

## PONTIFICIA UNIVERSIDAD CATOLICA DE CHILE ESCUELA DE INGENIERIA

# EVALUATION AND IMPROVEMENT OF THE CLIGEN MODEL FOR STORM AND RAINFALL EROSIVITY GENERATION IN CENTRAL CHILE

#### GABRIEL P. LOBO

Thesis submitted to the Office of Research and Graduate Studies in partial fulfillment of the requirements for the Degree of Master of Science in Engineering

Advisor:

**CARLOS A. BONILLA** 

Santiago de Chile, September 2014

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This thesis is dedicated to my family for their endless love and encouragement.

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#### **ABSTRACT**

CLIGEN (CLImate GENerator) is a stochastic weather generator that produces daily estimates of precipitation and individual storm parameters, including time to peak, peak intensity and storm duration. These parameters are typically used as inputs for other models, such as the Water Erosion Prediction Project (WEPP) model. Although CLIGEN has proven to be effective for predicting daily estimates, some discrepancies have been observed when generating storm parameters, such as the storm duration. Therefore, a study was conducted to evaluate and improve CLIGEN for storm generation. Individual rainfall events were identified from 1-h pluviograph records that were collected from 30 sites in Central Chile. In this study, 415 years of data were used; 18,012 storms were analyzed. In addition, rainfall erosivity was computed for all storms using the prescribed method to compare the energy provided by the measured and generated rainfall events. Using measured rainfall data, a procedure was developed to improve the CLIGEN estimates by calibrating the input parameter that controls the storm durations. This procedure in turn improved the rainfall intensities and erosivities. The model was tested before and after calibration with the measured rainfall data from the 30 sites in both the wet and the dry seasons. Based on a monthly rainfall analysis, the results demonstrated that the number of storms and rainfall amounts, which are not affected by the calibration process, were accurately estimated with CLIGEN. However, before the calibration, especially in the wet season, the storm durations and maximum intensities were consistently overestimated and underestimated at most of the sites and for most months. Therefore, the annual rainfall erosivities were underestimated with CLIGEN at 19 of the 30 sites. After performing the calibration, the R<sup>2</sup> value for the CLIGEN-generated storm durations increased from 0.41 to 0.65. The maximum intensities also exhibited an improvement; the R<sup>2</sup> value increased from 0.31 to 0.60. Consequently, annual rainfall erosivities were generated with an R<sup>2</sup> value of 0.89; these erosivities were accurately estimated at 29 of the 30 sites. Therefore, this calibration procedure proved to be an effective alternative for generating more reliable storm

patterns. The to the indivi			in deta	iil and analyz	zes the	parametei	rs related
<b>Keywords:</b> generator, W	rainfall	erosivity,	storm	generation,	water	erosion,	weather

#### **RESUMEN**

CLIGEN es un modelo estocástico de simulación de clima capaz de estimar las precipitaciones diarias y la distribución de las intensidades y duración de cada tormenta. Dichas variables son necesarias para los modelos de erosión de base física como el Water Erosion Prediction Project (WEPP). A pesar de que CLIGEN ha sido validado para las variables diarias de precipitación, este no ha mostrado buenos resultados para la simulación de las tormentas, en especial en la estimación de su duración. En el presente estudio se propone un método para lograr que CLIGEN simule tormentas más parecidas a las reales. Se identificaron eventos de lluvias a partir de registros horarios de precipitación provenientes de 30 estaciones meteorológicas ubicadas en la zona central de Chile y se analizaron más de 415 años de datos y 18.012 tormentas. Además se calculó la erosividad de las tormentas para poder comparar la energía cinética aportada por los eventos de lluvia simulados y medidos. A partir de los datos medidos de precipitación, se desarrolló un método para calibrar el parámetro de entrada que controla la duración y la intensidad de los eventos de lluvia en CLIGEN. Se implementó el modelo antes y después de calibrar utilizando datos medidos de las 30 estaciones meteorológicas. A partir de una comparación a nivel mensual se comprobó que CLIGEN simuló adecuadamente el número de tormentas y el agua caída por tormenta, variables que no dependen del parámetro calibrado. Sin embargo, antes de calibrar, el modelo sobreestimó y subestimó la duración y las intensidades de las tormentas, respectivamente, en la mayoría de las estaciones. Debido a esto, CLIGEN subestimó la erosividad anual en 19 de 30 estaciones. Después de calibrar, el modelo generó mejores resultados de duración, aumentando el R<sup>2</sup> de 0.41 a 0.65. Las intensidades máximas también mejoraron con la calibración, aumentando el R<sup>2</sup> de 0.31 a 0.60. A causa de esto mejoró significativamente la estimación de erosividad anual, la cual fue correctamente simulada en 29 de 30 estaciones después de calibrar. Por lo tanto, se demuestra que el método de calibración es una alternativa para simular tormentas más precisas utilizando CLIGEN. Este documento explica detalladamente dicho método y analiza diversos parámetros asociados a la simulación de tormentas.

Palabras clave: CLIGEN, ero	osion hídrica, er	osividad, genera	dor de climas, si	mulación
de tormentas, WEPP				

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#### 1. INTRODUCTION

#### 1.1. Overview

Soil conservation practices have become of increasing importance over the last decades. As world population increases, fertile land is reduced and land use is intensified, often leading to soil degradation (Pieri et al., 2006). One of the most important causes of soil degradation is water erosion, a process that causes loss of fertile soil and pollution of surface waters (Carpenter et al., 1998). Water erosion is a problem that stems from a combination of agriculture and intense rainfall, and may be exacerbated in the future because of more demanding agriculture and climatic change (Amore et al., 2004). Because of this, controlling water erosion to preserve soil and water quality and to maintain agricultural productivity has become of worldwide concern and one of the most pressing environmental issues (Pieri et al., 2006).

To prevent soil degradation, water erosion prediction has been used since 1940 as a tool for selecting soil conservation practices and other regulatory approaches (Laflen et al., 1997). Two kind of models have been developed for this purpose: empirically based models, such as the Revised Universal Soil Loss Equation (RUSLE) (Foster, 2008), and process-based models such as the Kinematic Runoff and Erosion Model (KINEROS) (Woolhiser et al., 1990) and the Water Erosion Prediction Project (WEPP) model (Flanagan and Nearing, 1995). Compared to the empirical, the process-based models provide several advantages such as the estimation of spatial and temporal distributions of soil loss and the flexibility to use the model under a wide range of conditions (Flanagan and Nearing, 1995).

A model like WEPP combines a process-based hydrology model, a daily water balance model, a plant growth and residue decomposition model, a soil consolidation model and a climate generator (Flanagan and Nearing, 1995). Fig. 1.1 provides a flow chart of the WEPP erosion prediction model system.

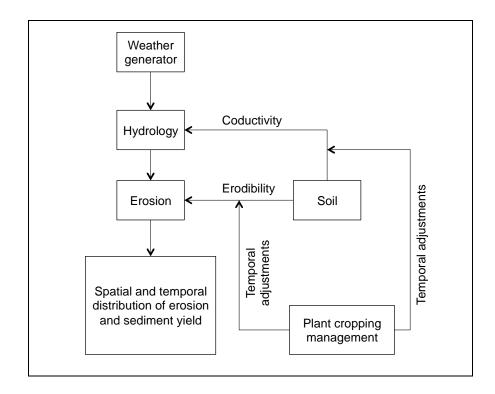


Figure 1.1. Flow chart of the WEPP erosion prediction model system (Adapted from Flanagan and Nearing (1995)).

