0.03

*Notes.* Column (1): object ID. Columns (2) and (3): cluster coordinates – right ascension (given as hh:mm:ss.s) and declination (given as dd:mm:ss.s) in J2000 retrieved from Simbad Astronomical Data base. Column (4): age of the object given as log (age) with corresponding errors in columns (5) and (6) and literature references (see below) in column (7). Column (8): metallicity values retrieved from the literature with their errors in column (9) and references in column (10). Column (11): V-band reddening values for the objects with corresponding errors in column (12) retrieved from the MCPS reddening estimation tool.

*References.* (1) Bica et al. (1986); (2) Chiosi & Vallenari (2007); (3) Elson & Fall (1985); (4) Elson & Fall (1988); (5) Mackey & Gilmore (2004); (6) Olszewski et al. (1991); (7) Vallenari et al. (1994).

history which is not necessarily typical for extragalactic populations (e.g. relatively little variation of  $[\alpha/\text{Fe}]$  ratios), and there are only a very limited number of AGB spectra available.

The Large and Small Magellanic Clouds (LMC and SMC, respectively) provide a unique opportunity to test the accuracy of present simple stellar population (SSP) models, since they contain a significant population of intermediate-age massive star clusters which are not easily accessible in our Galaxy. The ages and metallicities of these star clusters can be determined from deep colour–magnitude diagrams (CMDs) reaching below the main-sequence turn-off (MSTO).<sup>1</sup> Medium- and high-resolution spectroscopy of individual giants in these clusters also provides independent metallicity estimates. Therefore, their integrated-light properties (easily observed with small- and moderate-aperture telescopes) can be combined with the accurate age/metallicity measurements and used to test (and calibrate) the SSP models.

In Pessev et al. (2006) (hereafter Paper I), we used the Two-Micron All-Sky Survey (2MASS; Skrutskie et al. (2006)) to derive near-IR ( $JHK_S$ ) integrated-light magnitudes and colours for a large sample of MC star clusters, based on a homogeneous, accurately calibrated data set. In this study, we use the sample from Paper I and new photometry for nine additional objects (forming the largest data set of integrated near-IR magnitudes and colours of LMC/SMC star clusters to date) to test the performance of several SSP models. We combine the 2MASS data with optical photometry originating from the work of Bica et al. (1996) and the compilation of van den Bergh (1981). The technique adopted in Paper I – measuring  $JHK_S$  curves of growth to large radii allows us to utilize rather heterogeneous data bases of optical photometry, usually performed with a set of fixed apertures. We use 54 clusters from our sample as ‘test particles’. These clusters were chosen to have reli-

able age and metallicity measurements, covering a wide parameter space.

This paper is organized as follows. In Section 2, we define our extended sample and present the new photometry along with the compilation of visual magnitudes and colours. Four sets of SSP models are tested in Section 3, followed by concluding remarks in Section 4. Information about the properties of the cluster sample is presented in Appendices A and B. Transformations between the model grids in the Bessell & Brett (1988) system and the photometric system of 2MASS are provided in Appendix C.

## 2 PHOTOMETRY OF MAGELLANIC CLOUD CLUSTERS

### 2.1 Extending the sample – new near-IR integrated photometry of MC clusters

We selected nine objects (see Table 1 for details) to add to our original sample which was presented in Paper I. The total sample now includes all of the old clusters in the MCs (with the exception of the Reticulum cluster, which is excluded due to insufficient depth of the available 2MASS images) and all of the ‘near-IR-enhanced’ clusters from Persson et al. (1983). Some objects were included in this extended sample because they have new integrated-light optical magnitudes and colours available. Overall the sample provides optimal coverage of the age–metallicity parameter space of MC star clusters. We intend to add 2MASS  $JHK_S$  integrated photometry for additional clusters as new information based on deep CMDs becomes available in the future.

The 2MASS (Skrutskie et al. 2006) atlas images were recovered through the interactive image service available on the survey web page<sup>2</sup> (see Table 2 for information about the utilized images). We analysed these data following the reduction scheme presented in Paper I. Extinction corrections were derived using the online tools provided by the Magellanic Clouds Photometric Survey (MCPS, Zaritsky, Harris & Thompson 1997); details about extinction

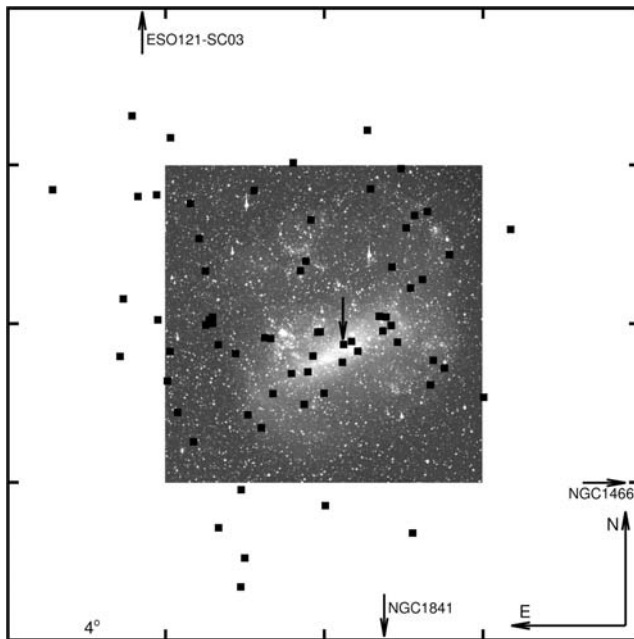
<sup>1</sup> Obtaining photometry with sufficient quality to secure reliable age and metallicity estimates for clusters in galaxies beyond the MCs requires a significant investment of observing time. To date only one such cluster, SKHB 312 in M31, has a CMD deep enough to probe the MSTO region (Brown et al. 2004). The photometry for this object was obtained as a result of a programme utilizing 126 *Hubble Space Telescope* (HST) orbits.

<sup>2</sup> <http://irsa.ipac.caltech.edu/applications/2MASS/IM/interactive.html>

**Table 2.** 2MASS atlas images of the clusters in the extended sample.

ID (1)	<i>N</i> (2)	<i>J</i> (3)	<i>H</i> (4)	<i>K<sub>S</sub></i> (5)
NGC 265	1	aJ_asky_980809s0810198.fits	aH_asky_980809s0810198.fits	aK_asky_980809s0810198.fits
NGC 1644	1	aJ_asky_991026s1140257.fits	aH_asky_991026s1140257.fits	aK_asky_991026s1140257.fits
NGC 1928	1	aJ_asky_981220s0850162.fits	aH_asky_981220s0850162.fits	aK_asky_981220s0850162.fits
NGC 1994	1	aJ_asky_000212s0190150.fits	aH_asky_000212s0190150.fits	aK_asky_000212s0190150.fits
NGC 2058	1	aJ_asky_000206s0240186.fits	aH_asky_000206s0240186.fits	aK_asky_000206s0240186.fits
NGC 2107	1	aJ_asky_980321s0080209.fits	aH_asky_980321s0080209.fits	aK_asky_980321s0080209.fits
NGC 2108	1	aJ_asky_980321s0080150.fits	aH_asky_980321s0080150.fits	aK_asky_980321s0080150.fits
NGC 2134	1	aJ_asky_981025s1000044.fits	aH_asky_981025s1000044.fits	aK_asky_981025s1000044.fits
NGC 2154	1	aJ_asky_981025s1110068.fits	aH_asky_981025s1110068.fits	aK_asky_981025s1110068.fits

*Notes.* Column (1): object ID. Column (2): number of image sets retrieved. Columns (3), (4) and (5): designations of the individual *J*, *H* and *K<sub>S</sub>* frames, respectively.

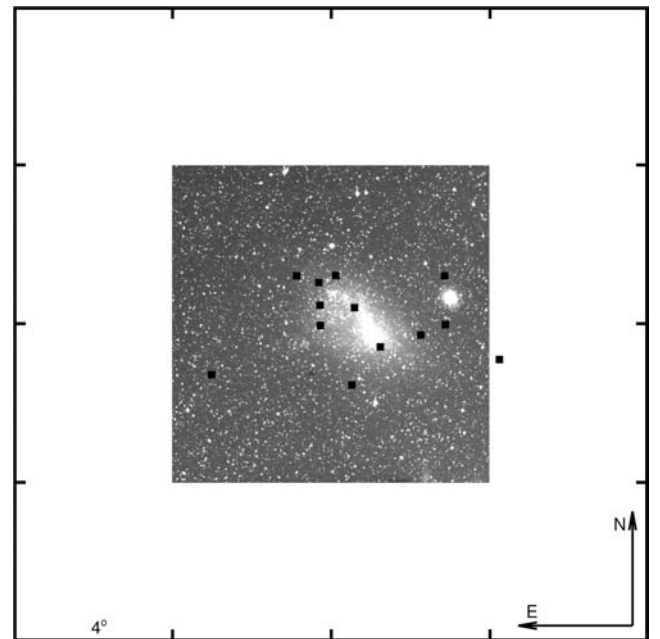


**Figure 1.** A finding chart of the LMC showing the clusters in our sample. The *R*-band image is centred on  $\alpha_{2000} = 05^{\text{h}}26^{\text{m}}37.7$  and  $\delta_{2000} = -68^{\circ}56'57.5$ . The arrow near the centre outlines the position of NGC 1928 ( $\alpha_{2000} = 05^{\text{h}}20^{\text{m}}57.7$  and  $\delta_{2000} = -69^{\circ}28'40.2$ ). This cluster is located close to the geometrical centre of the LMC bar, and was adopted by Bica, Dottori & Pastoriza (1986) as a reference point for the relative coordinates of the LMC cluster system. The labelled arrows show the direction towards the clusters lying outside the boundaries of this chart. The *R*-band image (G. Bothun 1997, private communication) covers  $8^{\circ} \times 8^{\circ}$ , while the dimensions of the chart are  $16^{\circ} \times 16^{\circ}$ .

estimates for the SMC and LMC are provided in Zaritsky et al. (2002) and Zaritsky et al. (2004), respectively. ( $A_V$  values and their uncertainties are listed in the last two columns of Table 1.)

All of the MC clusters with *JHK<sub>S</sub>* near-IR 2MASS photometry from Paper I and this work are shown in the finder charts (see Figs 1 and 2 for the LMC and SMC, respectively). The cluster positions are marked by the centres of our aperture sets, derived as described in Paper I. Table 3 contains *JHK<sub>S</sub>* photometry for the 9 new clusters.<sup>3</sup>

<sup>3</sup> The listed magnitudes are not corrected for reddening.



**Figure 2.** A finding chart of the SMC showing the clusters in our sample. The *R*-band image (G. Bothun 1997, private communication) is centred on  $\alpha_{2000} = 01^{\text{h}}04^{\text{m}}42.8$  and  $\delta_{2000} = -72^{\circ}52'32.4$ . SMC clusters cover a smaller area than LMC objects. There is only one cluster outside the *R* frame, but for illustration purposes the dimensions of this finder chart are identical to those of the LMC chart in Fig. 1.

*Notes on individual objects.* All the objects that required special attention during the reduction process are commented on below.

(i) *NGC 265.* This object is situated in a rich SMC star field and the depth of the images decreases from *J* to *K<sub>S</sub>*. An analysis of the curves of growth shows that for aperture diameters larger than 140 arcsec this trend causes some variation in the measured cluster colours. The photometry is carried out with the full set of apertures, but results for sizes exceeding 140 arcsec should be treated with caution.

(ii) *NGC 1644.* This faint compact cluster is situated close to the edge of the atlas image. The photometry is carried out up to 90 arcsec aperture diameter. The curve of growth in *K<sub>S</sub>* shows evidence for variations in the background level. Results for aperture sizes larger than 60 arcsec could be affected by these variations. Due to the proximity of the image edge, our automated procedure for deriving

**Table 3.** New near-IR photometry of MC clusters.

ID (1)	$\alpha_{2000}$ (2)	$\delta_{2000}$ (3)	$d$ (4)	Flag (5)	$D$ (6)	$J$ (7)	$J_{\text{err}}$ (8)	$H$ (9)	$H_{\text{err}}$ (10)	$K_{\text{S}}$ (11)	$K_{\text{S err}}$ (12)	
NGC 265	00:47:09.9	−73:28:39.3	7.5	AAB	20	13.00	0.03	12.43	0.03	12.53	0.05	
					40	11.80	0.03	10.48	0.02	10.41	0.02	
					60	11.54	0.06	10.31	0.03	10.27	0.05	
					80	11.35	0.08	10.15	0.05	10.04	0.06	
					100	11.16	0.11	10.05	0.07	9.92	0.09	
					120	10.96	0.13	9.90	0.09	9.79	0.12	
					140	10.78	0.15	9.84	0.12	9.71	0.15	
					160	:	10.42	0.14	9.61	0.12	9.64	0.18
					180	:	10.32	0.17	9.52	0.15	9.50	0.21
					200	:	10.18	0.19	9.44	0.17	9.42	0.24
NGC 1644	04:37:39.8	−66:11:55.5	6.5	BBB	20	12.08	0.03	11.62	0.02	11.43	0.02	
					40	11.51	0.06	11.05	0.05	10.84	0.05	
					60	11.31	0.11	10.88	0.10	10.76	0.10	
					80	:	11.12	0.17	10.74	0.16	10.61	0.16
					90	:	11.05	0.20	10.66	0.18	10.51	0.18
NGC 1928	05:20:57.8	−69:28:41.2	1	AAB	20	11.65	0.03	11.05	0.03	11.24	0.04	
					40	11.04	0.05	10.51	0.06	10.56	0.09	
					60	10.73	0.08	10.28	0.11	10.25	0.15	
					80	10.54	0.12	10.10	0.17	9.34	0.11	
					100	10.40	0.17	9.98	0.24	9.24	0.16	
					120	10.17	0.20	9.73	0.28	9.06	0.20	
					140	10.05	0.25	9.60	0.35	8.75	0.21	
					160	9.73	0.24	9.16	0.30	8.69	0.26	
					180	9.49	0.25	8.78	0.27	8.54	0.29	
					200	9.35	0.28	8.70	0.32	8.47	0.34	
NGC 1994	05:28:22.4	−69:08:31.3	2	BBA	20	8.33	0.01	7.63	0.01	7.45	0.01	
					40	8.28	0.01	7.59	0.01	7.40	0.01	
					60	8.25	0.01	7.57	0.01	7.38	0.01	
					80	8.22	0.02	7.55	0.01	7.36	0.01	
					100	8.14	0.02	7.47	0.01	7.35	0.02	
					120	7.95	0.03	7.26	0.02	7.14	0.02	
					140	7.80	0.03	7.10	0.02	6.95	0.03	
					160	7.78	0.04	7.09	0.02	6.93	0.04	
					180	7.76	0.05	7.07	0.03	6.92	0.04	
					200	7.74	0.05	7.06	0.04	6.91	0.05	
NGC 2058	05:36:54.0	−70:09:42.0	10	BBB	20	10.72	0.02	10.15	0.01	10.08	0.02	
					40	9.82	0.03	9.22	0.02	9.17	0.03	
					60	9.57	0.04	9.03	0.04	8.95	0.05	
					80	9.26	0.06	8.76	0.06	8.60	0.07	
NGC 2107	05:43:13.3	−70:38:29.8	2.5	BBB	20	10.81	0.03	9.98	0.02	9.70	0.02	
					40	10.21	0.07	9.54	0.04	9.31	0.05	
					60	10.05	0.13	9.43	0.08	9.20	0.11	
					80	9.90	0.20	9.35	0.14	9.12	0.18	
					100	9.70	0.26	9.14	0.18	8.92	0.24	
					120	9.47	0.31	8.87	0.20	8.63	0.27	
					140	9.34	0.39	8.72	0.24	8.32	0.27	
NGC 2108	05:43:56.7	−69:10:49.9	4	BBB	20	12.31	0.02	11.23	0.01	10.97	0.01	
					40	10.78	0.01	9.88	0.01	9.36	0.01	
					60	10.48	0.02	9.71	0.02	9.25	0.01	
					80	10.35	0.03	9.63	0.03	9.20	0.02	
					100	10.26	0.03	9.56	0.04	9.15	0.03	
					120	10.17	0.04	9.47	0.05	9.10	0.05	
					140	10.00	0.05	9.31	0.06	9.00	0.06	
					160	9.55	0.05	8.83	0.05	8.45	0.04	
					180	9.50	0.05	8.81	0.06	8.41	0.06	
					200	9.45	0.06	8.77	0.08	8.39	0.07	

Table 3 – continued

ID (1)	$\alpha_{2000}$ (2)	$\delta_{2000}$ (3)	$d$ (4)	Flag (5)	$D$ (6)	$J$ (7)	$J_{\text{err}}$ (8)	$H$ (9)	$H_{\text{err}}$ (10)	$K_S$ (11)	$K_{S \text{ err}}$ (12)
NGC 2134	05:51:56.5	−71:05:50.4	4.5	BBB	20	10.80	0.01	10.16	0.01	10.10	0.01
					40	10.18	0.02	9.68	0.01	9.65	0.01
					60	9.94	0.03	9.50	0.02	9.43	0.02
					80	9.78	0.04	9.39	0.03	9.25	0.03
					100	9.46	0.04	8.96	0.03	8.77	0.03
					120	9.42	0.06	8.93	0.05	8.74	0.05
					140	8.95	0.05	8.31	0.04	8.01	0.03
					160	8.86	0.06	8.22	0.04	7.89	0.04
					180	8.82	0.08	8.16	0.05	7.85	0.05
					200	8.82	0.10	8.18	0.07	7.86	0.06
NGC 2154	05:57:37.9	−67:15:43.7	2.0	BAB	20	11.24	0.01	10.38	0.01	9.86	0.01
					40	10.44	0.01	9.64	0.01	9.18	0.01
					60	10.16	0.02	9.38	0.01	8.92	0.01
					80	9.94	0.02	9.22	0.02	8.79	0.01
					100	9.80	0.03	9.11	0.02	8.68	0.02
					110	9.78	0.04	9.11	0.03	8.68	0.02

Notes. Column (1): the cluster designation. Columns (2) and (3): the right ascension and declination of the position used to centre the apertures for the integral photometry [(hh:mm:ss.s) and (dd:mm:ss.s), respectively]. Column (4): the offset (in arcseconds) measured on 2MASS images between that position and the cluster coordinates retrieved from SIMBAD. Column (5): a flag, providing information about the age (first letter), metallicity estimates (second letter) and the photometry (third letter) for each cluster. A corresponds to a reliable age, metallicity and photometry, B denotes the cases when the age and metallicity values are uncertain and when used in the third position B stands for the cases described in Section 2.1 and/or the photometry was provided in aperture sizes smaller than 200 arcsec. The aperture diameters (arcseconds) used for each measurement are listed in column (6), they are denoted with colon in case complications with photometry were suspected. The photometry information (uncorrected for reddening) is given in columns (7)–(12), in the order:  $J$  magnitude, photometric uncertainty in  $J$ , and the same information for the other two survey bands  $H$  and  $K_S$ . The photometric uncertainty in each band is calculated as the quadrature sum of the zero-point uncertainty, internal uncertainty of the photometry, and the uncertainty due to stochastic fluctuations of the background stellar population.

the aperture centres does not provide reliable results. Therefore, the cluster centre was chosen ‘by eye’, but we consider this position to be reliable due to the compactness of the object and lack of stellar contamination in the surrounding field.

(iii) *NGC 1928*. This is an old globular cluster (GC) (see Mackey & Gilmore 2004). Situated in the LMC bar region, this object suffers from strong background/foreground contamination. Combined with the limited depth of the cluster’s image on the 2MASS atlas frames, this makes the integrated photometry challenging. Due to the presence of several relatively bright stars in the vicinity of the cluster, we decided to use only the results based on the unresolved light from the object to derive the aperture centres. Several bright stars in the aperture set were subtracted after an analysis of their properties based on the IR colours explained in detail in Paper I. The resulting integrated-photometry curves of growth show residual effects of the background removal and the near-IR photometry should be treated with caution in this case.

(iv) *NGC 2058*. This cluster is located close to the edge of the atlas image. Photometry is carried out with a set of apertures up to  $D = 80$  arcsec.

(v) *NGC 2107*. The cluster lies close to the edge of the atlas image. In this case, photometry was carried out with a set of aperture sizes up to 140 arcsec. The curves of growth indicate that we obtain good sampling of the flux from the object.

(vi) *NGC 2108*. There are three luminous stars in the cluster. Their colours are consistent with those expected for carbon stars. It is worth while to mention that Ferraro et al. (2004) found the same number of AGB stars in their near-IR photometric study of this object. The age estimates of the cluster are also consistent with the presence of carbon stars, so they are included in the final photometry.