CLIGEN (CLImate GENerator), the stochastic climate generator incorporated in WEPP, uses historical data to simulate daily precipitation, maximum, minimum and dew point temperatures, solar radiation and wind velocity and direction, as well as the temporal distribution of storms (Kou et al., 2007). Among the commonly used stochastic daily weather generators, CLIGEN is the only one capable of simulating storm patterns (Zhang et al., 2008), which is crucial to get reliable soil loss estimates. This is because the rainfall intensities directly affect rill and interril erosion by controlling the peak runoff rate, storm runoff amount and the shear stress (Yu, 2000).

CLIGEN can be used for filling short climatic records, generating daily weather series in areas where there is no climatic records through spatial interpolation and for generating a variety of future climates to assess the potential impacts of climate changes on hydrological and natural resources (Yu, 2005; Zhang, 2005). However, since the model was released it has been subject to major changes such as the calibration of its

equations with new available data, and the implementation of subroutines for random number generation for data quality control (Zhang & Garbrecht, 2003). Errors in the model's source code were also uncovered and fixed for several of the model's routines (Yu, 2000). Nonetheless, the current version of CLIGEN (v5.3) still has shown some problems when estimating storms duration and relative peak intensity. These variables control the kinetic energy of the simulated rainfall (Foster, 2008) and thus highly affect the WEPP soil loss estimates (Zhang et al., 2008). Therefore, the objective of this study was to develop and validate a methodology to increase the accuracy of CLIGEN for storm generation. In this way, the purpose was to simulate a more reliable rainfall kinetic energy and more precise soil loss estimates when using WEPP. A better water erosion estimation with WEPP would be more suitable for designing and implementing soil conservation practices to reduce or reverse soil degradation and increase soil productivity.

#### 1.2. Objectives

The objective of this study was to evaluate CLIGEN for storm generation in Central Chile and to develop a procedure to improve its performance. For this purpose, the following activities were performed:

- 1) Construction of CLIGEN climatic input files as suggested by the authors of the model for 30 meteorological stations located in Central Chile.
- 2) Construction of CLIGEN climatic input files using a calibration procedure developed in this study for the same 30 meteorological stations
- 3) Validation of the calibration procedure by comparing the measured and the generated number of storms, total rainfall depth per storm, time to peak, storm durations and storm intensities, before and after the calibration.
- 4) Comparison between the generated and the measured rainfall erosivities before and after the calibration to verify if by calibrating the model there is a significant change on the erosive power of the rainfall.

#### 2. LITERARY REVIEW

CLIGEN is a stochastic weather generator that simulates daily precipitation, maximum, minimum and dew point temperatures, solar radiation and wind velocity and direction (Nicks et al., 1995). Among the commonly used stochastic daily weather generators, CLIGEN is the only model capable of simulating the temporal distribution of storms (Zhang et al., 2008). Because the rainfall intensity affects rill and interrill erosion by controlling the runoff rate and shear stress (Yu, 2000; Pieri et al., 2007), CLIGEN has been incorporated as part of the physically-based Water Erosion Prediction Project (WEPP) model interfaces (Flanagan and Nearing, 1995).

Previous studies have reported that CLIGEN can acceptably simulate daily precipitation occurrence and total rainfall (Johnson et al., 1996; Zhang and Garbrecht, 2003). However, only a limited number of studies have evaluated the temporal distribution of storms (Yu, 2000; Zhang and Garbrecht, 2003; Zhang, 2005; Zhang et al., 2008). These studies have reported that the weather generator tends to overestimate the duration of brief storms and underestimate the duration of prolonged storms, which results in inadequate intensity estimations (Headrick and Wilson, 1997; Zhang and Garbrecht, 2003). In particular, when the storm durations are underestimated, the intensities are overestimated, increasing the erosive power of the rainfall generated by the model (Zhang and Garbrecht, 2003). This result was reported by Yu (2002) when using CLIGEN to generate the R-factor of the Revised Universal Soil Loss Equation (RUSLE) (Renard et al., 1997) for various sites in the US. By comparing generated and measured erosivity values, Yu's study showed that CLIGEN overestimated the R-factor at every site, which indicates that the storm durations and intensities were underestimated and overestimated, respectively.

Yu (2000), Zhang and Garbrecht (2003) and Zhang (2005) suggested that the equations used in CLIGEN for storm patterns should be modified because they do not adequately simulate storms. However, none of these studies proposed a specific change in the equations or a method for obtaining more reliable storm patterns when using CLIGEN. Therefore, the objective of this study was to develop and test a method to

improve CLIGEN-generated storm patterns without modifying the model's equations and source code. The method was tested using 30 meteorological stations located in Central Chile and more than 415 years of hourly precipitation data.

#### 2.1. CLIGEN model for storm generation

CLIGEN version 5.3 generates daily precipitation occurrence and amount and internal storm variables, such as peak storm intensity, duration and time to peak. Rainfall occurrence is predicted using a first-order two-state Markov chain, which utilizes monthly probabilities of precipitation occurrence for a wet day following a wet day and for a wet day following a dry day from daily historical precipitation data. When a precipitation event is predicted, the rainfall amount is calculated using the following skewed normal distribution (Nicks et al., 1995):

$$\mathbf{x} = \frac{6}{g} \left\{ \left[ \frac{g}{2} \left( \frac{R - \mu}{s} \right) + 1 \right]^{\frac{1}{3}} - 1 \right\} + \frac{g}{6}$$
 (1)

where x is a standard normal deviate, R is the generated daily precipitation amount (mm) and  $\mu$  (mm), s (mm) and g are the mean, standard deviation and skewness coefficient of the daily precipitation amounts for the month, respectively. The values of  $\mu$ , s and g are directly extracted from historical data, while two random numbers are used to generate the normal deviate (x), which is then used to estimate the daily rainfall amount (R).

Storm intensities are generated using a double exponential function, which assumes that rainfall rates increase exponentially until the peak storm intensity is attained and subsequently decrease in the same way (Nicks et al., 1995). The peak storm intensity is calculated using the following equation proposed by Arnold and Williams (1989):

$$r_{p} = -2R\ln(1 - \alpha_{0.5}) \tag{2}$$

where  $r_p$  is the peak storm intensity (mm h<sup>-1</sup>), R is the daily precipitation amount (mm) and  $\alpha_{0.5}$  is a dimensionless parameter defined as the ratio of the maximum 0.5-h rainfall amount to the daily precipitation amount. The value of  $\alpha_{0.5}$  is determined from a two-parameter gamma distribution described by Sharpley and Williams (1990) with a shape

parameter set to 6.28 and a scale parameter that is computed using the mean of  $\alpha_{0.5}$  ( $\alpha_{0.5mean}$ ) for the month (Zhang and Garbrecht, 2003). The latter is calculated as follows:

$$\alpha_{0.5\,\text{mean}} = \frac{R_{0.5\,\text{mean}}}{R_{\text{mean}}} \tag{3}$$

where  $R_{0.5mean}$  is the monthly mean of the maximum 0.5-h rainfall amount (mm) and  $R_{mean}$  is the monthly mean precipitation amount per storm (mm). Furthermore,  $R_{0.5mean}$  is calculated using the following equation (Sharpley and Williams, 1990; Zhang and Garbrecht, 2003):

$$R_{0.5\,\text{mean}} = \begin{cases} -\frac{R_{0.5\,\text{max}}}{\ln\left(\frac{2}{2\,n+1}\right)} & n > 2.18\\ R_{0.5\,\text{mean}} & n \le 2.18 \end{cases}$$

$$(4)$$

where  $R_{0.5max}$  is the mean of the annual 0.5-h maximum amount for each month (mm) and n is the average number of rainy days for a given month (Yu, 2005). The values of  $R_{0.5max}$  must be estimated for each month by the user from historical rainfall data.

The storm duration is computed for every storm as follows:

$$D = -\frac{0.5\Delta}{\ln(1 - \alpha_{0.5})}\tag{5}$$

where D is the storm duration (h) and  $\Delta$  is a dimensionless parameter set to 3.99 in CLIGEN v5.3 based on the calibration of Yu (2000). Both equations (2) and (5) are subject to modification as more historical precipitation data are analyzed (Nicks et al., 1995).

Once the rainfall amount per storm (R), peak intensity  $(r_p)$  and duration (D) are computed for a single storm, the relative peak intensity  $(i_p)$  is calculated using the following ratio:

$$i_p = \frac{r_p D}{R} \tag{6}$$

Then, the relative storm intensity for the entire event is computed using the following double exponential function:

$$i(t) = \begin{cases} i_{\rho} e^{b(t-t_{\rho})} & 0 \le t < t_{\rho} \\ i_{\rho} e^{d(t_{\rho}-t)} & t_{\rho} \le t \le 1 \end{cases}$$

$$(7)$$

where i(t) is the relative storm intensity at relative time t,  $t_p$  is the relative time to peak and b and d are parameters that are determined using the assumptions and procedures described in Nicks et al. (1995). The time to peak is a parameter that must be estimated by the user from historical data.

#### 3. MATERIALS AND METHODS

#### 3.1. Meteorological stations and climatic data

The data used in this study were obtained from the 30 meteorological stations shown in Table 3.1, which are located in Central Chile and distributed between latitudes 32° 04' S and 39° 47' S (Fig. 3.1).

Table 3.1. Meteorological stations used in this study. The length of the hourly rainfall records may be shorter than the measurement period because of missing data.

Station Name	Latitude	Longitude	Elevation (m.a.s.l.)	Years of hourly rainfall records	Measurement period
Pedernal	32°05'	70°48'	1100	21	1972-1992
Sobrante	32°14'	70°47'	810	21	1972-1992
Los Vientos	32°50'	70°60'	130	4	2007-2011
Rancagua	32°50'	70°60'	170	10	2004-2013
Quillota	32°54'	71°13'	130	10	1982-1991
Lliu Lliu	33°06'	71°13'	260	14	1979-1992
Pirque	33°40'	70°35'	670	2	1979-1980
Melipilla	33°41'	71°12'	170	18	1975-1992
Rengo	34°25'	70°52'	310	23	1970-1992
Popeta	34°26'	70°47'	400	6	1970-1974
C. Las Nieves	34°30'	70°43'	700	22	1971-1992
Potrero Grande	35°11'	71°06'	460	21	1972-1992
Fundo el Peral	35°24'	71°47'	110	13	1974-1986
Colorado	35°38'	71°16'	420	24	1969-1992
Melozal	35°46'	71°47'	110	22	1971-1992
Ancoa Embalse	35°54'	71°17'	430	22	1971-1992
Bullileo	36°17'	71°25'	600	22	1971-1992
Chillán Viejo	36°38'	72°06'	125	9	1984-1992
Colhueco	36°39'	71°48'	300	8	1984-1992
Caracol	36°39'	71°23'	620	6	1987-1992
Diguillin	36°52'	71°39'	670	28	1965-1992
Quilaco	37°41'	71°60'	225	28	1965-1992
Cerro el Padre	37°47'	71°52'	400	17	1976-1992
El Vergel Angol	37°49'	72°39'	75	5	1976-1981
Contulmo	38°01'	73°14'	25	4	1987-1992
Traiguen	38°15'	72°40'	170	5	1988-1992
Manzanar	38°28'	71°42'	790	17	1972-1988
Pueblo Nuevo	38°44'	72°34'	100	4	1989-1992
Freire Sendos	38°58'	72°37'	100	3	1985-1987
Pucón	39°17'	71°57'	230	9	1984-1992

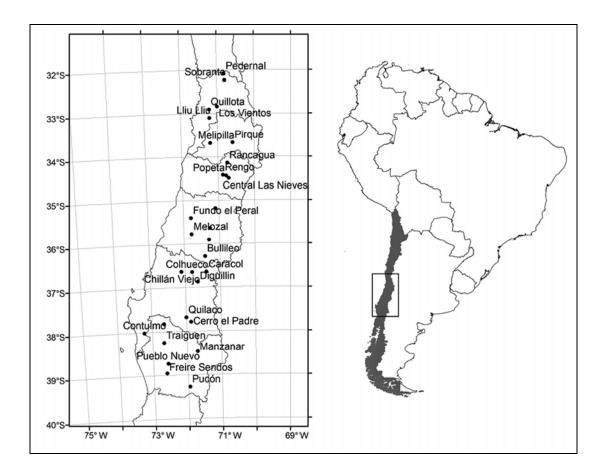


Figure 3.1. Spatial distribution of the meteorological stations used in this study.

The stations are part of two national rain gauge networks managed by the Dirección General de Aguas (DGA) and the Sistema Nacional de Calidad del Aire (SINCA). These stations were selected according to the availability of hourly measured rainfall data, which ranged from 3 to 28 years. These stations provided data for 418 years and 18,012 storms. The climate in this region of Chile is primarily semi-arid. Rainfall is typically generated by frontal systems and is highly erosive in some areas. Moreover, precipitation amounts increase with increasing latitude (Escobar and Aceituno, 1998; Bonilla and Vidal, 2011). CLIGEN input files were constructed for each station based on hourly and daily rainfall data and other measured data that are required by the model, such as maximum, minimum and dew point temperatures, solar radiation and wind velocity and direction.

#### 3.2. Uncalibrated input file preparation

A first set of input files was constructed for the 30 sites mentioned in section 3.1 using existing meteorological information. Because 0.5-h rainfall data are not typically recorded in Chile, these values were estimated from hourly data by fitting the following intensity-duration-Frequency (IDF) curve proposed by Wenzel (1982):

$$I = \frac{K}{D^n + b} \tag{8}$$

where I is the storm's mean intensity (mm h<sup>-1</sup>) for duration D (h) and K, n and b are dimensionless parameters that are fitted for every storm. The intensities for durations of 1-6 h were computed and a non-linear regression technique was used to fit the data. Then, the 0.5-h maximum precipitation amount was calculated for each storm and the maximum value for every month was averaged for every year, yielding the monthly  $R_{0.5max}$  parameters. CLIGEN also requires 0.5-h and 6-h rainfall amounts with a return period of 100 years to control extreme values. These two values were calculated for every station using the IDF curves developed by Pizarro et al. (2010).