(vii) *NGC 2134*. Several luminous stars are present within the cluster area. They affect the centring, so we use the results from the unresolved component. The colours of these stars are consistent

with those expected for carbon stars, and they are included in the final integrated photometry measurements.

(viii) *NGC 2154*. Due to the proximity of the object to the edge of the atlas image, the photometry is carried out with a set of apertures up to 110 arcsec in diameter.

## 2.2 Compiling a catalogue of optical cluster photometry

We conducted an extensive literature search for appropriate integrated optical cluster colours to combine with our near-IR measurements. Our compilation from the literature is presented in Table 4. It is based on integrated-light photoelectric observations and lists the  $V$  magnitudes,  $(B - V)$  and  $(U - B)$  colours plus their uncertainties; reddening values towards the objects with their corresponding uncertainties are also included. The photometry comes from different observers, so special care was taken to ensure that the individual results are consistent. Recent independent CCD data sets from Goudfrooij et al. (2006) and Hunter et al. (2003) were also used in the consistency checks. The cases where discrepancies cannot be readily explained are listed as notes in the last column of Table 4. As a rule, we provide information about the largest aperture size available. This reduces the effects of both the aperture centring (which could differ for the optical and near-IR data), the stochastic fluctuations of the background stellar population and of the stars in the clusters themselves. The photometry of all SMC clusters is taken from the homogeneous data set of Alcaïno (1978), and is also listed in Table 4. Reddening information is compiled from a number of sources (indicated in the table) and preference is given to values based on deep CMDs.

## 3 TESTING THE MODELS

In recent years, significant improvements in modelling the properties of SSPs have been achieved, and several independent sets of SSP

**Table 4.** Compilation of optical photometry.

ID (1)	Galaxy (2)	<i>D</i> (3)	<i>V</i> (4)	( <i>B</i> − <i>V</i> ) (5)	( <i>U</i> − <i>B</i> ) (6)	Reference (7)	<i>A<sub>V</sub></i> (8)	Reference (9)	SWB (10)	Note (11)
NGC 121	SMC	62	11.24 ± 0.01	0.76 ± 0.00	0.10 ± 0.01	1	0.16 ± 0.09	11	VII	
NGC 152	SMC	62	12.94 ± 0.04	0.70 ± 0.02	0.18 ± 0.02	1	0.16 ± 0.03	7	V	
NGC 265	SMC	62	12.13 ± 0.03	0.30 ± 0.01	−0.11 ± 0.05	1	0.19 <sup>+0.15</sup> <sub>−0.13</sub>	6	III	
NGC 330	SMC	62	9.60 ± 0.01	0.15 ± 0.01	−0.46 ± 0.00	1	0.37 ± 0.02	—	I	
NGC 339	SMC	62	12.84 ± 0.04	0.73 ± 0.01	0.03 ± 0.00	1	0.09 ± 0.12	11	VII	
NGC 361	SMC	62	12.24 ± 0.01	0.78 ± 0.00	0.14 ± 0.02	1	0.22 ± 0.09	11	VII	
NGC 411	SMC	62	12.21 ± 0.04	0.62 ± 0.01	0.24 ± 0.02	1	0.37 ± 0.03	7	V	
NGC 416	SMC	62	11.42 ± 0.00	0.73 ± 0.00	0.12 ± 0.00	1	0.25 ± 0.09	10	VII	
NGC 419	SMC	62	10.61 ± 0.01	0.65 ± 0.01	0.24 ± 0.01	1	0.20 ± 0.02	—	V	
NGC 458	SMC	62	11.73 ± 0.03	0.16 ± 0.00	−0.17 ± 0.01	1	0.32 ± 0.02	—	V	
NGC 1466	LMC	60	11.59 ± 0.03	0.68 ± 0.02	0.13 ± 0.03	15	0.28 ± 0.06	16	VII	
NGC 1644	LMC	60	12.89 ± 0.02	0.60 ± 0.03	0.19 ± 0.02	15	0.39 ± 0.02	—	V	
NGC 1651	LMC	100	12.28 ± 0.04	0.71 ± 0.04	0.28 ± 0.04	4	0.34 ± 0.03	8	V	
NGC 1711 <sub>(B)</sub>	LMC	50	12.50 ± 0.04	0.27 ± 0.04	−0.04 ± 0.04	4	0.56 ± 0.01	—	III	1
NGC 1711 <sub>(v)</sub>	LMC	60	10.11 ± 0.03	0.12 ± 0.01	−0.37 ± 0.02	15			III	1
NGC 1718	LMC	62	12.25 ± 0.01	0.76 ± 0.01	0.26 ± 0.02	2	0.31 ± 0.09	8	VI	
NGC 1751	LMC	100	11.73 ± 0.04	0.79 ± 0.04	0.27 ± 0.04	4	0.65 ± 0.06	—	VI	
NGC 1754	LMC	100	11.57 ± 0.04	0.75 ± 0.04	0.15 ± 0.04	4	0.28 ± 0.06	12	VII	
NGC 1777	LMC	38	12.80 ± 0.02	0.60 ± 0.03	0.17 ± 0.03	4	0.31 ± 0.09	8	IVB	
NGC 1783	LMC	60	10.97 ± 0.02	0.63 ± 0.02	0.20 ± 0.03	15	0.30 ± 0.03	—	V	
NGC 1786 <sub>(u)</sub>	LMC	60	10.16 ± 0.04	0.67 ± 0.00	0.06 ± 0.02	15	0.28 ± 0.16	5	VII	2
NGC 1786 <sub>(c)</sub>	LMC	60	10.88 ± 0.04	0.74 ± 0.00	0.10 ± 0.02	15			VII	2
NGC 1805	LMC	60	10.63 ± 0.03	0.11 ± 0.02	−0.55 ± 0.01	15	0.32 ± 0.02	—	I	
NGC 1806	LMC	60	11.27 ± 0.04	0.26 ± 0.02	0.73 ± 0.02	15	0.25 ± 0.04	—	V	
NGC 1818	LMC	60	9.85 ± 0.02	0.18 ± 0.02	−0.46 ± 0.00	15	0.39 ± 0.02	—	I	
NGC 1831	LMC	60	11.18 ± 0.02	0.34 ± 0.02	0.13 ± 0.02	15	0.34 ± 0.03	8	IVA	
NGC 1835	LMC	60	10.16 ± 0.05	0.74 ± 0.04	0.11 ± 0.03	15	0.25 ± 0.06	12	VII	
NGC 1841	LMC	25	14.08	0.90	0.50	14	0.62 ± 0.09	5	VII	
NGC 1846	LMC	60	11.40 ± 0.02	0.31 ± 0.05	0.74 ± 0.03	15	0.41 ± 0.04	—	VI	
NGC 1847	LMC	72	11.06 ± 0.02	0.20 ± 0.02	−0.33 ± 0.03	3	0.49 ± 0.02	—	I	
NGC 1850	LMC	60	9.36 ± 0.06	0.11 ± 0.03	−0.34 ± 0.07	15	0.33 ± 0.01	—	II	
NGC 1856	LMC	60	10.07 ± 0.02	0.34 ± 0.01	0.06 ± 0.01	15	0.65 ± 0.06	8	IVA	
NGC 1860	LMC	72	11.04 ± 0.02	0.14 ± 0.02	−0.39 ± 0.03	3	0.22 ± 0.03	—	I	
NGC 1866	LMC	60	9.89 ± 0.01	0.26 ± 0.02	−0.06 ± 0.01	15	0.28 ± 0.06	—	III	
NGC 1868	LMC	62	11.57 ± 0.02	0.45 ± 0.02	0.15 ± 0.03	3	0.12 ± 0.03	8	IVA	
NGC 1898	LMC	60	11.52 ± 0.06	0.75 ± 0.02	−0.03 ± 0.03	15	0.22 ± 0.06	12	VII	
NGC 1916	LMC	44	10.38 ± 0.02	0.78 ± 0.02	0.18 ± 0.03	3	0.42 ± 0.05	—	VII	
NGC 1928	LMC	62	11.88 ± 0.02	0.22 ± 0.02	−0.31 ± 0.03	3	0.20 ± 0.05	9	VII	
NGC 1939	LMC	38	11.78 ± 0.05	0.69 ± 0.05	0.09 ± 0.05	4	0.40 ± 0.08	9	VII	
NGC 1978	LMC	60	10.74 ± 0.04	0.78 ± 0.04	0.23 ± 0.07	15	0.76 ± 0.05	—	VI	
NGC 1984	LMC	50	9.99 ± 0.04	0.01 ± 0.04	−0.82 ± 0.04	4	0.36 ± 0.02	—	0	
NGC 1987	LMC	60	12.18 ± 0.01	0.51 ± 0.01	0.18 ± 0.02	15	0.28 ± 0.03	—	IVB	
NGC 1994	LMC	50	9.78 ± 0.04	0.09 ± 0.04	−0.69 ± 0.04	4	0.41 ± 0.02	—	I	
NGC 2004	LMC	72	9.60 ± 0.02	0.13 ± 0.02	−0.71 ± 0.03	3	0.33 ± 0.02	—	I	
NGC 2005	LMC	25	11.57 ± 0.00	0.73 ± 0.00	0.20 ± 0.00	14	0.37 ± 0.06	12	VII	
NGC 2011	LMC	45	10.58 ± 0.02	0.00 ± 0.02	−0.72 ± 0.03	3	0.47 ± 0.02	—	I	
NGC 2019	LMC	60	10.95 ± 0.01	0.77 ± 0.01	0.16 ± 0.02	15	0.37 ± 0.06	12	VII	
NGC 2031	LMC	72	10.83 ± 0.02	0.26 ± 0.02	−0.07 ± 0.03	3	0.40 ± 0.03	—	III	
NGC 2058 <sub>(v)</sub>	LMC	60	11.85 ± 0.04	0.24 ± 0.01	−0.12 ± 0.01	15	0.39 ± 0.02	—	III	3
NGC 2058 <sub>(G)</sub>	LMC	60	10.73 ± 0.03						III	3
NGC 2100	LMC	60	9.60 ± 0.04	0.16 ± 0.02	−0.56 ± 0.02	15	0.80 ± 0.02	—	I	
NGC 2107	LMC	60	11.51 ± 0.02	0.38 ± 0.03	0.13 ± 0.03	15	0.36 ± 0.04	—	IVA	
NGC 2108	LMC	62	12.32 ± 0.01	0.58 ± 0.01	0.22 ± 0.02	2	0.50 ± 0.05	—	IVB	
NGC 2121	LMC	62	12.37 ± 0.01	0.84 ± 0.01	0.25 ± 0.02	2	0.22 ± 0.06	8	VI	
NGC 2134	LMC	60	11.05 ± 0.04	0.26 ± 0.02	−0.02 ± 0.03	15	0.62 ± 0.03	—	III	
NGC 2136	LMC	60	10.54 ± 0.02	0.28 ± 0.02	−0.13 ± 0.02	15	0.58 ± 0.02	—	III	
NGC 2153	LMC	100	13.05 ± 0.04	0.69 ± 0.04	0.03 ± 0.04	4	0.27 ± 0.05	—	VII	
NGC 2154	LMC	62	12.32 ± 0.01	0.68 ± 0.01	0.24 ± 0.02	2	0.39 ± 0.03	—	V	
NGC 2155	LMC	62	12.60 ± 0.01	0.81 ± 0.01	0.23 ± 0.02	2	0.06 ± 0.03	8	VI	
NGC 2156	LMC	72	11.38 ± 0.02	0.12 ± 0.02	−0.07 ± 0.03	3	0.20 ± 0.02	—	III	
NGC 2157	LMC	60	10.16 ± 0.02	0.19 ± 0.02	−0.16 ± 0.01	15	0.42 ± 0.02	—	III	

Table 4 – continued

ID (1)	Galaxy (2)	$D$ (3)	$V$ (4)	$(B - V)$ (5)	$(U - B)$ (6)	Reference (7)	$A_V$ (8)	Reference (9)	SWB (10)	Note (11)
NGC 2159	LMC	72	$11.38 \pm 0.02$	$0.28 \pm 0.02$	$-0.14 \pm 0.03$	3	$0.29 \pm 0.03$	–	III	
NGC 2162	LMC	62	$12.70 \pm 0.01$	$0.68 \pm 0.01$	$0.31 \pm 0.02$	2	$0.09 \pm 0.06$	8	V	
NGC 2164	LMC	60	$10.34 \pm 0.01$	$0.10 \pm 0.01$	$-0.24 \pm 0.01$	6	$0.33 \pm 0.02$	–	II	
NGC 2172	LMC	72	$11.75 \pm 0.02$	$0.18 \pm 0.02$	$-0.16 \pm 0.03$	3	$0.26 \pm 0.03$	–	III	
NGC 2173	LMC	150	$11.88 \pm 0.05$	$0.82 \pm 0.05$	$0.28 \pm 0.05$	4	$0.22 \pm 0.06$	8	VI	
NGC 2190	LMC	61	$12.94 \pm 0.02$	$0.63 \pm 0.03$	$0.29 \pm 0.03$	4	$0.39 \pm 0.02$	–	V	
NGC 2193	LMC	38	$13.42 \pm 0.02$	$0.71 \pm 0.03$	$0.20 \pm 0.03$	4	$0.39 \pm 0.02$	–	V	
NGC 2203	LMC	150	$11.29 \pm 0.04$	$0.77 \pm 0.04$	$0.26 \pm 0.04$	4	$0.39 \pm 0.02$	–	VI	
NGC 2209	LMC	62	$13.15 \pm 0.01$	$0.52 \pm 0.01$	$0.36 \pm 0.02$	2	$0.47 \pm 0.09$	8	IVB	
NGC 2210	LMC	60	$10.94 \pm 0.03$	$0.71 \pm 0.03$	$0.11 \pm 0.01$	6	$0.28 \pm 0.09$	5	VII	
NGC 2213	LMC	62	$12.38 \pm 0.01$	$0.71 \pm 0.01$	$0.28 \pm 0.02$	2	$0.19 \pm 0.09$	8	V	
NGC 2214	LMC	60	$10.93 \pm 0.01$	$0.11 \pm 0.02$	$-0.27 \pm 0.01$	6	$0.39 \pm 0.02$	–	II	
NGC 2231	LMC	44	$13.20 \pm 0.01$	$0.67 \pm 0.01$	$0.24 \pm 0.02$	2	$0.39 \pm 0.02$	–	V	
NGC 2249	LMC	72	$12.23 \pm 0.02$	$0.43 \pm 0.02$	$0.20 \pm 0.03$	3	$0.03 \pm 0.06$	8	IVB	
NGC 2257	LMC	61	$12.62 \pm 0.02$	$0.62 \pm 0.03$	$0.01 \pm 0.03$	4	$0.00 \pm 0.00$	13	VII	
ESO121–003	LMC	61	$14.04 \pm 0.02$	$0.87 \pm 0.03$	$0.17 \pm 0.05$	4	$0.10 \pm 0.05$	9	VII	
Hodge4	LMC	38	$13.33 \pm 0.02$	$0.66 \pm 0.03$	$0.16 \pm 0.05$	4	$0.39 \pm 0.02$	–	V	
Hodge11	LMC	62	$11.98 \pm 0.01$	$0.63 \pm 0.01$	$0.00 \pm 0.02$	2	$0.23 \pm 0.02$	10	VII	
Hodge14	LMC	62	$13.42 \pm 0.01$	$0.72 \pm 0.01$	$0.21 \pm 0.02$	2	$0.25 \pm 0.06$	8	V	
Kron3	SMC	62	$12.05 \pm 0.02$	$0.69 \pm 0.01$	$0.05 \pm 0.02$	1	$0.00 \pm 0.06$	11	VII	
Lindsay1	SMC	62	$13.32 \pm 0.05$	$0.75 \pm 0.00$	$0.17 \pm 0.05$	1	$0.19 \pm 0.06$	11	VII	
Lindsay113	SMC	62	$13.61 \pm 0.04$	$0.73 \pm 0.02$	$0.05 \pm 0.09$	1	$0.00 \pm 0.06$	11	VII	
LW431	LMC	38	$13.67 \pm 0.02$	$0.74 \pm 0.03$	$0.13 \pm 0.05$	4	$0.39 \pm 0.02$	–	VII	
SL842	LMC	38	$14.15 \pm 0.02$	$0.79 \pm 0.03$	$0.11 \pm 0.05$	4	$0.39 \pm 0.02$	–	VII	

*Notes.* Column (1): the cluster designation. Column (2): the galaxy in which the object resides. The diameter of the aperture used for the integral visual magnitude and colour measurements is given in column (3). Column (4) gives the  $V$  magnitude and its uncertainty, while columns (5) and (6) list  $(B - V)$  and  $(U - B)$  colours and their corresponding uncertainties. These values are not reddening-corrected. References to the sources of the integrated-light measurements are listed in column (7). Column (8) presents  $A_V$  information and corresponding uncertainties. References to the reddening information are given in column (9). Preference is given to extinction estimates based on deep CMDs. In case these were not available, extinction values retrieved from the website of the MCPS are provided [marked with dashes in column (9)]. Column (10) shows the SWB (Searle, Wilkinson & Bagnuolo 1980) type of the object; for the LMC clusters the information comes from Bica et al. (1996); SWB types of SMC clusters were recovered from the  $S$ -parameter calibration of Elson & Fall (1985). Finally, some remarks to the objects or the photometry are given in column (11).

*Notes on column (11).* (1) The information about this object in Bica et al. (1996) and van den Bergh & Hagen (1968) is completely discrepant with each other. Both values are listed with lowercase ‘b’ and ‘v’ added in parenthesis to the cluster designation.

(2) There is a foreground star superposed on the object. The flux from the star and part of the cluster was measured in a 15-arcsec diaphragm and was subtracted from the flux of the larger ( $D = 60$  arcsec) aperture encompassing the object to derive the final colours and magnitudes. The uncorrected and corrected values are listed in lowercase ‘u’ and ‘c’ in parenthesis after the cluster designation, respectively. All the data is from van den Bergh & Hagen (1968). The photometric uncertainties for the uncorrected measurements are also adopted for the corrected ones. They should be considered a lower limit.

(3) Measurements for NGC 2058 from Goudfrooij et al. (2006) and van den Bergh & Hagen (1968) are discrepant by more than one magnitude in  $V$ . A possible explanation is misidentification of the object in the earlier study. Inspection of a  $14 \times 14$ -arcmin<sup>2</sup>  $V$  image available in SIMBAD revealed several less-luminous clusters in close proximity to the object, which might have caused the overestimate of the  $V$  magnitude in van den Bergh & Hagen. The  $V$  value from Goudfrooij et al. (2006) is also listed in the table. Lowercase ‘G’ and ‘v’ are added in parenthesis to the cluster designation to indicate the origin of the photometry (Goudfrooij et al. 2006 and van den Bergh & Hagen 1968, respectively).

*References.* (1) Alcaino (1978); (2) Bernard (1975); (3) Bernard & Bigay (1974); (4) Bica et al. (1996); (5) Brocato et al. (1996); (6) Chiosi & Vallenari (2007); (7) Crowl et al. (2001); (8) Kerber, Santiago & Brocato (2007); (9) Mackey & Gilmore (2004); (10) Mighell et al. (1996); (11) Mighell, Sarajedini & French (1998b); (12) Olsen et al. (1998); (13) Testa et al. (1995); (14) van den Bergh (1981); (15) van den Bergh & Hagen (1968); (16) Walker (1992).

models have been published. Here, we will focus our attention on comparing the models by Vazdekis, Bruzual & Charlot, Anders & Fritze-v. Alvensleben, and Maraston with the integrated photometry of MC clusters presented in Paper I and in this work. Our main goals are to: (i) determine which models best reproduce the observed cluster colours; (ii) establish whether clusters of different ages and metallicities can be accurately distinguished via a combination of optical–near-IR colours; and (iii) provide information that could help improve the model predictions. Below, we first briefly discuss the colours we will use to compare observed data with SSP model predictions as well as the near-IR photometric system we will adopt in that context. We then present the actual comparisons between data and SSP model predictions for distinct age groups. The selection of clusters for each age group is described in Appendices A and B.

### 3.1 Choice of optical–near-IR colours

To select a set of optical–near-IR colours that are most applicable for a proper and meaningful comparison between observed data and SSP model predictions, we look for colours that do a good job at breaking the well-known age–metallicity degeneracy while typically delivering photometry with adequate signal-to-noise ratios (S/Ns). For this purpose, we follow the work of Puzia, Mobasher & Goudfrooij (2007) who showed that the colour combination  $B - J$  versus  $J - K$  provides very good age resolution (through  $B - J$ ), while  $J - K$  is much more sensitive to metallicity than to age (except during a brief age interval after the AGB phase transition where  $J - K$  shows a modest age dependence; see also Ferraro et al. 2000). In addition, we present  $V - J$  versus  $J - K$  colour–colour diagrams

**Table 5.** Information about the composite clusters and model performance.

Composite colours (CC)			Model predictions (MP)				CC – MP			Distance		Population properties			
$(B - J)_0$	$(V - J)_0$	$(J - K_s)_0$		$(B - J)$	$(V - J)$	$(J - K_s)$	$\Delta(B - J)$	$\Delta(V - J)$	$\Delta(J - K_s)$	$R_B$	$R_V$	$(B - J)$ versus $(J - K_s)$	$(V - J)$ versus $(J - K_s)$		
$\sigma_{(B-J)_0}$	$\sigma_{(V-J)_0}$	$\sigma_{(J-K_s)_0}$	Model <sup>(a)</sup>												
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
Old GCs (ages $\geq 10$ Gyr): 14 objects, $\langle \text{Fe}/\text{H} \rangle = -1.71$ , $\log(\mathcal{M}_{\text{tot}}) = 6.47^{+0.09}_{-0.11}$ , $\log(\mathcal{M}_{\text{LLL}}) = 4.04$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.22$															
2.11	1.51	0.56	AF03	2.24	1.57	0.60	-0.13	-0.06	-0.04	4.77	4.27				
0.05	0.04	0.01	BC03	2.11	1.44	0.60	0.00	+0.07	-0.04	4.00	4.37	>10.30	-1.74	>10.30	-1.83
			M05	2.20	1.53	0.60	-0.09	-0.02	-0.04	4.39	4.03	10.18	-2.25	10.18	$\sim -2.25$
Old GCs (ages $\geq 10$ Gyr), $[\text{Fe}/\text{H}] < -1.71$ : five objects*, $\langle \text{Fe}/\text{H} \rangle = -2.08$ , $\log(\mathcal{M}_{\text{tot}}) = 6.01^{+0.11}_{-0.14}$ , $\log(\mathcal{M}_{\text{LLL}}) = 4.00$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.18$															
2.02	1.43	0.53	BC03	2.03	1.42	0.59	-0.01	+0.01	-0.06	2.00	2.00	>10.30	-2.10	>10.30	-2.34
0.12	0.09	0.03	M05	2.12	1.49	0.57	-0.10	-0.06	-0.04	1.57	1.49	$\sim 10.10$	$< -2.25$	10.10	$< -2.25$
Old GCs (ages $\geq 10$ Gyr), $[\text{Fe}/\text{H}] \geq -1.71$ : seven objects**, $\langle \text{Fe}/\text{H} \rangle = -1.46$ , $\log(\mathcal{M}_{\text{tot}}) = 6.24^{+0.08}_{-0.10}$ , $\log(\mathcal{M}_{\text{LLL}}) = 4.07$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.26$															
2.27	1.61	0.58	V00	2.16	1.47	0.61	+0.11	+0.14	-0.03	2.66	3.81	>10.25	-1.50	>10.25	-1.28
0.05	0.04	0.02	AF03	2.29	1.60	0.62	-0.02	+0.01	-0.04	2.04	2.02	>10.18	$< -1.70$	>10.18	$< -1.70$
			BC03	2.19	1.53	0.68	+0.08	+0.08	-0.10	5.25	5.39	>10.30	-1.42	>10.30	-1.19
			M05	2.30	1.59	0.63	-0.03	+0.02	-0.05	2.57	2.55	>10.18	-1.66	$\sim 10.18$	-1.65
10 > age $\geq 2$ Gyr sample: 15 objects, $\langle \text{Fe}/\text{H} \rangle = -0.89$ , $\langle \log(r) \rangle = 9.66$ , $\log(\mathcal{M}_{\text{tot}}) = 5.68^{+0.10}_{-0.13}$ , $\log(\mathcal{M}_{\text{LLL}}) = 4.19$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.37$															
2.34	1.67	0.83	V00	2.28	1.61	0.74	+0.06	+0.06	+0.09	9.12	9.22	9.30	-0.54	9.30	-0.68
0.04	0.03	0.01	AF03	2.36	1.68	0.73	-0.02	-0.01	+0.10	10.01	10.01	9.18	-0.28	9.18	-0.70
			BC03	2.19	1.53	0.68	+0.15	+0.14	+0.15	15.46	15.71	9.22	-0.12	9.30	-0.42
			M05 <sup>(b)</sup>	2.13	1.48	0.61	+0.21	+0.19	+0.22	22.62	22.89	9.71	-0.65	9.79	-0.61
												9.42	-0.80	9.54	-0.78
10 > age $\geq 4.6$ Gyr sample, $[\text{Fe}/\text{H}] < -0.88$ : seven objects, $\langle [\text{Fe}/\text{H}] \rangle = -1.30$ , $\langle \log(r) \rangle = 9.86$ , $\log(\mathcal{M}_{\text{tot}}) = 5.55^{+0.11}_{-0.14}$ , $\log(\mathcal{M}_{\text{LLL}}) = 4.11$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.22$															
2.25	1.57	0.71	V00	2.18	1.52	0.66	+0.07	+0.05	+0.05	2.76	2.69	9.74	-1.05	9.48	-1.08
0.06	0.05	0.02	AF03	2.26	1.59	0.65	-0.01	-0.02	+0.06	3.01	3.03	9.48	-0.96	9.30	-0.96
			BC03	2.08	1.43	0.62	+0.17	+0.14	+0.09	5.32	5.30	9.43	-0.73	9.38	-0.73
			M05 <sup>(b)</sup>	2.23	1.53	0.62	+0.02	+0.04	+0.09	4.51	4.57	9.91	-0.74	9.90	-0.75
												9.52	-1.35	9.51	-1.35
4.6 > age $\geq 2$ Gyr sample, $[\text{Fe}/\text{H}] \geq -0.88$ : eight objects, $\langle [\text{Fe}/\text{H}] \rangle = -0.52$ , $\langle \log(r) \rangle = 9.36$ , $\log(\mathcal{M}_{\text{tot}}) = 5.08^{+0.08}_{-0.09}$ , $\log(\mathcal{M}_{\text{LLL}}) = 3.98$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.28$															
2.43	1.77	0.92	V00 <sup>(c)</sup>	2.31	1.67	0.76	+0.12	+0.10	+0.16	8.54	8.67	9.15	0.20		
0.04	0.03	0.02	AF03	2.56	1.84	0.83	-0.13	-0.07	+0.09	5.86	5.07	8.89	0.40	8.84	0.00
			BC03	2.40	1.66	0.77	+0.03	+0.11	+0.15	7.54	8.35	9.21	0.21	9.17	0.20
			M05 <sup>(d)</sup>	2.44	1.74	0.90	-0.01	+0.03	+0.02	1.03	1.41	9.50	-0.59	9.60	-0.65
												9.37	-0.61	9.38	-0.57
														8.62	0.35
2 > age $\geq 1$ Gyr sample: 17 objects***, $\langle [\text{Fe}/\text{H}] \rangle = -0.45$ , $\langle \log(r) \rangle = 9.15$ , $\log(\mathcal{M}_{\text{tot}}) = 5.55 \pm 0.06$ , $\log(\mathcal{M}_{\text{LLL}}) = 3.75$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.11$															
2.13	1.60	0.88	V00	2.35	1.74	0.86	-0.22	-0.14	+0.02	7.40	7.07	9.00	-0.21		
0.03	0.02	0.02	AF03	2.40	1.75	0.81	-0.27	-0.15	+0.07	9.06	8.28	8.88	0.13	8.80	0.05
			BC03	2.24	1.61	0.83	-0.11	-0.01	+0.05	4.44	2.55	8.77	0.15	9.00	0.15
			M05 <sup>(e)</sup>	2.64	1.94	1.14	-0.51	-0.34	-0.26	21.40	21.40	9.26	-1.35	9.26	-1.35
												8.52	0.24	8.59	0.00

since the  $V$  band typically provides a higher S/N in observations than the  $B$  band.

### 3.2 Stochastic effects in the stellar populations

When a comparison between observations of star clusters and theoretical predictions is performed, it is important to keep in mind that models assume that clusters are sufficiently massive that all stages of stellar evolution are well sampled. Predictions of any model based on these assumptions will match the observations only in the limit of a sufficiently large number of observed stars. The mass of real stellar systems thus drives the validity of comparison with model predictions.

The level of stochastic fluctuations which arise at different total cluster masses has been addressed in a number of previous studies (e.g. Lançon & Mouhcine 2000; Bruzual 2002; Cerviño & Luridiana 2004). Most notably, Lançon & Mouhcine calculate the minimum masses of a stellar population with solar metallicity that ensure that

the luminosity fluctuations are less than 10 per cent of the mean luminosity ( $\mathcal{M}_{(10\text{ per cent})}$ ),  $\sigma_L/L \leq 10$  per cent (roughly corresponding to  $\sigma = 0.1$  mag) for several photometric passbands. Cerviño & Luridiana (2004) define a ‘lowest luminosity limit’ (LLL) which requires the total luminosity of a modelled cluster to be larger than the contribution of the brightest star included in the isochrones, and show that the highest LLL masses are derived for the  $K$  band. Any object which complies with these mass limits provides a meaningful comparison for the entire range of optical–near-IR colours in our study. Below, we check whether our composite clusters are more massive than the implied LLL masses by comparing the most-luminous star in the isochrone (at the mean age and metallicity of each composite cluster) with the estimated cluster mass (described below). Using the online tool CMD 1.2L<sup>4</sup> provided by L. Girardi, we adopt a Kroupa (2001) initial mass function (IMF) corrected for

<sup>4</sup> Available at <http://stev.oapd.inaf.it/lgirardi/cgi-bin/cmd>.



Table 5 – continued

Composite colours (CC)			Model predictions (MP)				CC – MP			Distance		Population properties			
$(B - J)_0$	$(V - J)_0$	$(J - K_S)_0$	Model <sup>(a)</sup>	$(B - J)$	$(V - J)$	$(J - K_S)$	$\Delta(B - J)$	$\Delta(V - J)$	$\Delta(J - K_S)$	$R_B$	$R_V$	$(B - J)$ versus $(J - K_S)$	$(V - J)$ versus $(J - K_S)$		
$\sigma_{(B-J)_0}$	$\sigma_{(V-J)_0}$	$\sigma_{(J-K_S)_0}$										$\log(\tau)$	$[\text{Fe}/\text{H}]$	$\log(\tau)$	$[\text{Fe}/\text{H}]$
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)	(16)
1 Gyr > age $\geq$ 200 Myr sample: eight objects, $\langle[\text{Fe}/\text{H}]\rangle = -0.34$ , $\langle\log(\tau)\rangle = 8.60$ , $\log(\mathcal{M}_{\text{tot}}) = 5.04^{+0.05}_{-0.06}$ , $\log(\mathcal{M}_{\text{LLL}}) = 3.60$ , $\log(\mathcal{M}_{(10\text{ per cent})}) = 5.05$															
1.09	0.95	0.60	AF03	1.85	1.59	0.95	-0.76	-0.64	-0.35	25.83	27.59				
0.04	0.03	0.02	BC03	1.24	1.01	0.72	-0.15	-0.06	-0.12	7.08	6.33	8.64	-0.89	8.78	-0.89
			M05	2.10	1.66	1.01	-1.01	-0.71	-0.41	32.52	31.31	8.40	-1.35	8.41	-1.35

*Notes.* Columns (1)–(3) list the weighted mean colours of the composite clusters, along with their corresponding errors. The number of clusters combined in each composite, their mean ages and metallicities plus the total accumulated mass are shown on the line above the colours. Masses associated with the LLL  $\mathcal{M}_{\text{LLL}}$  and 10 per cent accuracy limit  $\mathcal{M}_{(10\text{ per cent})}$  are presented for comparison. Columns (4)–(12) show the results of the model and data comparison. Column (4) denotes the model: M05 stands for Maraston (2005), BC03 for Bruzual & Charlot (2003), AF03 for Anders & Fritze-v. Alvensleben (2003), and V00 for Vazdekis (1999). Columns (5)–(7) give the interpolated colours predicted by the models for the mean ages and metallicities of the composite clusters. The corresponding differences in colour space (data minus model predictions) are given in columns (8)–(10). Finally, columns (11) and (12) give a distance between the positions predicted by the models and the composite cluster locations calculated as  $R_X = \sqrt{(\Delta C1/\sigma_{C1})^2 + (\Delta C2/\sigma_{C2})^2}$ , where  $\Delta C_i$  is the corresponding colour difference and  $\sigma_{C_i}$  is the uncertainty of the mean colour of the composite cluster.  $R_V$  stands for the distance in the  $(J - K_S)$  versus  $(V - J)$  colour–colour space, and  $R_B$  for the  $(J - K_S)$  versus  $(B - J)$  distance. The composite colours and corresponding uncertainties are calculated by summing the flux of the clusters in the corresponding subpopulation. The cumulative mass in each composite cluster is calculated as the sum of the individual cluster masses.

The following objects were excluded from the corresponding composite clusters (marked with the asterisks in the table) due to possible foreground/background contamination and/or small aperture diameters of the optical photometry.

\*NGC 1939 is excluded from the mean.

\*\*NGC 1928 is excluded from the mean.

\*\*\*NGC 1777 is excluded from the mean.

<sup>(a)</sup>We did not extrapolate in cases when the ages and metallicities of the composite clusters were out of the parameter space covered by the models. This is affecting the comparisons in the cases of ‘old’ GCs and for the youngest age bin. A rough estimate of the model performance in these cases can be obtained from the figures, showing the data for the corresponding age bins (see Figs 3, 4 and 7–10).

<sup>(b)</sup>In this case, there is degeneracy in the Maraston (2005) model predictions, in the sense that 10- and 4-Gyr isochrones are overlapping in the colour–colour space. The composite-cluster ages and metallicities inferred by the models with respect to the 4-Gyr isochrone are listed in the table on the row below the model predictions for the 10-Gyr isochrone.

<sup>(c)</sup>Some degeneracy is present for the 1-Gyr isochrone of Vazdekis (1999), especially in the  $(V - J)$  versus  $(J - K_S)$  colour–colour space.

<sup>(d)</sup>The properties of the composite cluster for the younger subsample in the  $10 > \text{age} \geq 2$  Gyr age bin are derived taking into account the degeneracy due to the intercept of the 10- and 4-Gyr isochrones. In the  $(V - J)$  versus  $(J - K_S)$  colour–colour diagram, the corresponding data also fall in the parameter space covered by the clusters with ages between 200 and 500 Myr. Ages and metallicities inferred by the M05 model for each of these cases are listed in columns (13)–(16) of the table: the first line (with respect to the 10-Gyr isochrone), second (4-Gyr isochrone) and third (200–500 Myr case).

<sup>(e)</sup>Colour degeneracy between 1–2 Gyr and 200 Myr–1 Gyr M05 models. The inferred stellar population properties are listed in the first (1–2 Gyr case) and second (200 Myr–1 Gyr) line of columns (13)–(16) in the table.

binaries (his equation 6), and find that all of our composite clusters easily satisfy the less-stringent LLL criterion. The LLL masses that we use are given in Table 5, and have been corrected for the difference in the adopted lower mass limits ( $0.01 M_\odot$  in Cerviño & Luridiana and  $0.1 M_\odot$  in this work). Cerviño & Luridiana (2004) compare their values of LLL with the  $\mathcal{M}_{(10\text{ per cent})}$  masses derived by Lançon & Mouhcine, scaled for differences in the adopted IMF between the two works. These scaled values of  $\mathcal{M}_{(10\text{ per cent})}$  are also presented in Table 6. This  $\mathcal{M}_{(10\text{ per cent})}$  limit is closely matched by composite cluster (age bin: 2–4.6 Gyr) and surpassed by all others, ensuring a robust comparison between our measurements and model predictions.

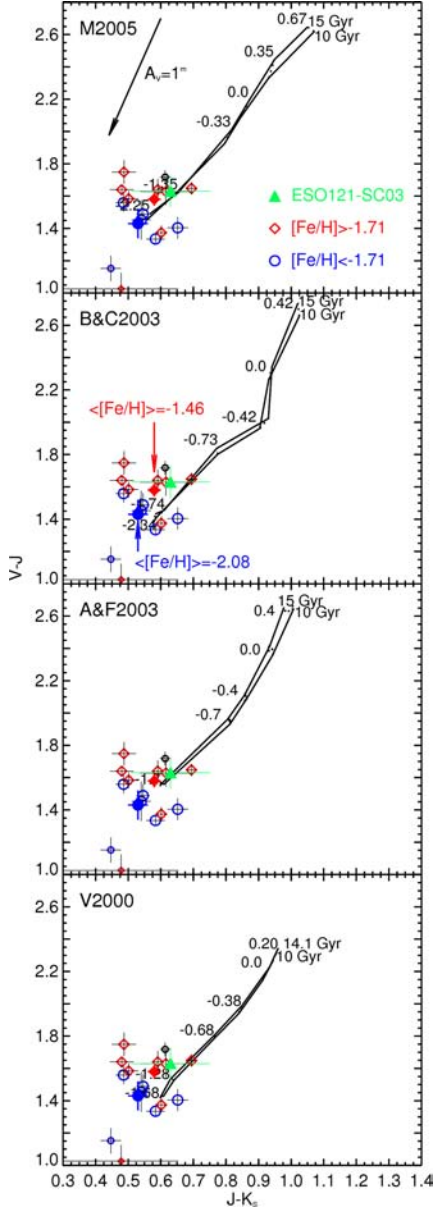
### 3.3 The old cluster population

Integrated  $JHK_S$  magnitudes were measured within the apertures of the optical photometry for all old clusters listed in Table B1. The photometry is presented in Table B2. We note that the data in the table are *measured* magnitudes, not corrected for reddening. A reddening correction is, however, applied when plotting the objects on the model grids in Figs 3–16. Reddening values based on deep CMDs from the literature are used where available. For the rest of

the sample, reddening estimates based on photometric information from the MCPS are applied.

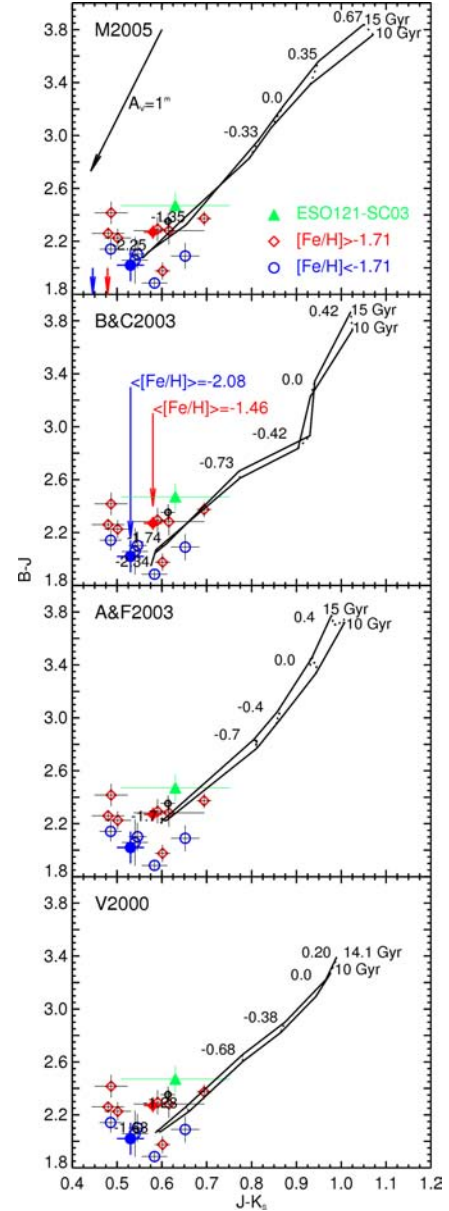
In Figs 3 and 4, we show a comparison between the model predictions and reddening-corrected colours for the 15 old MC star clusters in our sample. The error bars include uncertainties in the photometry, reddening correction, and an estimate of the error due to the statistical fluctuations within the field stellar population in the vicinity of each cluster. The most-significant outliers, NGC 1928 and NGC 1939 (the two points in the lower left-hand part of Fig. 3), suffer from significant crowding due to their location in the LMC bar (see the remarks about NGC 1928 in Section 2.1). This likely affected their optical photometry measurements, which were retrieved from the literature.<sup>5</sup> However, the measured colours for most (other) clusters are generally in good agreement with the model predictions.

<sup>5</sup> For example, Elson & Fall (1985) derived  $S = 22$  (age  $\sim 50$  Myr) for NGC 1928 based on the integrated-light colours from van den Bergh (1981). This contradicts the results of Mackey & Gilmore (2004) based on high-resolution *HST*/ACS imaging, demonstrating clearly that the field contamination in the LMC bar region can significantly affect the integrated-light measurements if not properly accounted for.