#### 3.3. Calibrated input file preparation

To increase the accuracy of CLIGEN-generated storm durations, a second set of 30 input files was constructed for the same meteorological stations; however, this set of input files was formulated using a two-step calibration procedure. The calibration consisted of computing  $R_{0.5max}$  parameters that lead to storm durations that more closely correspond to the measured values by manipulating the equations used in CLIGEN. This calibration was performed by combining Eqs. (3) and (4) and solving for  $R_{0.5max}$  as follows:

$$R_{0.5\,\text{max}} = \begin{cases} -R_{\text{mean}} \alpha_{0.5\,\text{mean}} \ln\left(\frac{2}{2\,n+1}\right) & n > 2.18 \\ R_{\text{mean}} \alpha_{0.5\,\text{mean}} & n \le 2.18 \end{cases}$$

$$(9)$$

Assuming that when  $\alpha_{0.5} \approx \alpha_{0.5 \, mean}$ , Eq. (5) yields the mean storm duration of a given month, the following expression is obtained by combining Eq. (5) solved for  $\alpha_{0.5}$  and Eq. (9):

$$R_{0.5\,\text{max}} = \begin{cases} R_{\text{mean}} \left[ e^{-0.5\Delta/D} - 1 \right] \ln \left( \frac{2}{2\,n+1} \right) & n > 2.18 \\ -R_{\text{mean}} \left[ e^{-0.5\Delta/D} - 1 \right] & n \le 2.18 \end{cases}$$
(10)

Then, using Eq. (10) for every month with the generated  $R_{mean}$  and n and measured D values, the resulting  $R_{0.5max}$  yields generated durations in CLIGEN that are closer to the measured values. The generated  $R_{mean}$  and n values must be used in Eq. (10) because in CLIGEN the storm duration is computed using the generated and not the measured values. By using Eq. (10) the input parameter  $R_{0.5max}$  becomes redefined and loses its physical meaning.

Eq. (10) was used to compute the monthly values of  $R_{0.5max}$  for the calibrated climatic input files. This calculation was performed using CLIGEN for a 100-year simulation with the uncalibrated input files and extracting the average monthly n and  $R_{mean}$  values from the generated data. Then, the average monthly D values were extracted from the measured data to be used in Eq. (10). Fig. 3.2 provides a summary of the procedure used to calibrate the  $R_{0.5max}$  parameter for every month. This procedure adjusts the  $\alpha_{0.5}$  for every month in Eq. (5), as  $\alpha_{0.5}$  depends on  $R_{0.5max}$ . An alternative option would be to calibrate  $\Delta$  in Eq. (5) by changing the source code, however, this is not as effective as calibrating  $\alpha_{0.5}$  because  $\Delta$  is not a month-dependent parameter.

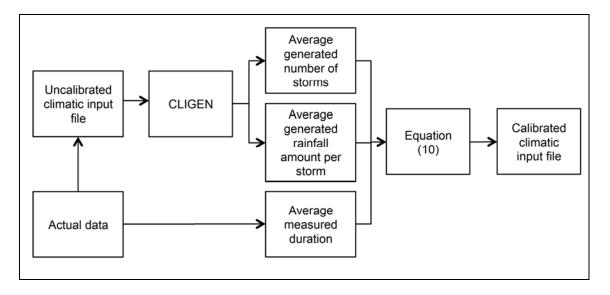


Figure 2.2. Procedure used to calibrate the climatic input files. The procedure is applied in every month to yield the monthly  $R_{0.5max}$  parameters.

#### 3.4. Evaluation methods

CLIGEN was used to generate climatic data for all of the sites using both the uncalibrated and calibrated input files. The generated rainfall was compared with the measured data based on the monthly number of storms, total rainfall amount per storm, mean intensity, 1-h maximum intensity and storm duration. The time to peak was compared on an annual basis because this parameter is not month-dependent. To test the equality of the measured and generated distributions for all parameters, the nonparametric Kolmogorov-Smirnov test (K-S) was applied with a significance level of 0.05. The K-S test was chosen because rainfall parameters do not often exhibit normal distributions (Zhang et al., 2008). The mean values and standard deviations for all variables were also compared.

Furthermore, the annual rainfall erosivity was computed for both the measured and generated rainfall data using the equations described by Foster (2008). This calculation was performed to evaluate whether differences in storm durations and intensities between the measured and generated data can affect the erosive power of the rain. As demonstrated by Yu (2002), there is a substantial effect of poorly predicted

storm durations and storm intensities on erosivity. Thus, rainfall kinetic energy for each measured and generated storm was calculated as follows (Foster, 2008):

$$E = \sum_{r=1}^{m} 0.29 \left[ 1 - 0.72 \exp(-0.082 i_r) \right] \Delta V_r$$
 (11)

where E is the kinetic energy of the storm (MJ mm ha<sup>-1</sup> h<sup>-1</sup>),  $i_r$  is the rainfall intensity for the  $r^{th}$  period (mm h<sup>-1</sup>) and  $\Delta V_r$  is the rainfall amount (mm) for the  $r^{th}$  increment of the storm hyetograph, which is divided into m intervals. Each storm's energy is then multiplied by the maximum amount of rain falling within 30 consecutive minutes ( $I_{30}$ ) expressed in mm h<sup>-1</sup> to obtain the storm's erosivity. Because the available data were recorded hourly,  $I_{30}$  was estimated for every storm using the IDF curve and the procedure described in section 2.2 to determine the measured erosivity. Finally, the annual erosivity was calculated by adding all the storm's erosivities for a year, and then averaging every year. Moreover, the means and standard deviations of both the measured and generated erosivities were compared; the K-S test was used to evaluate the equality of the measured and generated distributions.

#### 4. RESULTS AND DISCUSSION

The results presented herein are a comparison of the measured and the generated number of storms, precipitation amount per storm, time to peak, storm duration, storm intensities and rainfall erosivity for both the calibrated and uncalibrated input files. The calibration only affects the durations and the intensities because they are the variables in CLIGEN that depend on the  $R_{0.5max}$  parameter. The erosivity is also affected by the calibration because it depends on the storm durations and intensities.

Table 4.1 shows the results of the statistical analysis applied on a monthly basis to the storm parameters of the 30 stations, before and after the calibration. CLIGEN adequately estimated the number of storms for nearly all stations between September and March (the dry season), which corresponds to a period in which there are typically less than five rainfall events per month. However, during the wet season, the accuracy of the model decreased, especially in June where the measured and generated number of storms were statistically equal in 18 of the 30 stations (Table 4.1). This occurred because CLIGEN overpredicted the number of storms in months with more than five rainfall events (see Fig. 4.1). Fig. 4.1 compares the measured and generated monthly average number of storms at the 30 sites. These results are consistent with the findings of Wilks (1992) and Zhang and Garbrecht (2003), who showed that CLIGEN produces reliable results when there are few storms per month and becomes less reliable as the number of storms increases. However, the generated mean number of storms was correlated to the measured values in most months (R<sup>2</sup> value of 0.77). This result demonstrates that the first-order two-state Markov chain that is used to determine the precipitation occurrence in CLIGEN is appropriate, which was also shown by Koutsoyiannis (1994) and Wilks (1999).

Table 4.1. Results of the statistical analysis applied on a monthly basis to the storm parameters of the 30 stations, before and after calibration. For each storm parameter and month, the table shows the number of stations where the generated and measured values were equal according to the K-S test. The calibration process does not affect the number of storms and rainfall amount per storm.