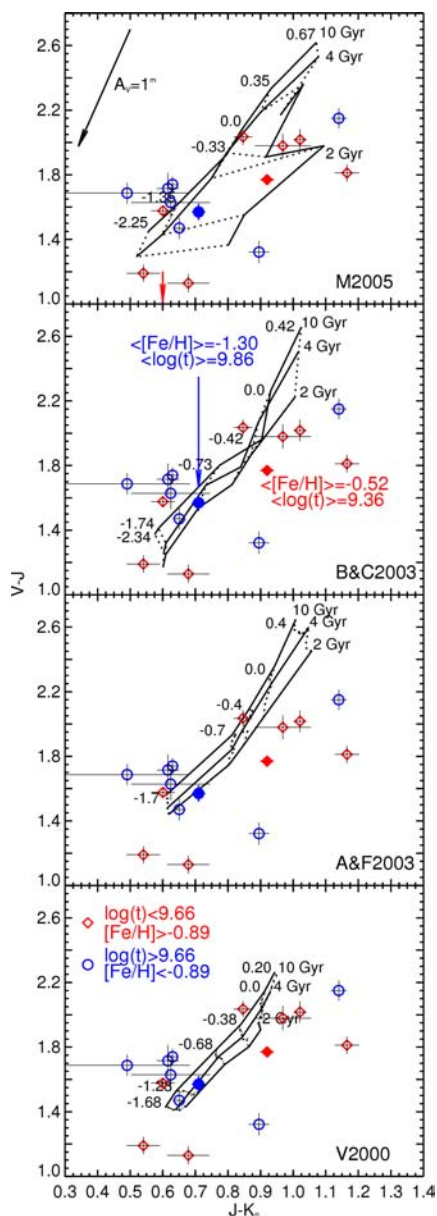
**Figure 3.**  $(V - J)$  versus  $(J - K_s)$  colour-colour diagrams for the old clusters. Isochrones for 10 and 15 Gyr are plotted with the solid lines and metallicity values are marked along them. The panels present the models of Maraston, Bruzual & Charlot, Anders & Fritze-v. Alvensleben and Vazdekis from the top to bottom panel, respectively. The reddening vector is shown in the top panel. The two outliers are NGC 1928 (small red diamond) and NGC 1939 (small blue circle). NGC 1916 (small black circle) suffers from differential reddening (no age and metallicity available). The 9-Gyr-old cluster ESO121-SC03 is shown as a green triangle. Clusters with metallicities lower than the mean value for the sample are plotted as the blue circles, while the others are denoted with the red diamonds. The mean colours for each of those subsamples are shown as the filled blue circle and red diamond, respectively. The corresponding mean  $[\text{Fe}/\text{H}]$  values are shown in the second panel.

As mentioned in the previous section, it is possible that stochastic fluctuations in the number of (e.g. giant) stars will cause a spread in cluster colours at any given age and metallicity. In order to assess this effect, we estimate the stellar mass which contributes to our integrated magnitudes for each MC cluster as follows. We use our extinction-corrected  $J$ -band magnitude (the 2MASS and Bessell &



**Figure 4.**  $(B - J)$  versus  $(J - K_s)$  colour-colour diagrams for the old clusters. As in Fig. 3 two different isochrones are plotted and metallicity values are marked. The panels are organized in the same order, with an extinction vector shown in the top panel. The two clusters, NGC 1928 and NGC 1939, fall outside the diagrams, and the directions towards them are marked with the red and blue arrows, respectively. NGC 1916 is shown as a small black circle.

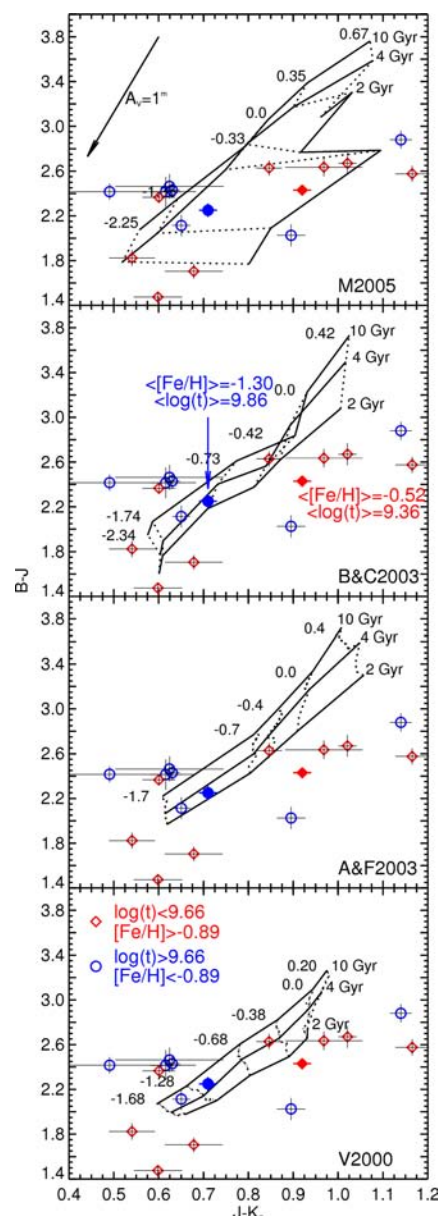
Brett photometric systems are closest in  $J$  and the 2MASS survey has its highest sensitivity in  $J$ , combined with the  $J$ -band mass-to-light ratios ( $M/L$ s) predicted by the Maraston (2005) models which assume a Kroupa (2001) IMF. These estimates of the stellar mass contributing to each observed colour are presented in Table B2. For comparison, we include mass estimates from McLaughlin & van der Marel (2005) which are determined from profile fitting (to determine the total cluster luminosity) combined with  $M/L_V$  determined from SSP model fitting of each cluster (assuming the BC03 models with a Chabrier-disc IMF). While the two estimates are in reasonable agreement, our masses are systematically lower. We found that the main driver of this difference is the systematically lower total cluster



**Figure 5.**  $(V - J)$  versus  $(J - K_s)$  colour–colour diagrams for the clusters between 2 and 10 Gyr. The isochrones for three different ages are plotted with the solid lines and metallicity values are marked along the model tracks for 10 Gyr. The black dotted lines stand for equal metallicity. The four panels show four SSP models as in Fig. 3. A reddening vector for  $A_V = 1$  mag is shown in the top panel. A legend to the individual symbols is provided in the bottom panel. The composite subsamples are marked with the filled symbols, along with their errors (colour-coded solid lines). The mean age and metallicity for each subsample are indicated in the second panel. The red arrow points to the position of *Hodge 4*, falling outside the boundaries of the plotted colour–colour space.

luminosities compared to the values determined by McLaughlin & van der Marel (2005). This effect could be predicted since we do not extrapolate the cluster light outside the aperture size used for the optical photometry. Secondary effects in the mass differences between the two works come from differences in the adopted ages and metallicities, and hence SSP  $M/L$ .

We divide the old cluster sample by metallicity into two subsamples, accumulating enough mass in each bin to render the effects

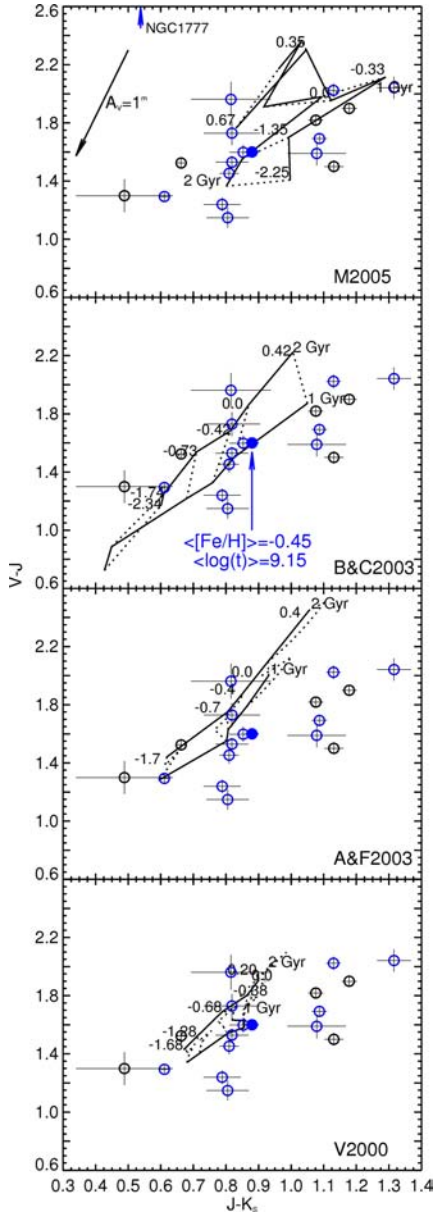


**Figure 6.** The same as Fig. 5, but for  $(B - J)$  versus  $(J - K_s)$ .

of stochastic fluctuations negligible. Clusters with  $[\text{Fe}/\text{H}] < -1.71$  are designated as ‘metal-poor’ and shown as the open blue circles in Figs 3 and 4), and those with  $[\text{Fe}/\text{H}] > -1.71$  are referred to as ‘metal-rich’ (depicted as open red diamonds). The mean magnitudes and colours corresponding to the objects of the subsample are calculated from the sum of the fluxes of individual objects in each bin.

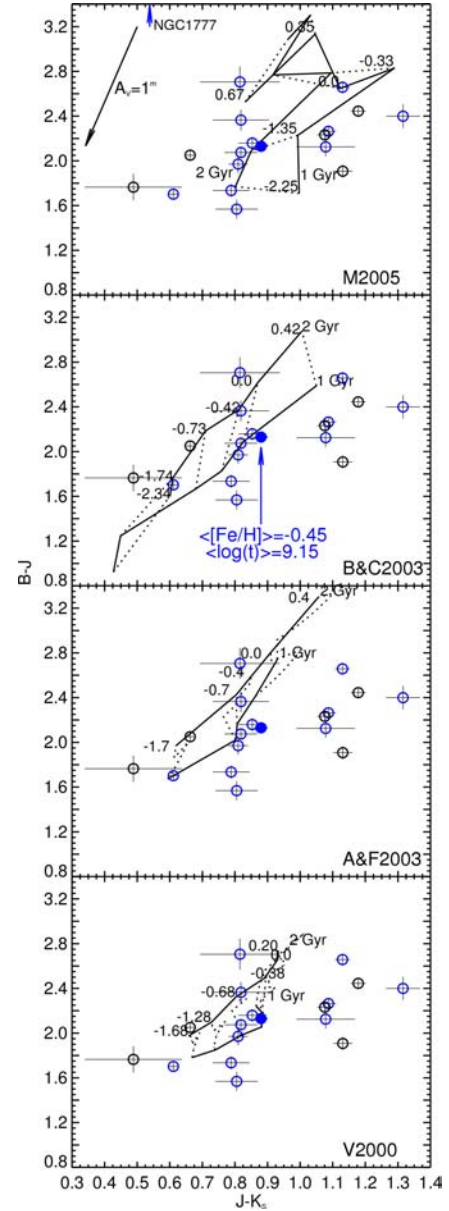
The metal-poor and metal-rich subsamples have mean  $[\text{Fe}/\text{H}]$  values of  $-2.08$  and  $-1.46$  dex, respectively, and are presented along with the resulting metallicities (filled blue circle for the metal-poor clusters and filled red diamond for the metal-rich ones). ESO121–SC03, the  $\sim 9$  Gyr cluster in the LMC, is also shown on these figures as a green triangle. The metal-rich and metal-poor GC colours clearly separate in the optical–near-IR colour–colour space, and generally follow the model predictions.

To provide a quantitative measure (and a summary) of the performance of the different models in terms of fitting the average colours



**Figure 7.**  $(V - J)$  versus  $(J - K_S)$  colour-colour diagrams for the clusters between 1 and 2 Gyr. Isochrones for the different ages are plotted with the solid lines and metallicity values are marked along the 2-Gyr isochrone. The four panels show four SSP models as in Figs 3–6. The blue circles represent clusters with reliable age and metallicity estimates retrieved from the literature, while the black circles denote the objects added to the sample on the basis of our  $S$ -parameter re-calibration (see Appendix A). The composite cluster is marked by a filled circle, along with its error (solid blue lines). The mean age and metallicity are indicated in the second panel.

of the various subsamples, we compiled the relevant information in Table 5 (for *all* age groups). The mean colours of the composite clusters are listed there along with the interpolated model predictions for the ages and metallicities corresponding to the composite points (using linear interpolation between adjacent model isochrones and iso-metallicity grid lines), as well as the measured colour differences between the data and the model predictions (we will hereafter refer to these colour differences as ‘absolute colour residuals’). In Table 5, we also present the inferred ages and metallicities of the

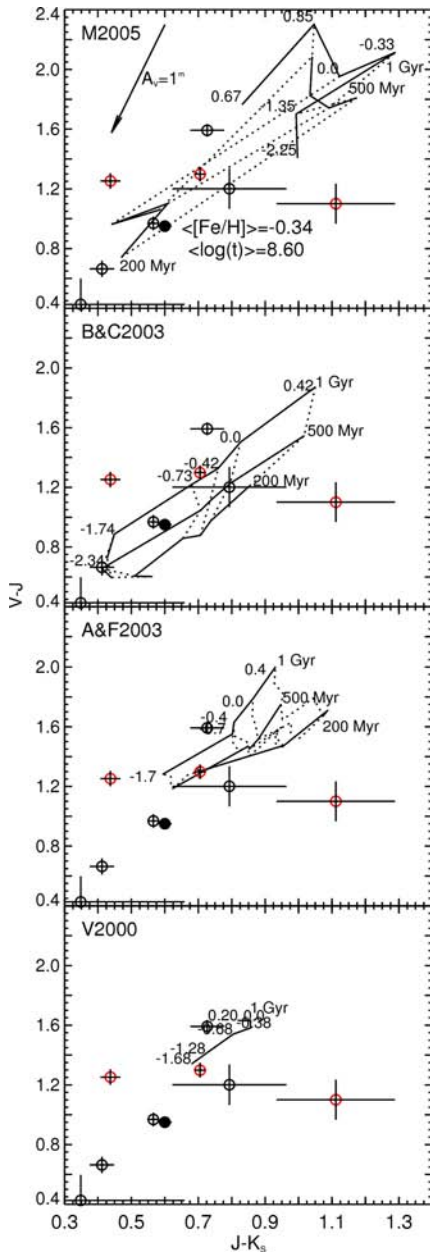


**Figure 8.** The same as Fig. 7, but for  $(B - J)$  versus  $(J - K_S)$ .

composite clusters according to the models. In some cases, it is not possible to derive reliable stellar population properties due to insufficient coverage of the model grids (those are left blank in the table). For the old metal-rich cluster subsample ( $\langle [\text{Fe}/\text{H}] \rangle = -1.46$ ), *all* models (Vazdekis 1999; Bruzual & Charlot 2003; Maraston 2005) infer ages exceeding the corresponding oldest model isochrones. Maraston models with Blue Horizontal Branch (BHB) are in a good agreement with the mean composite cluster ages for the entire old cluster sample and the metal-poor ( $\langle [\text{Fe}/\text{H}] \rangle = -2.08$ ) subsample, although the inferred metallicities are a little lower than the mean values for each composite point.

Inspection of Table 6 shows that the models of Maraston (2005) (with BHB) provide the best overall match to the observations of old clusters, especially in terms of estimating their ages, while the Bruzual & Charlot (2003) models formally do the best job of estimating SSP metallicities.

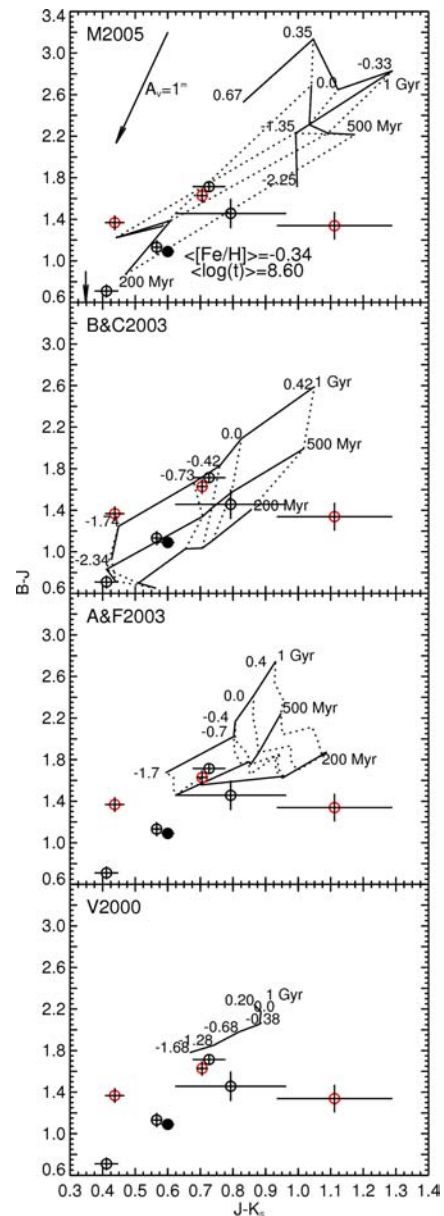




**Figure 9.**  $(V - J)$  versus  $(J - K_S)$  colour-colour diagrams for the clusters between 200 Myr and 1 Gyr. The information (order of presentation of the models, extinction) is shown as in the figures for the other age bins. Three isochrones are plotted for each model (except for V2000 whose models do not include colour information for ages younger than 1 Gyr). The dotted lines show equal metallicities, and their values are marked along the 1-Gyr isochrone. The red circles represent clusters with reliable age and metallicity estimates retrieved from the literature, and the black circles denote the objects added to the sample on the basis of our  $S$ -parameter re-calibration. The composite cluster is marked with the filled black symbol, along with its error (solid lines). Its mean age and metallicity are indicated at the top panel.

### 3.4 The $2 \leq \text{age} < 10$ Gyr cluster population

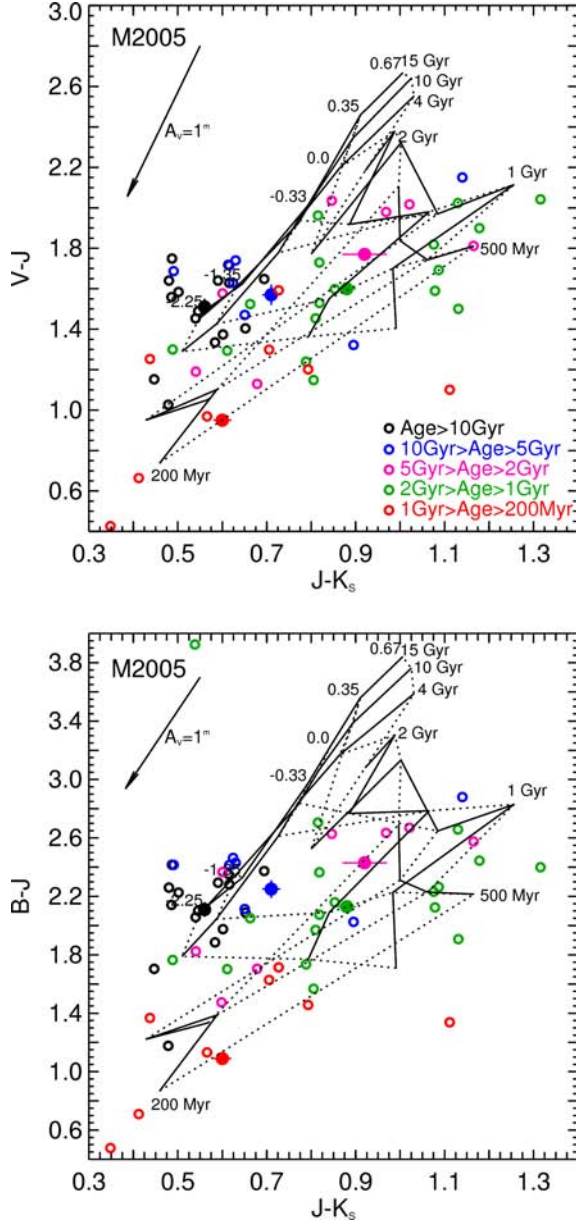
Nine LMC and six SMC clusters with adequate age and metallicity measurements were selected in this age interval. Information on the cluster ages, metallicities and masses are compiled in Tables B1 and B2. A comparison between our photometry and the model tracks in  $V - J$  versus  $J - K_S$  and  $B - J$  versus  $J - K_S$  colour-colour



**Figure 10.**  $(B - J)$  versus  $(J - K_S)$  colour-colour diagrams for the clusters between 200 Myr and 1 Gyr. Generally, the notes are the same as for the 200 Myr–1 Gyr  $(V - J)$  versus  $(J - K_S)$  colour-colour diagram. The only difference is the black arrow in the top panel, pointing towards the position of NGC 2156, which in this case is located out of the colour boundaries of the panels.