	Nun	nber of st	ations out				the CLIGEN-go	enerated storm
Month	Storm duration		Mean rainfall intensity		ers were statistically 1-h maximum intensity		Number of storms	Rainfall amount per storm
	Before	After	Before	After	Before	After		
January	20	18	27	25	29	27	28	28
February	21	24	28	30	27	29	27	28
March	20	24	29	28	29	29	28	29
April	6	20	24	20	24	24	26	24
May	2	7	25	26	15	24	24	23
June	6	11	26	27	13	23	18	20
July	5	13	23	25	12	25	26	23
August	4	11	27	26	15	28	22	28
September	5	14	23	24	18	30	27	27
October	11	18	23	26	19	29	27	26
November	15	20	30	26	28	29	26	27
December	19	20	26	27	24	26	30	26
Average	11.2	16.7	25.9	25.8	21.1	26.9	25.8	25.8

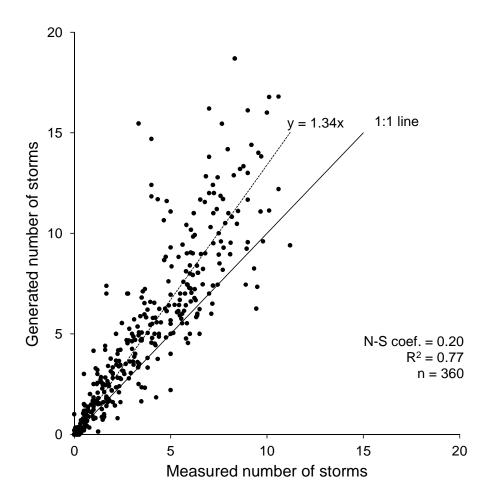


Figure 3.1. Comparison between measured and generated monthly average number of storms at the 30 sites.

The average rainfall amount per storm was accurately generated using CLIGEN when less than 15 mm of rain fell per event (Fig. 4.2), which is typical for rainfall events in the dry season. Fig. 4.2 compares the measured and the generated monthly average rainfall amount per storm at the 30 sites. These results are consistent with Table 4.1, which shows that the measured and generated rainfall amounts per storm were statistically equivalent at nearly every station in the dry season. However, in the wet season, when the rainfall amount per storm increases, the number of stations at which the rainfall amount was correctly estimated decreased, especially in June. This same

result was reported by both Zhang and Garbrecht (2003) and Kou et al. (2007), in which CLIGEN generated accurate rainfall amounts for small storms and became less accurate as the rainfall amount increased. However, as shown in Table 4.1, the rainfall amounts per storm were correctly estimated at most stations using CLIGEN regardless of the month. In addition, the mean values were adequately simulated in most months, i.e., an R<sup>2</sup> value of 0.77 and a Nash-Sutcliffe (N-S) efficiency value of 0.69. This finding demonstrates the effectiveness of the skewed normal distribution used in the model, which was previously shown by Elliot and Arnold (2001).

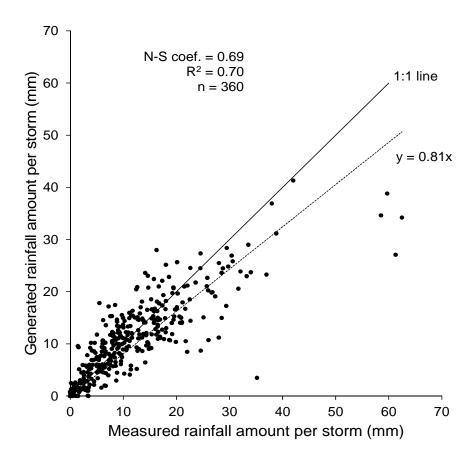


Figure 4.2. Comparison between measured and generated monthly average rainfall amounts per storm at the 30 sites.

The times to peak generated by CLIGEN were nearly identical to the measured values (data not shown), which is consistent with the findings of Zhang et al. (2008). Out of the 30 meteorological stations, only two stations (Pirque and Freire Sendos)

reported different times to peak after the K-S test. Because these two stations had the shortest measurement data sets, the length of the available records may have affected the K-S test more than the quality of the CLIGEN generated data. Nevertheless, at all of the stations, the differences between the means and standard deviations of the measured and generated times to peak were less than 3%.

Based on the K-S test, Table 4.1 also shows the number of meteorological stations at which the measured and generated storm durations, mean intensities and maximum 1-h intensities were equivalent before and after the calibration. Without the calibration, most of the generated storm durations were significantly different than the measured values, especially in the wet season. Before the calibration, the model consistently overpredicted the storm durations. This result is shown in Fig. 4.3, which compares the measured and the generated monthly average storm durations at the 30 sites before and after the calibration. In many cases, the CLIGEN-generated storms lasted 24 h, which is the maximum amount of time that a storm can last in the model (Nicks et al., 1995). This phenomenon occurs particularly in Central Chile because of the frontal nature of storms in this region, which makes the storm intensities nearly constant. According to Eq. (5), the storm duration depends only on the parameter  $\alpha$ as storm's duration increases as α decreases. The parameter  $\alpha$ is defined as the ratio of the maximum 0.5-h rainfall amount to the daily precipitation amount. In a frontal storm, α is typically small because the maximum 0.5-h intensity is nearly identical to the mean intensity. Therefore, CLIGEN tends to generate frontal storms with extended durations, showing that  $\alpha$ is not a robust predictor for the durations of this type of storms. However, because  $R_{0.5max}$  was estimated using an IDF curve before the calibration and  $R_{0.5max}$  affects  $\alpha$  , part of the error when estimating storm duration could be associated to the assumption that the maximum 0.5-h rainfall intensity can be estimated using an IDF curve. Appendix B shows how using an alternative method to compute the maximum 0.5-h rainfall intensity affects the estimation of  $R_{0.5max}$ .

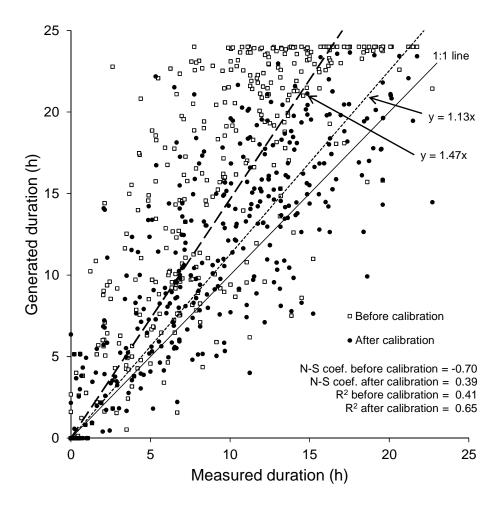


Figure 4.3. Comparison between measured and generated monthly average storm durations at the 30 sites. The data are shown before and after the calibration. The dashed and dotted lines show the linear regressions before and after calibrating CLIGEN, respectively.

As shown in Table 4.1, the number of stations at which the CLIGEN-generated durations were equivalent to the measured values increased after the calibration. However, nearly half of the stations still reported differences between the measured and the generated storm durations. The primary effect of the calibration can be observed in Fig. 4.3, which shows that the means of the generated storm durations are closer to the measured values after calibrating the model. After the calibration, the N-S efficiency and R<sup>2</sup> values increased from -0.70 to 0.39 and from 0.41 to 0.65, respectively. The new

storm durations were compared with the same measured data that were used to calibrate them because the purpose of this process is to generate the same mean duration as the one of the measured data. Because CLIGEN did not precisely reproduce the mean storm durations after the calibration, it is possible to conclude that the assumption used to derive Eq. (10) is not accurate for all cases. In addition, part of the error can also be attributed to the fact that CLIGEN smoothes the monthly  $R_{0.5max}$  values for the calculation of D, which is not considered in the calibration.