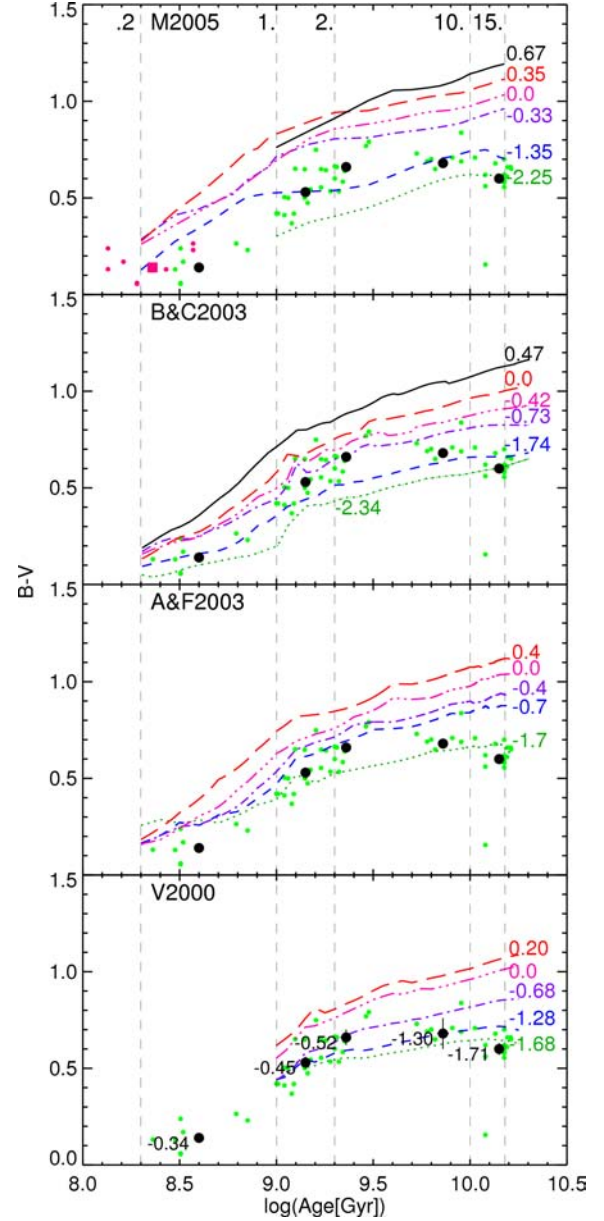
diagrams are shown in Figs 5 and 6, respectively. We further divide the 2–10 Gyr sample into two subsamples, with ages older than and younger than 4.6 Gyr. When compared with the Maraston (2005) models, these show that generally the younger subsample agrees with the predicted location of the 2 Gyr model, and that the older bin also falls in the expected region of colour-colour space.

Because this bin includes a large range of ages and some of the individual clusters have stellar mass estimates lower than  $\mathcal{M}_{\text{LLL}}$  (see Section 3.2), one can expect some scatter among the individual measurements with respect to the model predictions, which is indeed observed. Most of our mass estimates in this age bin are systematically lower than those of McLaughlin & van der Marel (2005)



**Figure 11.** Data of all 54 clusters from our test sample on top of the grid of Maraston (2005) models in the  $(V - J)$  versus  $(J - K_s)$  and  $(B - J)$  versus  $(J - K_s)$  colour–colour space. The individual points are colour-coded according to the age of the object (see the legend). The mean colours for each age bin are presented with the filled circles. The error bars show the corresponding error of the mean colour.

(see Section 3.3 for possible explanation). The composite clusters representing the entire sample in this age range and the metal-poor older subpopulation ( $4.6 \leq \text{age} < 10$  Gyr) both accumulate masses exceeding  $\mathcal{M}_{(10\text{ percent})}$ , so that the composite colours ought to yield meaningful comparisons to the SSP model predictions. Unfortunately, this is not quite the case for the younger metal-rich subpopulation ( $2 \leq \text{age} < 4.6$  Gyr). These clusters do, however, exceed  $\mathcal{M}_{\text{LLL}}$  by a factor of  $\sim 10$ , so while we might expect some bias in the colours it is certainly worth presenting information in this age range in Table 6. We point out that these results must be treated with some caution. Reliable ages and metallicities are needed for more clusters in this particular age interval in order to provide more accu-



**Figure 12.**  $(B - V)$  colour predicted by the models of Maraston (2005), Bruzual & Charlot (2003), Anders & Fritze (2003) and Vazdekis (1999) (from the top to bottom panel) as a function of age for different metallicities (labelled at the end of the colour-coded lines). The vertical dashed lines depict the boundaries of the age bins adopted in this study. The reddening-corrected colours of the individual clusters from our sample are represented with the small green dots. The solid black points show the mean colours of the subsamples, labelled by corresponding mean metallicities. The positions of the clusters in the youngest age bin when taking into account the ages derived by the  $S$ -parameter calibration of Girardi et al. (1995) are shown as the magenta dots on the top panel (the magenta square stands for the mean colour in this case). The prominent outlier in the oldest age bin is NGC 1928.

rate comparison between model predictions and observed properties of the stellar populations.

All four sets of models reproduce the mass-weighted average colours reasonably well in terms of quantitative colour differences (see Table 5). ages and metallicities inferred by *all* SSP models for the three composite clusters in this age interval are also listed in the table. There is some degeneracy present in the Maraston (2005)

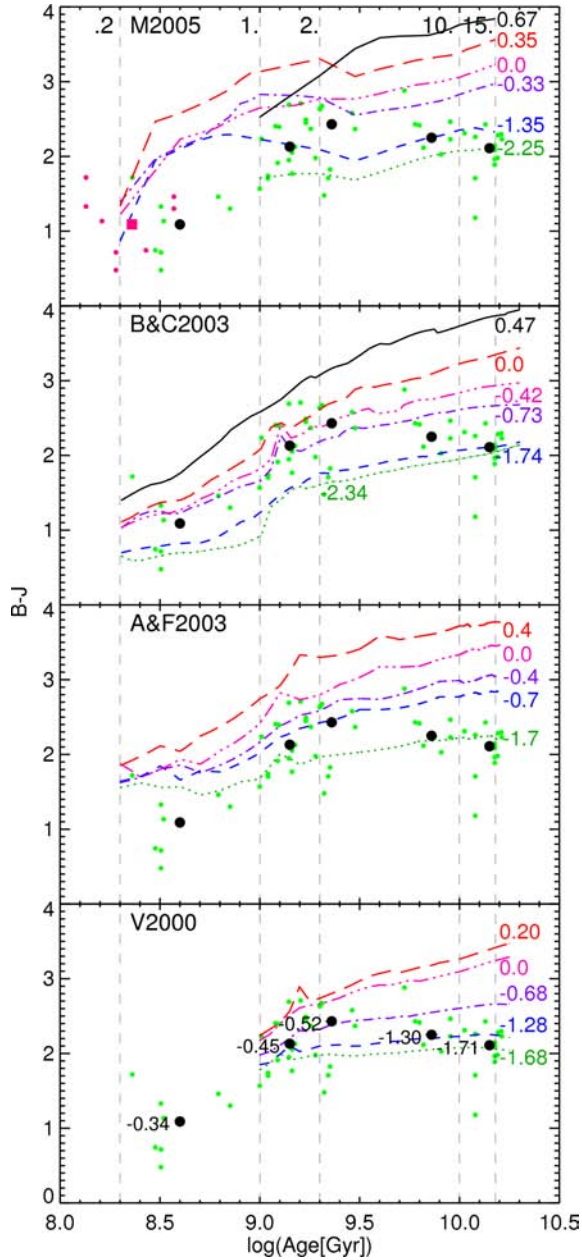


Figure 13. The same as Fig. 12, but for  $(B - J)$  colour.

models in this regime due to the intersection of the 10- and 4-Gyr isochrones in colour–colour space. Taking this into account, it is not possible to infer a single value for the stellar population’s age or metallicity. Stellar population properties measured with respect to different Maraston isochrones are listed in Table 5. There is good agreement between the mean ages of the composite clusters and the ages inferred by the model, but the corresponding metallicities are typically lower. Generally, all models provide consistent stellar population properties between both colour–colour diagrams typically showing somewhat lower ages and higher metallicities. In some cases, differences are observed in the inferred properties of the stellar populations for some subsamples in this age interval (see Table 5), when predictions are based on  $(V - J)$  versus  $(J - K_S)$  versus the  $(B - J)$  versus  $(J - K_S)$  colour–colour diagrams. Note that all models (except Maraston) infer supersolar metallicities for the

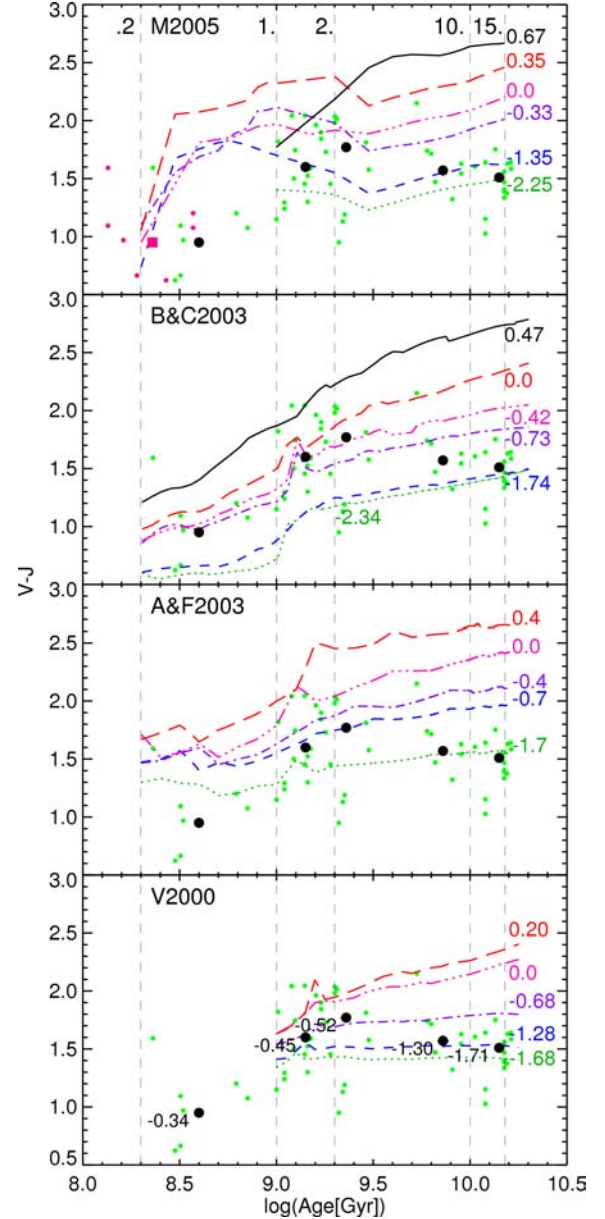


Figure 14. The same as Fig. 12, but for  $(V - J)$  colour.

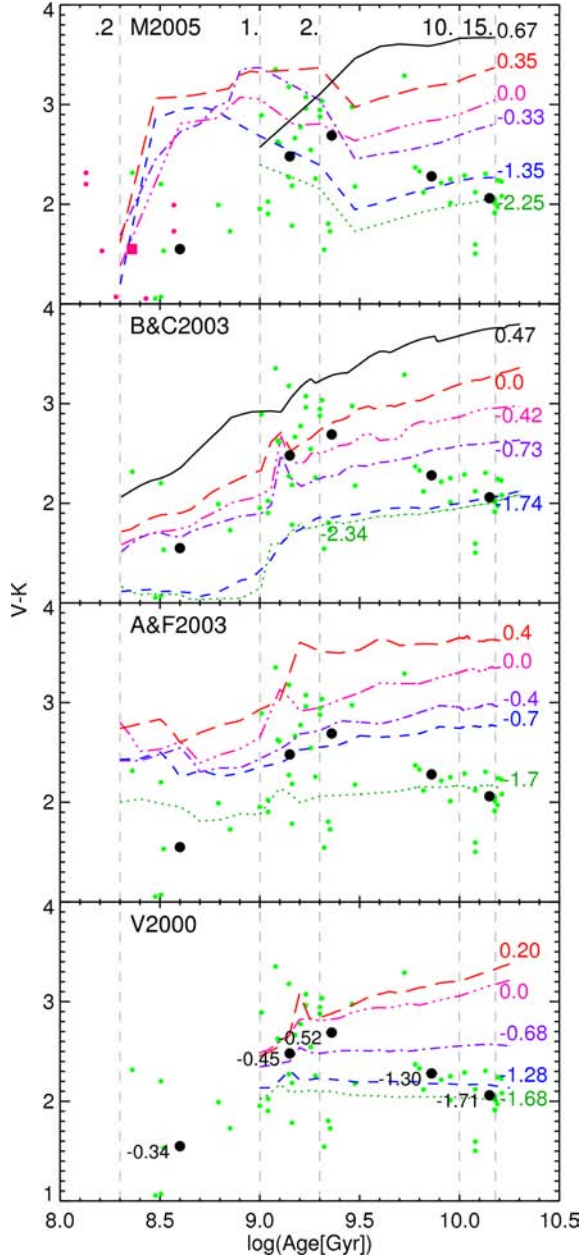
( $2 \leq \text{age} < 4.6$  Gyr) subpopulation. Further investigation is needed to determine whether it is a model ingredient or assumption that is responsible for the mismatch, or whether this mismatch occurs due to insufficient mass accumulated in the age bin.

Overall the Maraston (2005) models provide the best inference about the properties of the stellar populations in this age range.

### 3.5 The $1 \leq \text{age} < 2$ Gyr cluster population

Eleven LMC and two SMC clusters with adequate age and metallicity measurements from CMDs and/or spectroscopy of individual giant stars were selected in this age interval (see Tables B1 and B2). Our photometry and the model tracks in  $V - J$  versus  $J - K_S$  and  $B - J$  versus  $J - K_S$  colour–colour space are compared in Figs 7 and 8. This age interval covers a period after the ‘AGB phase transition’, that is, the onset of the AGB phase and coincides with the development of the red giant branch (RGB). Therefore,

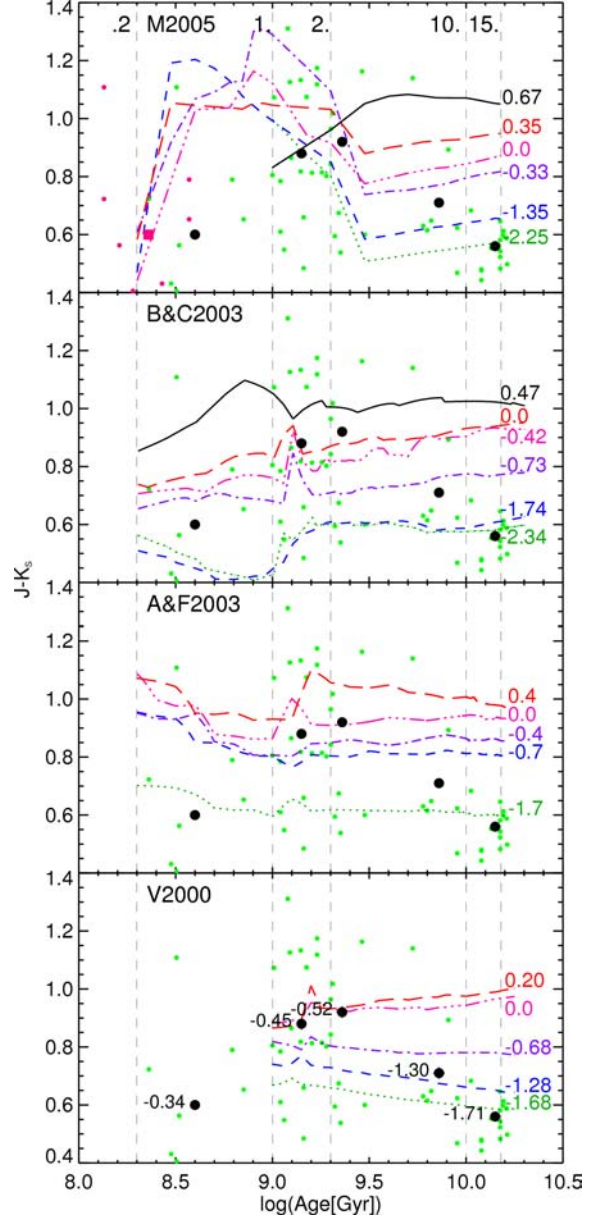




**Figure 15.** The same as Fig. 12, but for  $(V - K_S)$  colour.

a significant impact on the light output in the near-IR (especially in the  $K$  band) is expected. Hence, it is important to maximize the number of objects so as to accumulate enough mass and decrease the effects of the stochastic fluctuations in the stellar population. We added five clusters to our composite based on their re-calibrated ‘ $S$ -parameter’ values (the  $S$ -parameter is an age indicator based on integrated  $U - B$  and  $B - V$  colours, see Elson & Fall 1985; Girardi et al. 1995). Our re-calibration of the  $S$ -parameter based on recent cluster age determinations is described in detail in Appendix A. The total mass of the composite cluster with ages between 1 and 2 Gyr is  $\mathcal{M}_{\text{tot}} = 3.6 \times 10^5 \mathcal{M}_{\odot}$ , which exceeds  $\mathcal{M}_{(10 \text{ percent})}$ .

Overall, the colours of clusters in this age range agree reasonably well with the SSP model predictions. Maraston models most accurately reproduce the age of the composite cluster, although it indicates too low a metallicity. The latter is the reason why the



**Figure 16.** The same as Fig. 12, but for  $(J - K_S)$  colour.

Maraston model has the largest colour residual for this age range in Table 5. The performance of the other three models in this age range is similar to one another: they all indicate an age that is somewhat too young and a metallicity that is somewhat too high, but the absolute colour residuals are smaller than that of the Maraston model. Quantitatively, the Bruzual & Charlot (2003) model comes out best in this age range in terms of absolute colour residuals.

### 3.6 The 200 Myr $\leq$ age < 1 Gyr cluster population

In this age range, we identified only three clusters (two in the LMC and one in the SMC) with reliable age and metallicity estimates based on presently available deep CMDs (see Table B1). As in the previous age bin, we added other clusters based on our re-calibration of the  $S$ -parameter (see Appendix A), resulting in the addition of five objects to this age bin. Model tracks in the  $V - J$  versus  $J - K_S$  and  $B - J$  versus  $J - K_S$  colour-colour space are presented



along with our photometry results in Figs 9 and 10. The total mass of the composite cluster of this age range is  $\mathcal{M}_{\text{tot}} = 1.1 \times 10^5 \mathcal{M}_{\odot}$ , as listed in Table 5. Unfortunately, this barely exceeds  $\mathcal{M}_{(10 \text{ per cent})}$ . More reliable age and metallicity estimates are needed for MC star clusters in this age interval to be able to provide calibration data that could be crucial to improve the treatment of the AGB phase and perform further tests of the models. Overall, the Bruzual & Charlot (2003) and Maraston (2005) models perform best in this age range. The models of Bruzual & Charlot (2003) and Maraston (2005) yield similar metallicity estimates, which are *too low*. Bruzual & Charlot (2003) overestimate slightly the mean age of the composite cluster, while Maraston (2005) infer age that is younger. The Bruzual & Charlot (2003) models have the smallest colour residuals in this age range.

### 3.7 The complete sample

In Fig. 11, we present the entire cluster sample, from 200 Myr to 12 Gyr, studied in the previous sections. One of the main attractions for using a combination of reddening-corrected optical and near-IR integrated colours is that it is supposed to break the age–metallicity degeneracy. Can it actually do this? First, we note the important caveat that in the MCs, the typical cluster mass increases with age. This is partly a statistical effect (e.g. Hunter et al. 2003; Whitmore, Chandar & Fall 2007), due to the fact that the younger age bins cover shorter times, and fewer clusters formed originally in these shorter time-intervals, leading statistically to a somewhat lower typical cluster mass at younger ages. The large spread in intrinsic colours among young clusters is due in part to the low masses of these clusters which naturally causes stochastic fluctuations in the numbers of massive IR-luminous stars. Another contributor to the larger spread in colours is the fact that the IR-luminous stars in these objects (i.e. the AGB stars) have shorter lifetimes and higher luminosities relative to their counterparts at older ages (i.e. RGB stars). Despite these effects, we find that, overall, clusters in different age bins do in fact appear to occupy different regions of colour–colour space, although with a relatively large spread. The solid points reflect the mean colour for each age bin discussed in the previous sections, most of which have accumulated masses larger than  $\mathcal{M}_{(10 \text{ per cent})}$ . The solid points in Fig. 11 suggest that the following conclusions can be safely drawn for massive SSPs based solely on the combination of  $B - J$  and  $J - K$  (or  $V - J$  and  $J - K$ ) colours: (i) ages older than roughly 9 Gyr can be separated from those younger than  $\approx 5$  Gyr; (ii) ages of  $\approx 2$  Gyr can be adequately separated from those older than  $\approx 5$  Gyr; and (iii) finally, ages younger than 1 Gyr separate nicely from those older than 1 Gyr.