The standard deviations of the generated storm durations were consistently smaller than the measured values. This result is demonstrated by the variation coefficients of the samples, which ranged from 0.02 to 0.4 and from 0.8 to 1.2 for the generated and measured storm durations respectively. This finding suggests that the storm durations in Central Chile are more variable than those predicted using CLIGEN. Therefore, even though the proposed calibration process produces storm durations that more closely resemble the observed durations, their standard deviations remain different. The model does not incorporate duration variability in its equations. Hence, the only source of variability lies in the gamma distribution that generates the  $\alpha_{0.5}$  value described in Eq. (5), which does not accurately represent the variability of the storm durations.

Fig. 4.4 shows a comparison between the measured and the generated monthly average mean rainfall intensities at the 30 sites before and after the calibration. With the calibration, the R<sup>2</sup> value increased from 0.31 to 0.60, while the N-S efficiency decreased from 0.14 to 0.12. Moreover, Table 4.1 shows that most of the generated mean storm intensities were statistically equivalent to the measured values regardless of the calibration. This finding shows that the differences between the average mean storm intensities shown in Fig. 4.4 were not statistically significant.

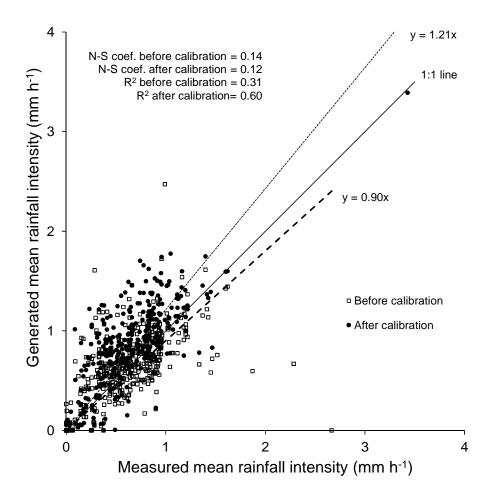


Figure 4.4. Comparison between the measured and the generated monthly average mean rainfall intensities at the 30 sites. The data are shown before and after the calibration.

The dashed and dotted lines show the linear regressions before and after calibrating CLIGEN, respectively.

Fig. 4.5 compares the measured and the generated monthly average maximum 1-h storm intensities before and after calibrating the climatic data files. Prior to the calibration, the model consistently underpredicted the 1-h maximum intensities. After the calibration, the results improved. The R<sup>2</sup> value increased from 0.36 to 0.63, while the N-S efficiency increased from 0.19 to 0.46. This finding is supported by the data in Table 4.1, especially in the rainy months, with a significant increment in the number of stations where the measured and generated 1-h maximum intensities were equivalent

after the calibration. Because the model generated more accurate mean storm durations after the calibration and because the total rainfall was correctly estimated, the storm intensities were also correctly estimated.

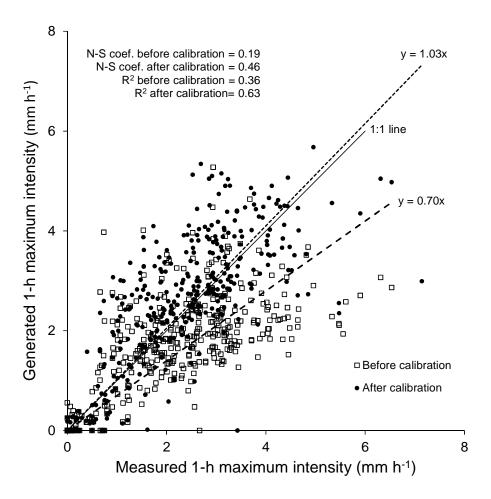


Figure 4.5. Comparison between the measured and the generated monthly average 1-h maximum storms intensities at the 30 sites. The data are shown before and after the calibration. The dashed and dotted lines show the linear regressions before and after calibrating CLIGEN, respectively.

Fig. 4.6 shows a comparison between the generated and the measured mean annual erosivities before and after the calibration at the 30 sites. CLIGEN generated better estimations of erosivity when the calibration was used. The R<sup>2</sup> and the N-S efficiency values increased from 0.66 to 0.89 and from 0.49 to 0.86, respectively. Before

the calibration, CLIGEN underestimated the maximum storm intensities; therefore, the kinetic energies and the rainfall erosivities were also underestimated. After the calibration, the maximum intensities were more accurately estimated, especially in the rainy months, which is when the erosivity is concentrated in the study area (Bonilla and Vidal, 2012).

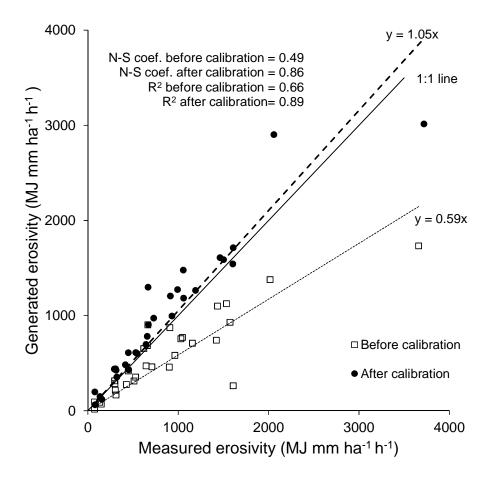


Figure 4.6. Comparison between the measured and generated annual rainfall erosivities. The data are shown before and after calibrating CLIGEN for the 30 sites. The dashed and dotted lines show the linear regressions before and after calibrating CLIGEN, respectively.

Because the average number of storms, rainfall amount per storm, storm durations and storm intensities were adequately estimated after the calibration, CLIGEN also provided

better erosivity results. Out of the 30 meteorological stations, 11 reported statistically equivalent values of erosivity before the calibration, while 29 stations were statistically equivalent after the calibration. This result demonstrates that CLIGEN generated erosivity values with the same means and standard deviations as the measured data even though the standard deviations of the storm durations were not accurately estimated. Therefore, the storm duration variability does not significantly affect the erosivity variability. Hence, the variable portions of the storms that are not represented in CLIGEN must have low intensities and a minimal effect on erosivity, which is typical during the formation and weakening of storms.

Because erosivity was accurately estimated using CLIGEN after the calibration and erosivity is directly proportional to erosion, soil loss estimates using WEPP will be more accurate when using the calibrated climatic data files. Moreover, because rainfall occurrence and amount increases as the latitude increases in Chile, it is possible to conclude that the effectiveness of the calibration is independent of these variables. However, because this calibration was tested on only frontal storms, there is no evidence that this procedure will work as well for other climate types. The method will, however, be effective in areas where frontal storms are predominant.

### 5. CONCLUSIONS

The calibration method developed in this study is simple to implement and improves CLIGEN-generated storms without modifying the source code and the model's equations. By calibrating the input parameter that controls storm durations, the correlation between measured and generated durations increased. The calibration in turn improved the rainfall intensities and erosivities.

Before the calibration, the mean storm durations were poorly predicted using CLIGEN at almost every site and month. After the calibration, the results improved significantly. However, the model failed to replicate the variability in the storm durations regardless of the calibration, which is because the gamma distribution used in CLIGEN to generate the storm durations produces results that are less variable than the actual durations. Furthermore, after the calibration, the generated 1-h maximum storm intensities were estimated more accurately, especially during the wet season, which is the season with the largest effect on water erosion in the study area. After the calibration, the model failed to replicate rainfall erosivity at one of the 30 sites, while before the calibration, the model failed at 19 sites. This finding demonstrates that improving the storm duration estimates was sufficient to yield accurate rainfall intensity erosivity estimates.