### 3.8 Age–colour comparison

In this section, we compare the observed cluster colours and the mean subsample colours with model predictions as a function of age. Integrated-light colour age evolution is a basic SSP model prediction and MC clusters are the only objects that allow these predictions to be tested for intermediate ages. This information is shown here to provide feedback to model builders by identifying ages at which the discrepancies occur, hence pointing to the responsible stages of stellar evolution and model ingredients that need further attention and refinement. Results for several optical and near-IR colours are presented in Figs 12–16.

The  $(B - V)$  colour is presented in Fig. 12. The clusters in our test sample comply with the LLL criterion (see Section 3.2) in the optical and the distribution of the individual points around the model tracks

is reasonably tight. There is good agreement between the properties of the composite clusters and the model predictions. The correlation between age and optical colours is well illustrated in this figure as well as the relatively poor metallicity resolution.

Figs 13–16 present combinations of optical–near-IR colours (except for  $(J - K_s)$  in Fig. 16). These illustrate that the majority of the models tested in this paper show a ‘bump’ towards redder colours between 1 and 2 Gyr, which is likely due to the development of the RGB. The exception appears to be the Maraston (2005) model. However, the latter shows a relatively pronounced effect of the AGB phase transition (starting at a few hundred Myr). Note the steep increase in the predicted colours, due to the increased flux in the near-IR passbands. This increased AGB contribution in the Maraston models may be a reason why the development of the RGB is not as visually prominent as in the other models.

Also note that the colours of the composite and the individual clusters in the youngest age bin are in much better agreement with the predictions of the Maraston (2005) models if age estimates from Girardi et al. are used (these are the ages which were available at the time). Our re-calibration of the  $S$ -parameter described in Appendix A shifts the ages in this interval to older values by 0.2 dex, introducing a slight discrepancy with the Maraston (2005) models, but in good agreement with the Bruzual & Charlot models. In other words, the models of Maraston seem to reflect our knowledge of the ages of MC clusters prior to 2005. Our study may be used to make appropriate updates to the models.

## 4 CONCLUDING REMARKS

We have presented new integrated  $JHK_s$  2MASS photometry for nine MC clusters, bringing our total sample (when combined with the results of Paper I) to 54 clusters with reliable ages  $\geq 200$  Myr. In addition, we compile integrated-light  $B$  and  $V$  photometric measurements, extinction estimates, and a data base of reliable age and metallicity determinations (mostly recent results) from the literature for our sample clusters. We divide the clusters into different age (e.g.  $\geq 10$  Gyr, 3–9 Gyr, 3–4 Gyr, 1–2 Gyr, and 200 Myr–1 Gyr) and metallicity (when possible), and quantify the observed spread in the intrinsic cluster colours in these ranges. Care was taken to account for the spread in the observational data around the model predictions due to the stochastic fluctuations in the stellar populations of the clusters. The smallest spread in intrinsic colours is found for clusters with ages  $\gtrsim 10$  Gyr, the colours of which are well reproduced by all four sets of SSP model predictions. The systematic shift between the model predictions and the observed colours for a sample of old Milky Way (MW) GCs reported by Cohen et al. (2007) is not observed in our MC cluster analysis. The largest spread in colour is found for clusters in the age range 2–4 Gyr. We believe that much of the spread in the colours for *individual* clusters younger than 10 Gyr results from stochastic fluctuations in the numbers of IR-luminous stars, since individual clusters tend to have less than  $\mathcal{M}_{(10 \text{ per cent})}$ <sup>6</sup> contributing to the observed colours.

Composite  $(B - J)_0$ ,  $(V - J)_0$ , and  $(J - K_s)_0$  cluster colours are calculated for each age–metallicity interval, and compared with the predictions of four widely used population synthesis models (Vazdekis 1999; Anders & Fritze-v. Alvensleben 2003; Bruzual & Charlot 2003; Maraston 2005), in order to evaluate their performance. We interpolate the model grids to calculate the offset or

<sup>6</sup> Stellar mass needed to decrease the luminosity uncertainty due to stochastic effects in the stellar population to 10 per cent.

distance in colour–colour space between the model predictions and the age and metallicity for our composite cluster colours. All four sets of models reproduce the colours of old ( $\geq 10$  Gyr) MC clusters quite well, with the Maraston (2005) and Bruzual & Charlot (2003) models giving slightly better fits than the other two.

In the age range of 2–10 Gyr, the Maraston (2005) models have the largest separation in optical–near-IR colour–colour space between the 2- and 10-Gyr model tracks, which best reproduces our observed composite colours in the 2–3 Gyr and 3–9 Gyr ranges. While the composite colour for 2–3 Gyr-old clusters falls just off the grid for the other three models, actual quantitative distances between the model predictions and composite cluster colours are not significantly different among the four models. In the 1–2 Gyr and 0.2–1 Gyr age ranges, the Bruzual & Charlot (2003) models generally give the best quantitative match to our composite MC cluster colours. Taking into account the inferred ages and metallicities, there is little difference between the Bruzual & Charlot (2003) and Maraston (2005) model performance. The cluster colours fall off the Anders & Fritze-v. Alvensleben (2003) and Vazdekis (1999) model predictions in the two youngest age ranges, largely due to their limited coverage at low metallicities.

Based on the comparisons presented in this work, it is found that each model has strong and weak points when used to analyse the optical+near-IR colours of unresolved stellar populations. There is no model set that clearly outperforms the others in all respects. Overall, the Bruzual & Charlot (2003) models typically yield the best quantitative match to our composite cluster colours. The Maraston (2005) models are a close second. The same two models also yield the best match to the composite cluster ages and metallicities.

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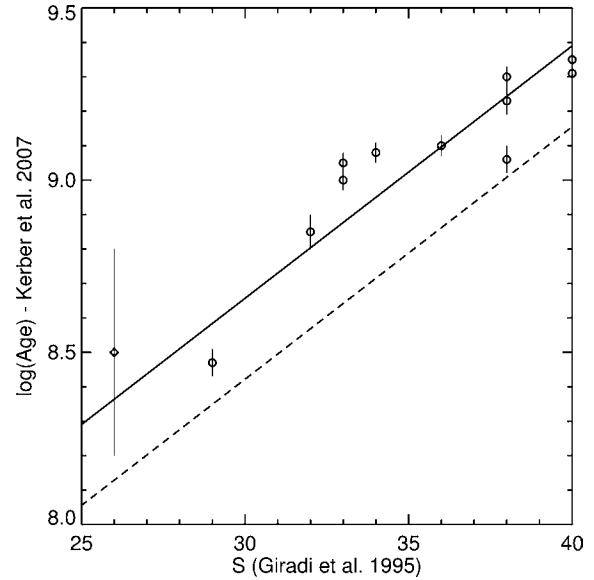
## APPENDIX A: S-PARAMETER-AGE RE-CALIBRATION

There are presently very few CMD-based ages for MC clusters in our youngest age bin (200 Myr–1 Gyr). One possible solution is to use the ‘*S*-parameter’ calibration for LMC clusters, which would allow us to select additional clusters for analysis in Section 3.4. The *S*-parameter, introduced by Elson & Fall (1985), provides an empirical relation between the age of a cluster and its integrated ( $U - B$ ) versus ( $B - V$ ) colours. Girardi et al. (1995) revised the *S*-parameter–age calibration based on 24 clusters which had age estimates from high-quality (*at the time*) ground-based CCD observations. They obtained the following relation between *S* and cluster age (in  $\log(\tau)$ ):

$$\log(\tau/[\text{yr}]) = (0.0733 \pm 0.0032) S + 6.227 \pm 0.096. \quad (\text{A1})$$

With an rms dispersion,  $\log(\tau) = 0.137$ .

We performed an independent analysis of the *S*-parameter using new age estimates for MC clusters derived from *HST*-based CMDs by Kerber et al. (2007). These include the age range for which we have few CMD-based ages ( $\sim 0.3$  Gyr to  $\sim 1$  Gyr). The optical colours from Table 4 were used to derive *S*-parameter values according to the definition given by Girardi et al. (1995). A comparison between the Kerber et al. and Girardi et al. age estimates for 12 clusters shows that there is an offset, such that the Kerber et al. ages are systematically older. The uncertainty-weighted mean offset of the Kerber et al. ages from the Girardi et al. calibration is 0.235 in



**Figure A1.** Ages from Kerber et al. (2007) and Chiosi & Vallenari (2007) as a function of the *S*-parameter. The dashed line represents the Girardi et al. (1995) calibration. NGC 265 (indicated with a diamond) was added to improve the sampling in the 200 Myr–1 Gyr age interval. The weighted mean offset of the data points with respect to the original relation is shown with a solid line.

**Table A1.** Ages and *S*-parameter values for the clusters from the Kerber et al. (2007) sample ( $25 \leq S \leq 40$ ).

Cluster ID (1)	<i>S</i> (2)	$\log(\tau)$ (3)	$\log(\tau)$ (4)	$\log(\tau)$ (5)
NGC 1651	38	$9.00 \pm 0.14$	$9.30 \pm 0.03$	$9.23 \pm 0.12$
NGC 1718	40	$9.15 \pm 0.14$	$9.31 \pm 0.03$	$9.38 \pm 0.12$
NGC 1777	38	$9.00 \pm 0.14$	$9.06 \pm 0.04$	$9.23 \pm 0.12$
NGC 1831	32	$8.56 \pm 0.14$	$8.85 \pm 0.05$	$8.79 \pm 0.12$
NGC 1856	30	$8.42 \pm 0.14$	$8.47 \pm 0.04$	$8.65 \pm 0.12$
NGC 1868	33	$8.64 \pm 0.14$	$9.05 \pm 0.03$	$8.87 \pm 0.12$
NGC 2162	37	$8.93 \pm 0.14$	$9.10 \pm 0.03$	$9.16 \pm 0.12$
NGC 2209	34	$8.71 \pm 0.14$	$9.08 \pm 0.03$	$8.94 \pm 0.12$
NGC 2213	38	$9.00 \pm 0.14$	$9.23 \pm 0.04$	$9.23 \pm 0.12$
NGC 2249	33	$8.64 \pm 0.14$	$9.00 \pm 0.03$	$8.87 \pm 0.12$
SL506	40	$9.15 \pm 0.14$	$9.35 \pm 0.03$	$9.38 \pm 0.12$
NGC 265	26	$8.13 \pm 0.14$	$8.5 \pm 0.3$	$8.36 \pm 0.12$

*Notes.* Column (1) is the cluster ID. The *S*-parameter value and the corresponding age according to Girardi et al. (1995) are listed in columns (2) and (3). Column (4) is  $\log(\tau)$  for the cluster from Kerber et al. (2007). The ages derived by our calibration are given in column (5).

**Table A2.** Extension of the sample based on the *S*-parameter.

ID (1)	<i>S</i> (2)	$\log(\tau)$ (3)	ID (1)	<i>S</i> (2)	$\log(\tau)$ (3)
NGC 1866	27	$8.43 \pm 0.12$	NGC 1644	37	$9.16 \pm 0.12$
NGC 2031	26	$8.36 \pm 0.12$	NGC 1783	37	$9.16 \pm 0.12$
NGC 2107	32	$8.79 \pm 0.12$	NGC 1987	35	$9.01 \pm 0.12$
NGC 2134	28	$8.50 \pm 0.12$	NGC 2108	36	$9.09 \pm 0.12$
NGC 2156	28	$8.50 \pm 0.12$	NGC 2154	38	$9.23 \pm 0.12$

*Notes.* Column (1) is the cluster ID. Column (2) lists the derived *S*-parameter values, along with the calculated ages in column (3).

$\log(\tau)$ . We confirmed that the difference between the age estimates is *not* caused by the adoption of different stellar isochrones (Bertelli et al. 1994 and Girardi et al. 2002, respectively, for studies of Girardi et al. and Kerber et al.), since they are indistinguishable from each other in the *B* and *V* bands which were used by Kerber et al. (2007). Kerber et al. have better data and apply a more robust technique for age determination; therefore, we re-calibrate the cluster ages with the appropriate offset:

$$\log(\tau/[\text{yr}]) = 0.0733 S + 6.458. \quad (\text{A2})$$

The standard deviation of Kerber et al. (2007) data around the new relation is  $\sigma = 0.123$ .

The objects selected to extend the sample based on the *S*-parameter values from equation (A2) are listed in Table A2.

## APPENDIX B: DEFINING THE TEST SAMPLE

In order to test the performance of SSP models, we need to define a reliable test sample: objects with age and metallicity measurements based on high-quality data, covering an appropriate parameter space. We prefer age and metallicity estimates based on CMDs, particularly those taken with *HST*, but also include metallicity estimates from individual stars, integrated spectroscopy and age estimates for the youngest age bins from the *S*-parameter (described in Appendix A). In order to clarify possible age-related effects in the SSP models performance, we decided to split the sample into several age bins: (i) GCs older than 10 Gyr; (ii) clusters with ages between 2 and 10 Gyr; (iii) clusters older than 1 Gyr and younger than 2 Gyr; and (iv) clusters with ages between 200 Myr and 1 Gyr. The latter two age bins are where the effects of AGB and RGB stars on the near-IR integrated-light properties are most-pronounced.

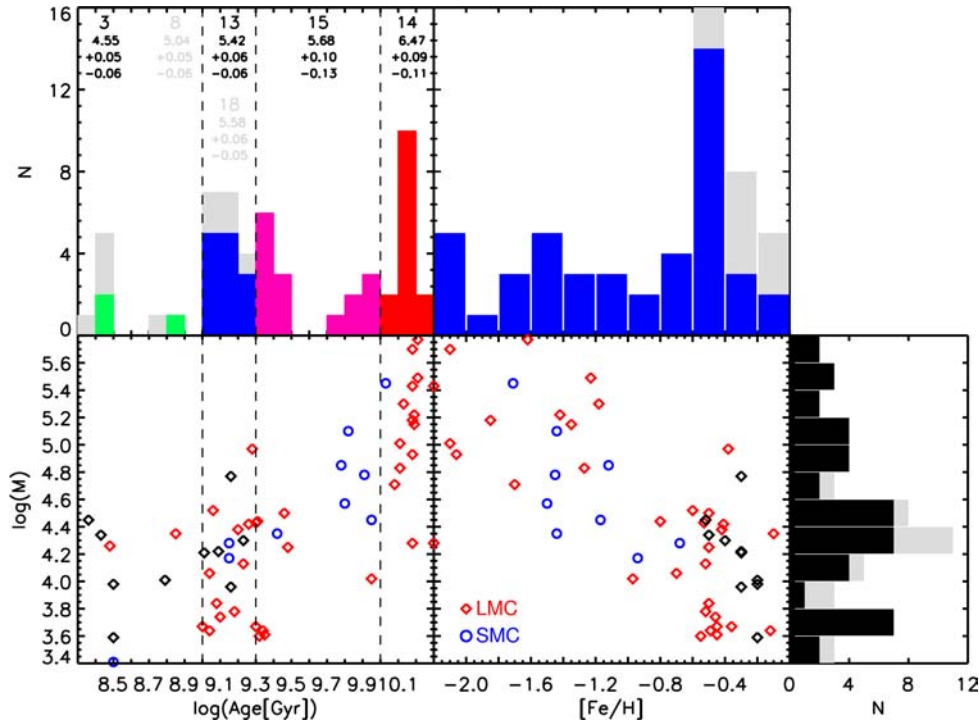
The intrinsic spread in integrated colours for clusters with a given age and metallicity increases with decreasing mass (Bruzual 2002),

due to stochastic fluctuations in the number of massive stars. Therefore, we consider clusters with masses exceeding  $\mathcal{M}_{(10 \text{ per cent})}$  to be reliable test particles. Since many clusters (particularly in the youngest age bins) have mass estimates lower than this value, we also present cumulative colours for each age bin, where the measured colours correspond to masses exceeding this limit.

### B1 The old cluster population (ages $\geq 10$ Gyr)

Olszewski, Suntzeff & Mateo (1996) listed 14 LMC clusters believed to be as old as the oldest Galactic globulars. More recent studies have established that ESO121-SC03 should be excluded from their original list, since it is somewhat younger at 8.3–9.8 Gyr (Mackey et al. 2006), given that the typical age of a Galactic GC exceeds 10 Gyr. On the other hand, the two ‘suspected’ old globulars, NGC 1928 and NGC 1939, were confirmed (see references below), giving a total of 15 ancient GCs in the LMC. NGC 121 is the only known old GC in the SMC (Mighell et al. 1998b). The adopted age and metallicity for each cluster, with associated references, are listed in Table B1. The table is supplemented with extinction information based on individual cluster CMDs and values retrieved from MCPS (Zaritsky et al. 1997). The estimated stellar mass which contributes to the integrated-light measurements for each cluster (based on our 2MASS *J*-band integrated-light photometry and *M/Ls* from Maraston 2005) are listed in column 7 of Table B2, and are lower than the total cluster masses. Total cluster mass estimates from McLaughlin & van der Marel (2005) are also given.

We believe that the following 10 old clusters are reliable test particles: four inner LMC objects (NGC 1786, NGC 1835, NGC 1898 and NGC 2019); one outer LMC cluster (NGC 2210), and NGC 121 in the SMC. The other three outer objects (NGC 1841, NGC 2257 and Hodge 11) have integrated-light measurements taken in apertures (set by the optical data set) which sample only a