Even though the calibration method proposed was used and validated in Central Chile, the method should be effective in other places with similar geography and where frontal storms are predominant because the calibration procedure does not depend on the number of storms or the rainfall amount. The only requirement for using the method is the availability of rainfall data measured at small time intervals, such as every hour. Therefore, the calibration method is a tool that can be used with the current version of CLIGEN because no source code modification is required. Because the equations for estimating the storm durations and maximum intensities are still subject to modification, the calibration can be used to simulate these parameters with improved accuracy until new equations are implemented and validated.

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## **APPENDIX**

### APPENDIX A. BOX PLOTS OF VARIOUS STORM PARAMETERS

The figures presented herein provide box plots for the number of storms, rainfall amount per storm, time to peak, storm duration, mean rainfall intensity, 1-h maximum rainfall intensity and rainfall erosivity of the measured and generated data of Bullileo station before and after the calibration. The number of storms, rainfall amount per storm and time to peak are not affected by the calibration process.

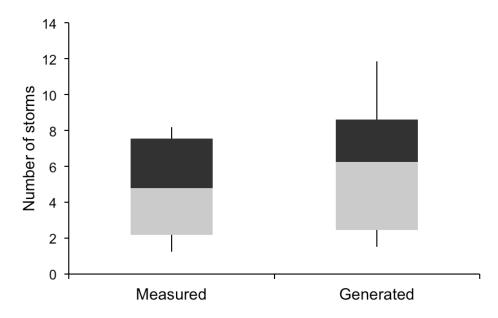


Figure A1. Box plots of the measured and generated number of storms for Bullileo station.

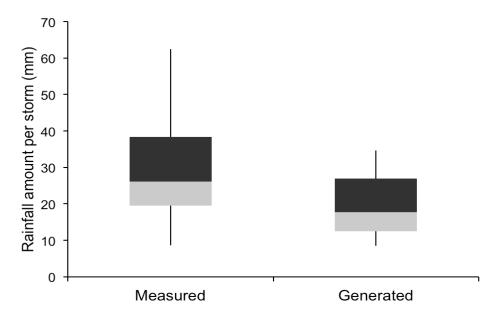


Figure A2. Box plots of the measured and generated rainfall amount per storm for Bullileo station.

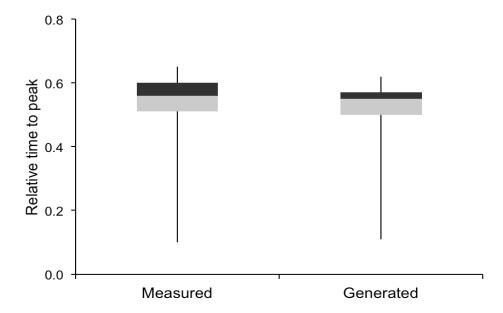


Figure A3. Box plots of the measured and generated relative time to peak for Bullileo station.

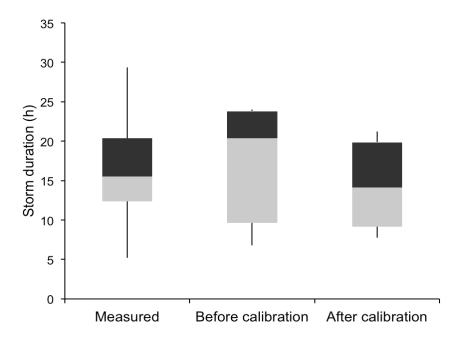


Figure A4. Box plots of the measured and generated storm duration before and after the calibration for Bullileo station.

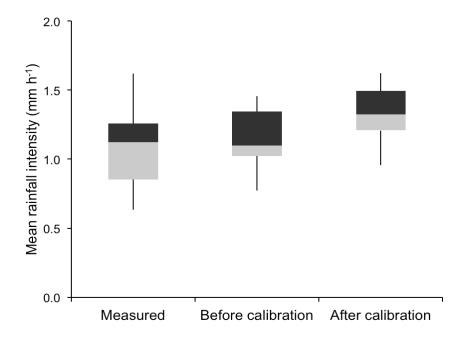


Figure A5. Box plots of the measured and generated mean rainfall intensity before and after the calibration for Bullileo station.

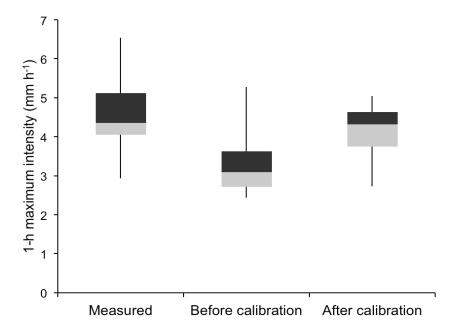


Figure A6. Box plots of the measured and generated 1-h maximum rainfall intensity before and after the calibration for Bullileo station.

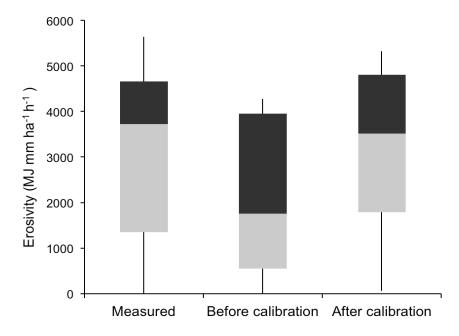


Figure A7. Box plots of the measured and generated rainfall erosivity before and after the calibration for Bullileo station.

# APPENDIX B. AN ALTERNATIVE METHOD TO COMPUTE THE MAXIMUM 0.5-H RAINFALL INTENSITY

In this study, the maximum 0.5-h rainfall intensity was computed for each storm using the IDF curve described in section 3.3. The results obtained for every storm were used to compute the monthly  $R_{0.5\text{max}}$  parameters that are required to run CLIGEN. The results show that the model does not accurately generate storm parameters that are related to  $R_{0.5\text{max}}$  (storm duration and intensity), which is why the calibration procedure was developed. However, the inaccuracy of CLIGEN prior to the calibration could have been due to the assumption that the maximum 0.5-h rainfall intensity can be estimated using an IDF curve. To test this hypothesis, the monthly  $R_{0.5\text{max}}$  were computed for all the stations using the global equation proposed by Bell (1969) that relates 0.5-h and 1-h maximum rainfall amounts. The average  $R_{0.5\text{max}}$  of all the stations yielded by Bell's equation, the IDF curve and the calibration method are compared in the following chart:

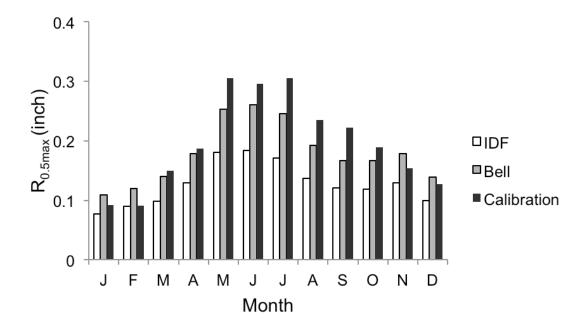


Figure B1. Average  $R_{0.5\text{max}}$  of all the stations using Bell's equation, Wenzel's IDF curve and the calibration method

As shown, Bell's equation provides higher  $R_{0.5max}$  results than the IDF curve, and is generally closer to the calibrated  $R_{0.5max}$ . However, significant differences exist between the  $R_{0.5max}$  parameters obtained using Bell's equation and the calibration method. This demonstrates that, when using Bell's equations for the estimation of  $R_{0.5max}$ , the generated storm patterns will be imprecise in the study sites, making the calibration process a necessary step for accurate storm patterns generation using CLIGEN.