**Table B1.** Information about the cluster test sample.

Cluster ID (1)	[Fe/H] (2)	age (3)	$E(B - V)$ (4)	$E(V - I)$ (5)	$A_{V(\text{CMD})}$ (6)	$A_{V(\text{MCPS})}$ (7)	Note (8)
Old GCs (ages $\geq 10$ Gyr)							
LMC							
NGC 1466	$-1.85 \pm 0.1$	(22)	$15 \pm 3$	(11)	$0.09 \pm 0.02$	(22)	$0.28 \pm 0.06$ 0.39 $\pm$ 0.02 O
NGC 1754	$-1.42 \pm 0.15$	(18)	$15.6 \pm 2.2$	(18)	$0.09 \pm 0.02$	(18)	$0.28 \pm 0.06$ 0.40 $\pm$ 0.04 I
NGC 1786	$-2.1 \pm 0.3$	(2)	$15 \pm 3$	(2)	$0.09 \pm 0.05$	(2)	$0.12 \pm 0.05$ (2) $0.28 \pm 0.16$ 0.62 $\pm$ 0.04 I
NGC 1835	$-1.62 \pm 0.15$	(18)	$16.2 \pm 2.8$	(18)	$0.08 \pm 0.02$	(18)	$0.25 \pm 0.06$ 0.35 $\pm$ 0.07 I
NGC 1841	$-2.2 \pm 0.2$	(2)	$15 \pm 3$	(2)	$0.20 \pm 0.03$	(2)	$0.28 \pm 0.03$ (2) $0.62 \pm 0.09$ 0.39 $\pm$ 0.02 O
NGC 1898	$-1.18 \pm 0.16$	(18)	$13.5 \pm 2.2$	(18)	$0.07 \pm 0.02$	(18)	$0.22 \pm 0.06$ 0.43 $\pm$ 0.05 I
NGC 1916							0.42 $\pm$ 0.05 I
NGC 1928	$-1.27 \pm 0.14$	(13)	GC $\pm$ 2	(13)		$0.08 \pm 0.02$ (13)	$0.20 \pm 0.05$ 0.43 $\pm$ 0.03 I
NGC 1939	$-2.10 \pm 0.19$	(13)	GC $\pm$ 2	(13)		$0.16 \pm 0.03$ (13)	$0.40 \pm 0.08$ 0.62 $\pm$ 0.05 I
NGC 2005	$-1.35 \pm 0.16$	(18)	$15.5 \pm 4.9$	(18)	$0.12 \pm 0.02$	(18)	$0.37 \pm 0.06$ 0.47 $\pm$ 0.04 I
NGC 2019	$-1.23 \pm 0.15$	(18)	$16.3 \pm 3.1$	(18)	$0.12 \pm 0.02$	(18)	$0.37 \pm 0.06$ 0.44 $\pm$ 0.06 I
NGC 2210	$-2.2 \pm 0.2$	(2)	$15 \pm 3$	(2)	$0.09 \pm 0.03$	(2)	$0.12 \pm 0.03$ (2) $0.28 \pm 0.09$ 0.39 $\pm$ 0.02 O
NGC 2257	$-1.7 \pm 0.2$	(21)	10 – 14	(21)	0.0	(21)	$0.00 \pm 0.00$ 0.39 $\pm$ 0.02 O
Hodge11	$-2.06 \pm 0.2$	(15)	$15 \pm 3$	(15)	$0.075 \pm 0.005$	(15)	$0.23 \pm 0.02$ 0.39 $\pm$ 0.02 O
Reticulum	$-1.66 \pm 0.12$	(13)	GC $\pm$ 2	(13)		$0.07 \pm 0.02$ (13)	$0.18 \pm 0.05$ 0.39 $\pm$ 0.02 O
SMC							
NGC 121	$-1.71 \pm 0.10$	(16)	$10.6 \pm 0.7$	(16)	$0.05 \pm 0.03$	(16)	$0.16 \pm 0.09$ 0.18 $\pm$ 0.01
Clusters with $2 \leq \text{age} < 10$ Gyr							
LMC							
NGC 1651	$-0.53 \pm 0.03$	(9)	$2.00 \pm 0.15$	(12)	$0.11 \pm 0.01$	(12)	$0.34 \pm 0.03$ 0.35 $\pm$ 0.05
NGC 1718	$-0.80 \pm 0.03$	(9)	$2.05 \pm 0.15$	(12)	$0.10 \pm 0.03$	(12)	$0.31 \pm 0.09$ 0.51 $\pm$ 0.06
NGC 2121	$-0.50 \pm 0.03$	(9)	$2.90 \pm 0.50$	(12)	$0.07 \pm 0.02$	(12)	$0.22 \pm 0.06$ 0.53 $\pm$ 0.04
NGC 2155	$-0.50 \pm 0.05$	(9)	$3.00 \pm 0.25$	(12)	$0.02 \pm 0.01$	(12)	$0.06 \pm 0.03$ 0.43 $\pm$ 0.04
NGC 2193	$-0.49 \pm 0.05$	(9)	$2.2 \pm 0.5$	(20)			0.39 $\pm$ 0.02
SL663	$-0.54 \pm 0.05$	(9)	$3.15 \pm 0.40$	(12)	$0.07 \pm 0.02$	(12)	$0.22 \pm 0.06$ 0.38 $\pm$ 0.04
SL842	$-0.36 \pm 0.20$	(19)	2.0	(8)			0.39 $\pm$ 0.02
Hodge4	$-0.55 \pm 0.06$	(9)	$2.1 \pm 0.3$	(23)			0.39 $\pm$ 0.02
Hodge14	$-0.45 \pm 0.10$	(12)	$2.25 \pm 0.15$	(12)	$0.08 \pm 0.02$	(12)	$0.25 \pm 0.06$ 0.39 $\pm$ 0.02
ESO121–03	$-0.97 \pm 0.10$	(12)	8.3 – 9.8	(12)		$0.04 \pm 0.02$ (13)	$0.10 \pm 0.05$ 0.39 $\pm$ 0.02
SMC							
NGC 339	$-1.50 \pm 0.14$	(16)	$6.3 \pm 1.3$	(16)	$0.03 \pm 0.04$	(16)	$0.09 \pm 0.12$ 0.18 $\pm$ 0.01
NGC 361	$-1.45 \pm 0.11$	(16)	$8.1 \pm 1.2$	(16)	$0.07 \pm 0.03$	(16)	$0.22 \pm 0.09$ 0.17 $\pm$ 0.02
NGC 416	$-1.44 \pm 0.12$	(15)	$6.6 \pm 0.5$	(15)	$0.08 \pm 0.03$	(15)	$0.25 \pm 0.09$ 0.20 $\pm$ 0.02
Kron3	$-1.12 \pm 0.12$	(6)	$6.0 \pm 1.3$	(16)	$-0.03 \pm 0.02$	(16)	$0.00 \pm 0.06$ 0.18 $\pm$ 0.01
Lindsay1	$-1.17 \pm 0.10$	(6)	$9.0 \pm 1.0$	(16)	$0.06 \pm 0.02$	(16)	$0.19 \pm 0.06$ 0.18 $\pm$ 0.01
Lindsay113	$-1.44 \pm 0.16$	(6)	$5.3 \pm 1.3$	(16)	$0.00 \pm 0.02$	(16)	$0.00 \pm 0.06$ 0.18 $\pm$ 0.01
Clusters with $1 \leq \text{age} < 2$ Gyr							
LMC							
NGC 1644	-0.3	(*)	$1.45^{+0.46}_{-0.35}$	(*)			0.39 $\pm$ 0.02
NGC 1777	$-0.60 \pm 0.10$	(12)	$1.15 \pm 0.15$	(12)	$0.10 \pm 0.03$	(12)	$0.31 \pm 0.09$ 0.39 $\pm$ 0.02
NGC 1783	-0.3	(*)	$1.45^{+0.46}_{-0.35}$	(*)			0.30 $\pm$ 0.03
NGC 1868	$-0.70 \pm 0.10$	(12)	$1.10 \pm 0.10$	(12)	$0.04 \pm 0.01$	(12)	$0.12 \pm 0.03$ 0.39 $\pm$ 0.02
NGC 1978	$-0.38 \pm 0.07$	(7)	$1.9 \pm 0.1$	(17)			0.76 $\pm$ 0.05
NGC 1987	-0.3	(*)	$1.02^{+0.33}_{-0.23}$	(*)			0.28 $\pm$ 0.03
NGC 2108	-0.3	(*)	$1.23^{+0.39}_{-0.30}$	(*)			0.50 $\pm$ 0.05
NGC 2154	-0.4	(*)	$1.70^{+0.54}_{-0.41}$	(*)			0.39 $\pm$ 0.03
NGC 2162	$-0.46 \pm 0.07$	(9)	$1.25 \pm 0.10$	(12)	$0.03 \pm 0.02$	(12)	$0.09 \pm 0.06$ 0.39 $\pm$ 0.02
NGC 2173	$-0.42 \pm 0.03$	(9)	$1.60 \pm 0.20$	(12)	$0.07 \pm 0.02$	(12)	$0.22 \pm 0.06$ 0.39 $\pm$ 0.02

**Table B1** – *continued*

Cluster ID (1)	[Fe/H] (2)	age (3)	$E(B - V)$ (4)	$E(V - I)$ (5)	$A_V(\text{CMD})$ (6)	$A_V(\text{MCPS})$ (7)	Note (8)
Clusters with $1 \leq \text{age} < 2$ Gyr							
LMC							
NGC 2190	$-0.12 \pm 0.20$	(19)	1.1	(8)		$0.39 \pm 0.02$	
NGC 2203	$-0.41 \pm 0.03$	(9)	1.8	(8)		$0.39 \pm 0.02$	
NGC 2209	$-0.50 \pm 0.10$	(12)	$1.20 \pm 0.10$	(12)	$0.15 \pm 0.03$	$0.47 \pm 0.09$	$0.39 \pm 0.02$
NGC 2213	$-0.52 \pm 0.04$	(9)	$1.70 \pm 0.20$	(12)	$0.06 \pm 0.03$	$0.19 \pm 0.09$	$0.40 \pm 0.04$
NGC 2231	$-0.52 \pm 0.04$	(9)	1.5	(8)			$0.39 \pm 0.02$
NGC 2249	$-0.45 \pm 0.10$	(12)	$1.00 \pm 0.10$	(12)	$0.01 \pm 0.02$	$0.03 \pm 0.06$	$0.39 \pm 0.02$
SMC							
NGC 152	$-0.94 \pm 0.15$	(4)	$1.4 \pm 0.2$	(4)	$0.05 \pm 0.01$	$0.16 \pm 0.03$	$0.19 \pm 0.02$
NGC 411	$-0.68 \pm 0.07$	(1)	$1.4 \pm 0.2$	(1)	$0.12 \pm 0.01$	$0.37 \pm 0.03$	$0.17 \pm 0.02$
Clusters with $0.2 \leq \text{age} < 1$ Gyr							
LMC							
NGC 1831	$-0.10 \pm 0.10$	(12)	$0.71^{+0.09}_{-0.08}$	(12)	$0.11 \pm 0.01$	$0.34 \pm 0.03$	$0.39 \pm 0.02$
NGC 1856	$-0.40 \pm 0.10$	(12)	$0.30 \pm 0.03$	(12)	$0.21 \pm 0.02$	$0.65 \pm 0.06$	$0.22 \pm 0.03$
NGC 1866	$-0.50 \pm 0.10$	(10)	$0.33^{+0.09}_{-0.07}$	(*)			$0.28 \pm 0.06$
NGC 2031	$-0.52 \pm 0.21$	(5)	$0.23^{+0.07}_{-0.06}$	(*)			$0.40 \pm 0.03$
NGC 2107	$-0.2$	(*)	$0.62^{+0.19}_{-0.15}$	(*)			$0.36 \pm 0.04$
NGC 2134	$-0.2$	(*)	$0.32^{+0.10}_{-0.08}$	(*)			$0.62 \pm 0.03$
NGC 2156	$-0.2$	(*)	$0.32^{+0.10}_{-0.08}$	(*)			$0.20 \pm 0.02$
SMC							
NGC 265	$-0.62^{+0.23}_{-0.61}$	(3)	$0.32^{+0.32}_{-0.16}$	(3)	$0.06^{+0.05}_{-0.04}$	$0.19^{+0.15}_{-0.13}$	$0.34 \pm 0.02$

*Notes.* Column (1): cluster designation. Columns (2) and (3): metallicity and the age of the cluster with corresponding references given in parenthesis. Reddening information based on CMDs plus corresponding references is listed in columns (4), (5) and (6).  $A_V$  retrieved from MCPS data base is presented in column (7). Finally, notes are given in column (8).

In column (8), I and O stand for the positions of the objects in the LMC. ‘I’ means inner (bar) and ‘O’ means outer clusters. There are slight variations in this classification from author to author. Here, we classify the objects as in Mackey & Gilmore (2004).

Mackey & Gilmore (2004) concluded that NGC 1928, NGC 1939 and Reticulum are coeval in age with the oldest MW GCs within 2 Gyr. In this table, this result is denoted by ‘GC  $\pm 2$ ’.

ESO121–SC03 is the only object in the LMC age–metallicity gap. It is younger than the genuine old GCs, but significantly older than the intermediate-age massive clusters from this galaxy. It will be compared with the model predictions alongside the objects from the next age bin.

*References.* (1) Alves & Sarajedini (1999); (2) Brocato et al. (1996); (3) Chiosi & Vallenari (2007); (4) Crowl et al. (2001); (5) Dirsch et al. (2000); (6) Da Costa & Hatzidimitriou (1998); (7) Ferraro et al. (2006); (8) Geisler et al. (1997); (9) Grocholski et al. (2006); (10) Hill et al. (2000); (11) Johnson et al. (1999); (12) Kerber et al. (2007); (13) Mackey & Gilmore (2004); (14) Mackey, Payne & Gilmore (2006); (15) Mighell et al. (1996); (16) Mighell et al. (1998b); (17) Mucciarelli et al. (2007); (18) Olsen et al. (1998); (19) Olszewski et al. (1991); (20) Rich, Shara & Zurek (2001); (21) Testa et al. (1995); (22) Walker (1992); (23) Woo et al. (2003).

fraction of the total stellar population in each cluster. The stellar masses which contribute to the integrated-light measurements are lower than  $\mathcal{M}_{(10\text{ percent})}$ , and therefore these clusters may have a larger spread in colour–colour space.

Here, we provide more details on the available cluster age and metallicity information. Olsen et al. (1998) studied NGC 1754, NGC 1835, NGC 1898, NGC 1916, NGC 2005 and NGC 2019. Their  $F555W$  and  $F814W$  WFC2 CMDs reach an apparent magnitude  $V \approx 25$ , well below the MSTO point. The metallicities were derived using the technique of (Sarajedini 1994, hereafter S94). In most cases, there is good agreement between the photometric results of Olsen et al. (1998) and the spectroscopy of individual cluster members of Olszewski et al. (1991). For the clusters showing large discrepancies (NGC 2005 and NGC 2019), the metallicities in Olszewski et al. are significantly lower, although Olszewski et al. do note that the measurements for these clusters are uncertain. Grocholski et al. (2006) recently estimated  $[\text{Fe}/\text{H}] = -1.31 \pm 0.05$  for NGC 2019 based on moderate-resolution Ca II triplet spectroscopy of five cluster stars, in good agreement with the

result of Olsen et al. ( $[\text{Fe}/\text{H}] = -1.23 \pm 0.15$ ). Age estimates relative to those of MW GCs with similar metallicity were measured according to the method of Vandenberg, Bolte & Stetson (1990).

Another three old LMC clusters (NGC 1466, NGC 2257, and Hodge11) were observed with WFC2  $F555W$  and  $F814W$  filters by Johnson et al. (1999). In this case, the authors did not attempt to derive their own metallicity estimates, but adopted already published values instead.

Mackey & Gilmore (2004) published ACS Wide Field Channel (WFC)  $F555W$  and  $F814W$  photometry for NGC 1928 and NGC 1939 (clusters located in the LMC bar region), and for the remote outer cluster Reticulum. Employing the S94 method, Mackey & Gilmore derived metallicities that are consistent with earlier measurements. Grocholski et al. (2006) also published  $[\text{Fe}/\text{H}] = -1.57 \pm 0.03$  for Reticulum, which is in very good agreement with  $[\text{Fe}/\text{H}] = -1.66 \pm 0.12$  given by Mackey & Gilmore. The relative ages of the three clusters with respect to MW clusters with a similar metallicity were derived using the techniques of Vandenberg et al. (1990).

**Table B2.** 2MASS integrated-light photometry and mass estimates.

Cluster ID (1)	<i>D</i> (2)	<i>J</i> (3)	<i>H</i> (4)	<i>K<sub>S</sub></i> (5)	$\log(m)_{\text{near-IR}}$ (6)	$\log(m)_{\text{Lit}}$ (7)
Old GCs (ages $\geq 10$ Gyr)						
LMC						
NGC 1466	60	$9.83 \pm 0.02$	$9.39 \pm 0.01$	$9.30 \pm 0.01$	$5.18 \pm 0.07$	$5.24 \pm 0.04$
NGC 1754	100	$9.74 \pm 0.06$	$9.24 \pm 0.04$	$9.08 \pm 0.05$	$5.22^{+0.06}_{-0.08}$	$5.07 \pm 0.05$
NGC 1786	60	$8.57 \pm 0.01$	$8.09 \pm 0.01$	$8.00 \pm 0.01$	$5.70^{+0.14}_{-0.22}$	$5.57 \pm 0.05$
NGC 1835	60	$8.34 \pm 0.01$	$7.82 \pm 0.01$	$7.71 \pm 0.01$	$5.77 \pm 0.08$	$5.71 \pm 0.05$
NGC 1841	25	$12.23 \pm 0.02$	$11.69 \pm 0.02$	$11.48 \pm 0.02$	$4.28^{+0.05}_{-0.06}$	$5.31^{+0.07}_{-0.06}$
NGC 1898	62	$9.52 \pm 0.02$	$9.18 \pm 0.03$	$9.00 \pm 0.03$	$5.30^{+0.08}_{-0.09}$	$5.35 \pm 0.06$
NGC 1916	44	$8.36 \pm 0.01$	$7.91 \pm 0.01$	$7.68 \pm 0.01$	$5.79^{+0.04}_{-0.05}$	$5.77 \pm 0.05$
NGC 1928	62	$10.71 \pm 0.09$	$10.27 \pm 0.12$	$10.20 \pm 0.15$	$4.83^{+0.07}_{-0.09}$	
NGC 1939	38	$10.34 \pm 0.02$	$9.89 \pm 0.02$	$9.83 \pm 0.02$	$5.01^{+0.06}_{-0.07}$	
NGC 2005	25	$9.93 \pm 0.01$	$9.39 \pm 0.01$	$9.27 \pm 0.01$	$5.15 \pm 0.06$	$5.27 \pm 0.05$
NGC 2019	60	$9.10 \pm 0.02$	$8.65 \pm 0.02$	$8.54 \pm 0.02$	$5.49^{+0.05}_{-0.07}$	$5.47 \pm 0.05$
NGC 2210	62	$9.25 \pm 0.01$	$8.72 \pm 0.01$	$8.66 \pm 0.01$	$5.43^{+0.09}_{-0.11}$	$5.40 \pm 0.05$
NGC 2257	61	$10.98 \pm 0.02$	$10.60 \pm 0.03$	$10.50 \pm 0.03$	$4.71^{+0.03}_{-0.04}$	$5.00^{+0.12}_{-0.07}$
Hodge11	62	$10.48 \pm 0.02$	$9.88 \pm 0.02$	$9.86 \pm 0.02$	$4.93 \pm 0.03$	$5.17^{+0.07}_{-0.06}$
SMC						
NGC 121	62	$9.52 \pm 0.01$	$8.90 \pm 0.01$	$8.81 \pm 0.01$	$5.45^{+0.15}_{-0.21}$	$5.57 \pm 0.04$
Clusters with $2 \leq \text{age} < 10$ Gyr						
LMC						
NGC 1651	100	$10.00 \pm 0.02$	$9.23 \pm 0.02$	$9.10 \pm 0.02$	$4.43 \pm 0.04$	$4.53^{+0.11}_{-0.09}$
NGC 1718	62	$10.01 \pm 0.01$	$9.13 \pm 0.01$	$8.94 \pm 0.01$	$4.44^{+0.08}_{-0.10}$	$4.57 \pm 0.22$
NGC 2121	62	$10.40 \pm 0.03$	$9.73 \pm 0.03$	$9.20 \pm 0.02$	$4.50^{+0.08}_{-0.10}$	$5.00^{+0.08}_{-0.07}$
NGC 2155	62	$10.98 \pm 0.02$	$10.31 \pm 0.11$	$10.37 \pm 0.03$	$4.25^{+0.13}_{-0.18}$	$4.56^{+0.09}_{-0.08}$
NGC 2193	38	$12.01 \pm 0.05$	$11.36 \pm 0.04$	$11.27 \pm 0.04$	$3.64^{+0.03}_{-0.04}$	$4.13 \pm 0.08$
SL663*	60	$11.22 \pm 0.02$	$11.08 \pm 0.04$	$11.02 \pm 0.04$	$4.18^{+0.08}_{-0.10}$	$4.67^{+2.49}_{-0.45}$
SL842	38	$11.89 \pm 0.07$	$11.14 \pm 0.05$	$10.86 \pm 0.05$	$3.67^{+0.03}_{-0.04}$	$3.91 \pm 0.10$
Hodge4	38	$12.10 \pm 0.02$	$11.78 \pm 0.06$	$11.44 \pm 0.05$	$3.66^{+0.03}_{-0.04}$	$5.31^{+1.91}_{-0.45}$
Hodge14	62	$12.05 \pm 0.03$	$11.37 \pm 0.03$	$11.47 \pm 0.04$	$3.61^{+0.07}_{-0.08}$	$4.00 \pm 0.09$
ESO121-03	61	$12.34 \pm 0.09$	$11.59 \pm 0.07$	$11.70 \pm 0.08$	$4.02^{+0.14}_{-0.18}$	
SMC						
NGC 339	62	$11.06 \pm 0.02$	$10.70 \pm 0.02$	$10.43 \pm 0.02$	$4.57^{+0.28}_{-0.99}$	$4.90 \pm 0.07$
NGC 361	62	$10.76 \pm 0.02$	$9.97 \pm 0.01$	$9.83 \pm 0.02$	$4.78^{+0.11}_{-0.15}$	$5.30^{+0.10}_{-0.08}$
NGC 416	62	$9.77 \pm 0.01$	$9.16 \pm 0.01$	$9.08 \pm 0.01$	$5.10^{+0.10}_{-0.13}$	$5.21 \pm 0.05$
Kron3	62	$10.31 \pm 0.01$	$9.69 \pm 0.01$	$9.68 \pm 0.01$	$4.85 \pm 0.03$	$5.15 \pm 0.06$
Lindsay1	62	$11.64 \pm 0.03$	$11.26 \pm 0.03$	$11.14 \pm 0.04$	$4.45^{+0.09}_{-0.11}$	
Lindsay113	62	$11.46 \pm 0.02$	$10.49 \pm 0.01$	$10.32 \pm 0.01$	$4.35 \pm 0.03$	
Clusters with $1 \leq \text{age} < 2$ Gyr						
LMC						
NGC 1644	60	$11.31 \pm 0.11$	$10.88 \pm 0.10$	$10.76 \pm 0.10$	$3.96^{+0.03}_{-0.04}$	
NGC 1777	38	$9.06 \pm 0.01$	$8.59 \pm 0.01$	$8.46 \pm 0.01$	$4.52^{+0.08}_{-0.10}$	$4.28 \pm 0.11$
NGC 1783	60	$9.23 \pm 0.01$	$8.62 \pm 0.01$	$8.52 \pm 0.01$	$4.77^{+0.04}_{-0.05}$	
NGC 1868	62	$10.19 \pm 0.01$	$9.71 \pm 0.01$	$9.56 \pm 0.01$	$4.10^{+0.07}_{-0.09}$	$4.33 \pm 0.18$
NGC 1978	60	$8.74 \pm 0.02$	$8.04 \pm 0.01$	$7.81 \pm 0.02$	$4.97 \pm 0.04$	
NGC 1987	60	$10.16 \pm 0.02$	$9.48 \pm 0.01$	$9.04 \pm 0.01$	$4.21^{+0.04}_{-0.05}$	
NGC 2108	62	$10.46 \pm 0.02$	$9.70 \pm 0.02$	$9.25 \pm 0.02$	$4.22^{+0.04}_{-0.05}$	
NGC 2154	62	$10.14 \pm 0.02$	$9.36 \pm 0.01$	$8.90 \pm 0.01$	$4.30 \pm 0.04$	
NGC 2162	62	$10.89 \pm 0.04$	$10.21 \pm 0.03$	$10.01 \pm 0.03$	$3.74^{+0.16}_{-0.26}$	$4.02 \pm 0.15$
NGC 2173	150	$9.76 \pm 0.10$	$9.10 \pm 0.07$	$8.91 \pm 0.07$	$4.38^{+0.07}_{-0.09}$	$4.70 \pm 0.07$