## APPENDIX C. LIST OF SYMBOLS

Table C1. List of symbols

Symbol	Meaning	Type
$\overline{n}$	Average number of storms per month	Monthly output
R	Generated daily precipitation amount (mm)	Generated for each storm
μ	Mean of the daily precipitation amount (mm)	Monthly input
S	Standard deviation of the daily precipitation amount (mm)	Monthly input
g	Skewness coefficient of the daily precipitation amount	Monthly input
x	Standard normal deviate used in CLIGEN to compute R	Generated for each storm
$r_p$	Peak storm intensity (mm h <sup>-1</sup> )	Generated for each storm
$lpha_{0.5}$	Ratio of the maximum 0.5-h rainfall amount to the daily precipitation amount	Generated for each storm
$R_{0.5mean}$	Monthly mean of the maximum 0.5-h rainfall amount (mm)	Generated for each storm
$R_{mean}$	Monthly mean precipitation amount per storm (mm)	Generated for each storm
$R_{0.5max}$	Mean of the annual 0.5-h maximum amount for each month (mm)	Monthly input
D	Storm duration (h)	Generated for each storm
Δ	Parameter used to compute storm duration	Fixed value
	Relative storm intensity at relative time t	Generated for each storm
$i_p$	Relative peak intensity	Generated for each storm
$t_p$	Relative time to peak	Generated for each storm

# APPENDIX D. HYETOGRAPH SAMPLE OF BULLILEO STATION

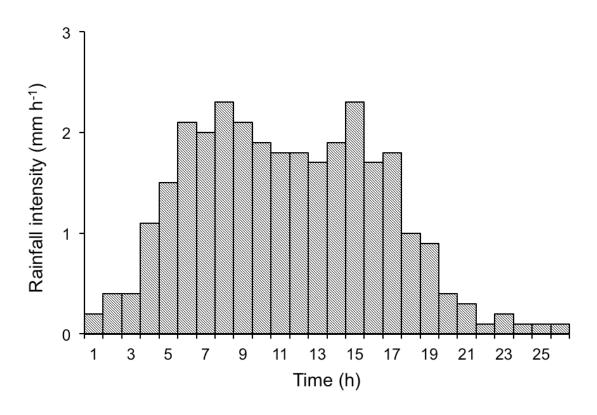


Figure D1. Hyetograph of a storm at Bullileo station

### APPENDIX E. CLIGEN CLIMATIC INPUT FILE SAMPLE

Bulliled	CHL					9999	999 0					
LATT= -3		LONG= -	-71.41	YEARS:	= 23. 1	TYPE= 2	2					
ELEVATI(	ON =	10. TF	P5 = 0.	.63 TP6	5= 3.36	5						
MEAN P	0.51	0.71	0.63	0.85	1.34	1.33	1.19	1.00	0.80	0.62	0.45	0.48
S DEV P	0.63	1.13	0.87	1.20	1.38	1.33	1.20	1.13	0.88	0.72	0.59	0.61
SKEW P	2.16	2.37	2.01	2.70	1.79	1.80	1.67	2.20	1.62	1.59	2.19	2.07
P(W/W)	0.16	0.20	0.25	0.46	0.62	0.70	0.63	0.61	0.54	0.53	0.40	0.34
P(W/D)	0.04	0.05	0.06	0.14	0.17	0.26	0.22	0.24	0.18	0.16	0.11	0.07
TMAX AV	84.81	84.00	79.13	69.43	59.67	54.69	54.03	57.95	62.83	68.02	74.14	80.56
TMIN AV	53.57	52.81	50.06	45.36	42.94	41.91	39.31	40.80	42.28	44.88	48.65	52.02
SD TMAX	5.48	6.17	6.34	7.31	6.15	5.16	5.02	5.58	6.15	6.19	6.57	6.67
SD TMIN	3.82	4.25	5.02	6.48	6.99	7.23	7.33	6.92	5.42	5.43	4.62	4.40
SOL.RAD	660.2	587.6	472.8	310.3	175.8	142.4	172.1	218.6	356.2	446.7	602.4	592.0
SD SOL	105.2	109.8	109.9	106.7	92.6	77.4	86.8	113.9	126.7	187.2	158.3	203.5
MX .5 P	0.29	0.21	0.21	0.22	0.33	0.29	0.38	0.26	0.19	0.21	0.23	0.18
DEW PT	48.44	47.28	48.34	45.41	43.82	42.86	42.15	42.59	42.50	45.02	44.19	47.02
Time Pk	0.011	0.059	0.119	0.217	0.301	0.409	0.502	0.606	0.713	0.790	0.897	1.000
% N	6.58	7.76	11.82	15.77	17.10	22.82	13.17	17.04	15.95	14.54	8.33	10.14
MEAN	0.30	0.37	0.26	0.42	0.75	0.60	0.78	0.54	0.46	0.26	0.33	0.30
STD DEV	0.20	0.28	0.05	0.39	0.86	0.50	0.72	0.64	0.27	0.12	0.25	0.11
SKEW	4.18	2.71	1.12	2.63	2.42	2.30	2.27	6.65	3.81	7.26	3.48	1.02
% NNE	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
MEAN	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
STD DEV	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
SKEW	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

Figure E1. Climatic input file of Bullileo station

Each line of the climatic input file represents a climatic parameter, while the columns represent months. January is first column, while is December the last one. Time to peak (Time Pk) is the only exception since the columns represents the accumulated relative frequency of the time to peak divided into 12 classes. The meaning of each parameter of the climatic input file is shown in the followinf table:

Table E1. Parameters of the CLIGEN climatic input files

Meaning
Latitude in degrees of the meteorological station
Longitude in degrees of the meteorological station
Number of years of observed data
Predominant storm type of the site (Type I, IA, II or III)
Elevation of the station (ft)
Maximum 0.5-h rainfall amount with a return period of 100 years (inch)
Maximum 6-h rainfall amount with a return period of 100 years (inch)
Mean rainfall amount (inch)
Standard deviation of the rainfall amount (inch)
Skewness of the rainfall amount
Probability of a wet day following a wet day
Probability of a wet day following a dry day
Mean daily maximum temperature (F)
Mean daily minimum temperature (F)
Standard deviation of the daily maximum temperature (F)
Standard deviation of the daily minimum temperature (F)
Mean of the daily solar radiation (langley)
Standard deviation of the daily solar radiation (langley)
Mean of the annual 0.5-h maximum amount (inch)
Mean dew point temperature (K)
Relative time to peak
Percentage of times when the wind blows north
Mean of the wind velocity when it blows north (m s <sup>-1</sup> )
Standard deviation of the wind velocity when it blows north (m s <sup>-1</sup> )

### APPENDIX F. WENZEL'S IDF CURVE ADJUSTED TO A STORM

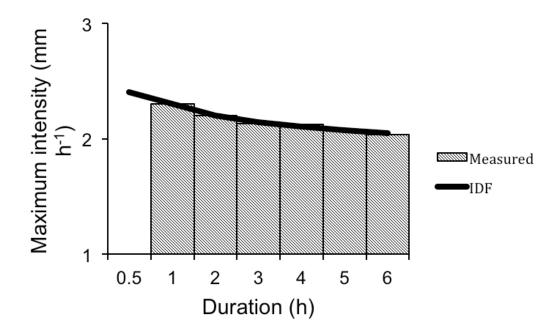


Figure F1. Wenzel's IDF curve adjusted to a sample storm of Bullileo station