**Table B2** – *continued*

Cluster ID (1)	D (2)	<i>J</i> (3)	<i>H</i> (4)	<i>K<sub>S</sub></i> (5)	$\log (m)_{\text{near-IR}}$ (6)	$\log (m)_{\text{Lit}}$ (7)
Clusters with $1 \leq \text{age} < 2$ Gyr						
LMC						
NGC 2190	61	$11.42 \pm 0.04$	$10.79 \pm 0.04$	$10.57 \pm 0.04$	$3.64^{+0.03}_{-0.04}$	
NGC 2203	150	$9.28 \pm 0.07$	$8.61 \pm 0.05$	$8.40 \pm 0.05$	$4.42^{+0.03}_{-0.04}$	
NGC 2209	62	$10.77 \pm 0.04$	$9.90 \pm 0.04$	$9.38 \pm 0.03$	$3.84^{+0.06}_{-0.07}$	$4.36^{+2.59}_{-0.31}$
NGC 2213	62	$10.40 \pm 0.02$	$9.55 \pm 0.01$	$9.25 \pm 0.01$	$4.13^{+0.12}_{-0.17}$	$4.30 \pm 0.10$
NGC 2231	44	$11.33 \pm 0.08$	$10.51 \pm 0.05$	$10.19 \pm 0.04$	$3.78^{+0.03}_{-0.04}$	$4.36 \pm 0.12$
NGC 2249	36	$11.06 \pm 0.05$	$10.57 \pm 0.05$	$10.25 \pm 0.04$	$3.67^{+0.37}_{-0.04}$	$4.03 \pm 0.20$
SMC						
NGC 152	62	$10.78 \pm 0.02$	$9.95 \pm 0.01$	$9.62 \pm 0.01$	$4.17^{+0.06}_{-0.07}$	$4.56 \pm 0.09$
NGC 411	62	$10.49 \pm 0.03$	$9.84 \pm 0.03$	$9.61 \pm 0.03$	$4.28 \pm 0.04$	$4.47 \pm 0.10$
Clusters with $0.2 \leq \text{age} < 1$ Gyr						
LMC						
NGC 1831	60	$9.86 \pm 0.01$	$9.34 \pm 0.01$	$9.15 \pm 0.01$	$4.16 \pm 0.04$	$4.59 \pm 0.18$
NGC 1856	60	$8.98 \pm 0.02$	$8.59 \pm 0.02$	$8.44 \pm 0.02$	$4.26 \pm 0.04$	$4.88 \pm 0.12$
NGC 1866	60	$8.72 \pm 0.01$	$8.28 \pm 0.01$	$8.11 \pm 0.01$	$4.34^{+0.07}_{-0.08}$	$4.91 \pm 0.12$
NGC 2031	72	$8.95 \pm 0.03$	$8.28 \pm 0.03$	$8.16 \pm 0.04$	$4.45 \pm 0.04$	$4.48^{+0.06}_{-0.05}$
NGC 2107	60	$10.05 \pm 0.13$	$9.43 \pm 0.08$	$9.20 \pm 0.11$	$4.01^{+0.04}_{-0.05}$	
NGC 2134	60	$9.94 \pm 0.03$	$9.50 \pm 0.02$	$9.43 \pm 0.02$	$3.98^{+0.03}_{-0.04}$	
NGC 2156	72	$10.81 \pm 0.17$	$10.43 \pm 0.22$	$10.43 \pm 0.26$	$3.59^{+0.04}_{-0.05}$	$3.65 \pm 0.08$
SMC						
NGC 265	62	$10.90 \pm 0.13$	$9.88 \pm 0.09$	$9.76 \pm 0.12$	$3.41^{+0.18}_{-0.30}$	

*Notes.* Column (1): the cluster identification. Column (2): the diameter of the used aperture (to match the optical photometry). *J*, *H* and *K<sub>S</sub>* integrated magnitudes with corresponding errors are listed in columns (3)–(5). Column (6) presents an estimate of the stellar mass which contributes to the measured integrated colours. These are typically lower than the total cluster mass. The mass estimates are based on the cluster age, metallicity, observed *J*-band magnitude, and the model predictions of Maraston (2005). Column (7) lists the total mass estimates of the objects in common between this study and McLaughlin & van der Marel (2005).

\*No integrated-light optical photometry was recovered from the literature for SL663. Near-IR measurements are presented for aperture diameter of 60 arcsec.

## B2 Clusters in the $2 \leq \text{age} < 10$ Gyr interval

A survey of the literature revealed 15 SMC/LMC clusters in this age range. Their ages and metallicities alongside the corresponding references are listed in Table B1. Most of the LMC cluster metallicity estimates come from Grocholski et al. (2006). Their results are based on CaT spectroscopy of multiple stars in each cluster and generally are in a good agreement with earlier studies (e.g. Olszewski et al. 1991). Cluster metallicities based on spectroscopic measurements also agree with the CMD-based metallicity estimates of Kerber et al. (2007). The latter work is the source of the age and extinction estimates for the majority of the LMC objects.

All six of the SMC clusters included in the 2–10 Gyr bin fall within the age range between 5–8 Gyr; no LMC clusters with these ages are known. Most of the information about these SMC clusters was retrieved from the papers of Mighell, Sarajedini & French (1998a) and Mighell et al. (1998b), based on deep *HST* WFPC2 observations. Metallicities and reddening for the objects were derived applying the S94 method. The age estimates listed in Table B1 are by assuming an age of 9.0 Gyr for Lindsay I. Independent estimates of Alcaíno, Alvarado & Kurtev (2003) confirm this value. Spectroscopic metallicities for three SMC clusters were recovered from Da Costa & Hatzidimitriou (1998).

Integrated-light near-IR photometry and mass estimates for the ( $2 \leq \text{age} < 10$  Gyr) subsample are presented in Table B2. We should note that the masses of the LMC objects are of the order of  $10^4 \mathcal{M}_{\odot}$ ;

therefore, a relatively large spread relative to the model predictions is not unexpected. Only NGC 416 has an estimated mass  $> 10^5 \mathcal{M}_{\odot}$ .

## B3 Clusters in the $1 \leq \text{age} < 2$ Gyr interval

As in the previous section, the bulk of the LMC cluster properties in this age range come from Grocholski et al. (2006) and Kerber et al. (2007). The adopted values are presented in Table B1. Occasionally, we supplement age information from Geisler et al. (1997) and metallicity information from Olszewski et al. (1991). The clusters in this age range have sampled stellar masses around  $10^4 \mathcal{M}_{\odot}$ , and again some spread is expected in the individual data points. Only NGC 1978 is close to  $10^5 \mathcal{M}_{\odot}$ .

Some details on individual clusters in this age interval are provided below. Ferraro et al. (2006) showed that despite its large observed ellipticity and suspected metallicity spread (Alcaíno et al. 1999; Hill et al. 2000), NGC 1978 is not the product of merged clusters. They derived metallicities for 11 giant stars cluster in NGC 1978 from high-resolution UVES/FLAMES VLT spectroscopy. No significant variations in the giant's metal abundance were found (resulting mean  $[\text{Fe}/\text{H}]$  is listed in Table B1). We conclude that NGC 1978 can be used as a test particle in our analysis. The age of this object was derived by Mucciarelli et al. (2007) applying fit of theoretical isochrones to *HST*/ACS data. Information for the two SMC objects is retrieved from the works of Alves &



Sarajedini (1999) and Crowl et al. (2001). Five additional objects were added using the calibration presented in Appendix A.

#### B4 Clusters in the 200 Myr $\leq$ age < 1 Gyr interval

Based on a search of the literature, we only identified three clusters in the 200 Myr–1 Gyr age range, with age estimates based on deep CMDs. In order to expand our test sample, we use the  $S$ -parameter re-calibration from Appendix A information. Based on equation (A2), five more clusters were added to this age bin. The properties of the sample are also summarized in Table B1.

There are age and metallicity estimates for some of the objects from this subsample available in the literature. Dirsch et al. (2000) presented data for six LMC clusters based on CCD Strömberg photometry. We adopt their metallicity estimate for NGC 2031.

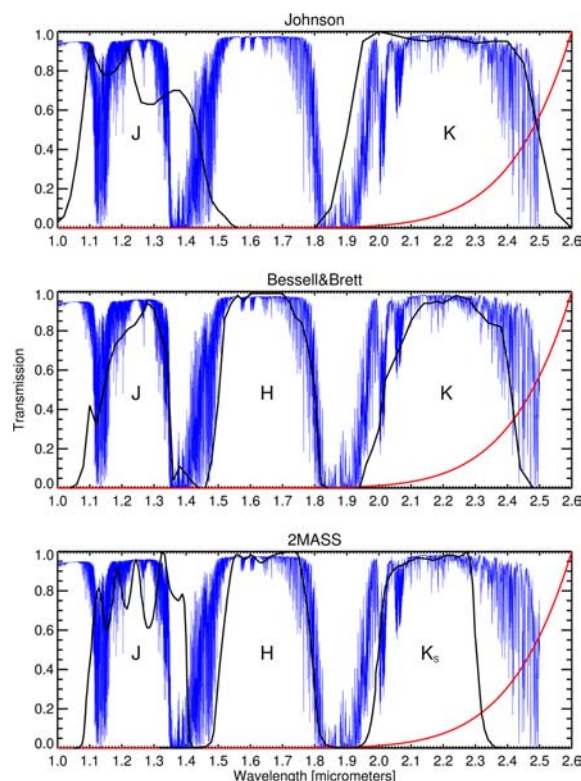
Information for several more clusters in the 200 Myr–1 Gyr age interval is available in the recent study of Wolf et al. (2007). The authors use Bruzual–Charlot high-resolution stellar population synthesis models to fit the SEDs and simultaneously estimate ages and metallicities of GCs in the MCs and M31. Their age results are in a good agreement with our  $S$ -parameter ages.

### APPENDIX C: TRANSFORMATION OF MODEL COLOURS TO THE 2MASS SYSTEM

Today’s SSP model predictions for near-IR colours are provided in various photometric systems. In order to avoid systematic offsets, observations and model predictions should be compared in the same photometric system.

Johnson (1965) defined a photometric system, in both the optical and near-IR, which is presently perhaps the most widely used. Unfortunately, however, the near-IR passbands of Johnson are broader than the atmospheric transmission windows. This can lead to substantial variations in sky background levels (which can also vary on short time-scales). Hence, there can be significant differences between observations conducted in the original Johnson (1965) filter set and more recent near-IR systems, which have been developed to fit within the atmospheric windows and to decrease the thermal background at longer wavelengths ( $K$  band).

Bessell & Brett (1988) examined the relations between the near-IR photometric systems of several different observatories and introduced a homogenized near-IR system based on the works of Glass (1985) and Johnson (1966). The filter transmission curves of the Johnson (1965) and the Bessell & Brett (1988) systems are shown in the top and middle panels of Fig. C1. In the bottom panel, we plot the 2MASS filter system (Skrutskie et al. 2006). The estimated mean atmospheric transmission for CTIO taken from the online 2MASS



**Figure C1.** Filter transmission curves of the Johnson (1965), Bessell & Brett (1988) and 2MASS photometric systems. The atmospheric transmission for the south 2MASS facility (CTIO) is plotted in blue. Red represents the thermal emission of the atmosphere at 20°C (scaled to reach unity at 2.6  $\mu$ m for illustration purposes). It is obvious that the ‘ $K$ -short’ ( $K_s$ ) filter significantly reduces the influence of the thermal background compared to the Johnson and Bessell & Brett systems. The 2MASS  $J$  is broader than the atmospheric window, and the transmission variability was accounted for during the extensive calibration observations. The  $H$  filter was introduced to the Johnson (1965) system somewhat later (Johnson, MacArthur & Mitchell 1968) and the transmission curve was never published. The near-IR colours for the majority of the SSP models use the filter transmissions of Bessell & Brett (1988).

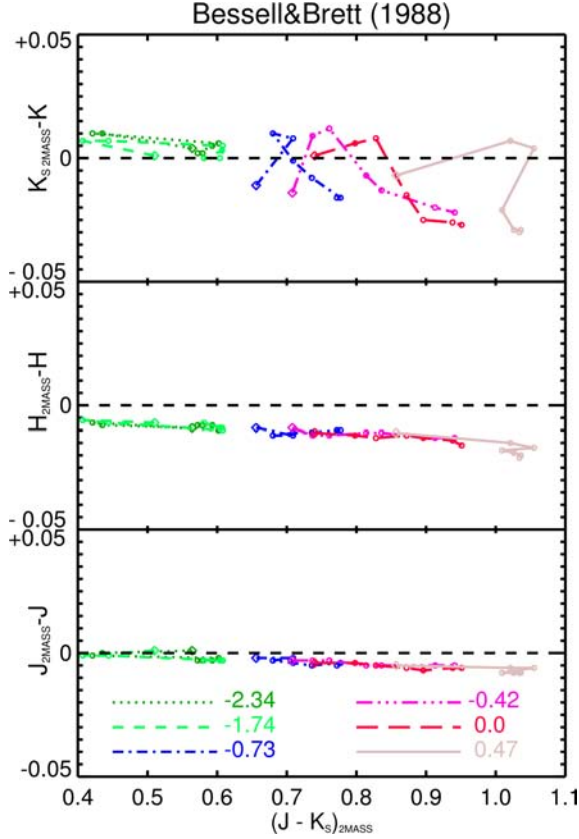
All-sky Release Explanatory Supplement<sup>7</sup> and the thermal emission of Earth’s atmosphere (blackbody with a temperature of 20°C) are overplotted in blue and red. Differences between the systems are clearly visible. The 2MASS photometric system by Skrutskie et al. appears to be least affected by the Earth’s atmosphere and by the thermal background. It is also clear that observations in these different systems will result in different near-IR colours.

The 2MASS system seems to be a natural choice, given the extensive sky coverage and the precise internal photometric calibration. Among the SSP models being considered here, only Bruzual & Charlot (2003) provide 2MASS near-IR colours. The other models use near-IR passbands on the Bessell & Brett photometric system, although they are sometimes referred to as Johnson  $JHK$  passbands. However, it is clear that the system of Bessell & Brett (1988) has different filter throughput from Johnson (as illustrated in Fig. C1). Given the advantages of the 2MASS photometric system, we encourage the SSP model builders to provide output in the 2MASS

**Table C1.** Transformation coefficients between 2MASS and Bessell & Brett systems for equations (C1)–(C3).

[Fe/H]	$a_J$	$b_J$	$a_H$	$b_H$	$a_{K_s}$	$b_{K_s}$
−2.34	−0.011	0.005	−0.008	−0.004	−0.037	0.026
−1.74	−0.014	0.006	−0.015	0.000	−0.023	0.016
−0.73	−0.023	0.012	−0.003	−0.009	−0.100	0.067
−0.42	−0.011	0.005	−0.014	−0.001	−0.098	0.072
0.0	−0.014	0.007	−0.022	0.006	−0.198	0.158
0.47	−0.008	0.001	−0.033	0.017	0.015	−0.029

<sup>7</sup> [http://www.ipac.caltech.edu/2mass/releases/allsky/doc/sec3\\_1b1.tbl16.html](http://www.ipac.caltech.edu/2mass/releases/allsky/doc/sec3_1b1.tbl16.html)



**Figure C2.** The differences between 2MASS and Bessell & Brett (1988) near-IR magnitudes as a function of  $(J - K_S)_{2MASS}$ . The dependence of the age and metallicity is also shown [diamonds represent age of 0.2 Gyr for each metallicity (colour-coded) and the following circles on the line correspond to 0.5, 1, 2, 5, 10 and 15 Gyr, respectively]. Note the scatter for  $K_{S2MASS} - K$ , illustrating the need of independent fits for the different stellar populations.

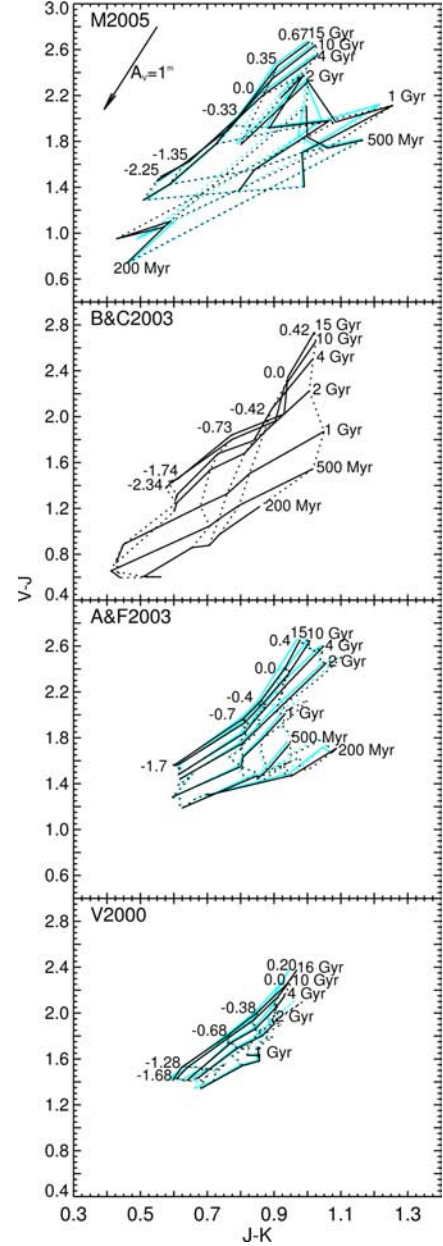
system. For the purposes of this work, we transform the near-IR colours predicted by the models to the 2MASS system. To do so, we convolved SEDs provided by Bruzual & Charlot (2003) with the filter transition curves from Bessell & Brett (1988) and (Skrutskie et al. 2006) using the IRAF/STSDAS SYNPHOT package. Synthetic near-IR colours and magnitude differences were derived for a wide age–metallicity parameter space. The differences between the synthetic 2MASS and Bessell & Brett magnitudes as a function of  $(J - K_S)_{2MASS}$  colour are presented in Fig. C2. It is obvious that different transformation equations should be applied for the different populations as a function of metallicity, especially for  $K$  and  $K_S$ . We derived a set of transformation equations adequate for our purposes:

$$J_{2MASS} = J_{BB88} + [a_J(J - K)_{BB88} + b_J], \quad (C1)$$

$$H_{2MASS} = H_{BB88} + [a_H(J - K)_{BB88} + b_H], \quad (C2)$$

$$K_{S2MASS} = K_{BB88} + [a_{K_S}(J - K)_{BB88} + b_{K_S}]. \quad (C3)$$

The transformation coefficients as a function of metallicity are listed in Table C1. These transformations were used to recompute the model colours. As an example, the differences between the original and the transformed model grids are shown in  $(V - J)$  versus  $(J - K)$  colour–colour space in Fig. C3. The grids for the Bessell & Brett



**Figure C3.** Illustration of the variance of model grids computed in the photometric systems of Bessell & Brett (1988; in cyan) and 2MASS (in black).  $(V - J)$  versus  $(J - K)$  [ $(J - K_S)$  for 2MASS] for the models of Maraston (M2005), Anders & Fritze (A&F2003) and Vazdekis (V2000) are presented. The models of Bruzual & Charlot (B&C2003) were originally computed in the 2MASS photometric system. The ages are given on the right-hand side of the isochrones and the metallicities are labelled along the oldest isochrone for each model. A reddening vector corresponding to one magnitude of visual extinction is shown in the top panel.

(1988)  $JHK$  system used by the Maraston (2005), Anders & Fritze-v. Alvensleben (2003) and Vazdekis (1999) models are shown in cyan and the corresponding grids using the 2MASS system are shown in black. We use the 2MASS system for the subsequent analysis.

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